### Multi-mode Acoustic Gravitational-wave Experiment (MAGE)















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## **QDM Lab Precision Metrology**

### **Metrological Systems:**

**Photonic** 

- WGM Resonators
- Specially Designed Microwave Cavities





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(b)



### **Motivation: Fundamental Physics**



### Axion Detector are Sensitive to Ultra-High Frequency GWs (UHFGWs) Inverse Gertsenshtein effect

PHYSICAL REVIEW D 105, 116011 (2022)

### Detecting high-frequency gravitational waves with microwave cavities

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Asher Berlin,<sup>1,2,3</sup> Diego Blas,<sup>4,5</sup> Raffaele Tito D'Agnolo<sup>®</sup>,<sup>6</sup> Sebastian A. R. Ellis<sup>®</sup>,<sup>7,6</sup>
Roni Harnik,<sup>2,3</sup> Yonatan Kahn,<sup>8,9,3</sup> and Jan Schütte-Engel<sup>®</sup>,<sup>8,9,3</sup>
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$$j_{\text{eff}} \supset g_{a\gamma\gamma}\partial_{l}a\mathbf{B}_{0} \simeq \omega_{a}\theta_{a}\mathbf{B}_{0} \qquad \mathbf{E}_{a} = g_{a\gamma\gamma}a\mathbf{B}_{0} = \theta_{a}\mathbf{B}_{0}$$

$$j_{\text{eff}}^{\mu} \equiv \partial_{\nu}\left(\frac{1}{2}hF^{\mu\nu} + h_{\alpha}^{\nu}F^{\alpha\mu} - h_{\alpha}^{\mu}F^{\infty\nu}\right)$$

$$j_{\text{eff}} \sim \omega_{g}hB_{0}$$
identifying  $\theta_{a} \sim h$ 

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Living Reviews in Relativity (2021)24:4 https://doi.org/10.1007/s41114-021-00032-5

#### **REVIEW ARTICLE**

#### Challenges and opportunities of gravitational-wave searches at MHz to GHz frequencies

Nancy Aggarwal<sup>1</sup> · Odylio D. Aguiar<sup>2</sup> · Andreas Bauswein<sup>3</sup> · Giancarlo Cella<sup>4</sup> · Sebastian Clesse<sup>5</sup> · Adrian Michael Cruise<sup>6</sup> · Valerie Domcke<sup>7,8,9</sup> · Daniel G. Figueroa<sup>10</sup> · Andrew Geraci<sup>11</sup> · Maxim Goryachev<sup>12</sup> · Hartmut Grote<sup>13</sup> · Mark Hindmarsh<sup>14,15</sup> · Francesco Muia<sup>9,16</sup> · Nikhil Mukund<sup>17</sup> · David Ottaway<sup>18,19</sup> · Marco Peloso<sup>20,21</sup> · Fernando Quevedo<sup>16</sup> · Angelo Ricciardone<sup>20,21</sup> · Jessica Steinlechner<sup>22,23,24</sup> · Sebastian Steinlechner<sup>22,23</sup> · Sichun Sun<sup>25,26</sup> · Michael E. Tobar<sup>12</sup> · Francisco Torrenti<sup>27</sup> · Caner Ünal<sup>28</sup> · Graham White<sup>29</sup>

Received: 6 April 2021 / Accepted: 15 September 2021 © The Author(s) 2021

### **Precision Detectors: Sensitive to New Physics**

### comparing sensitivities









NIOBE









### DETECTOR COMPARISON: Defining Instrument Sensitivity independent of signal (Spectral): Also sensitive to GWs



**Comparing Instrument Spectral Sensitivity of Dissimilar** Electromagnetic Haloscopes to Axion Dark Matter and High Frequency Gravitational Waves

Special Issue

Edited by

The Dark Universe: The Harbinger of a Major Discovery

Michael E. Tobar \*<sup>10</sup>, Catriona A. Thomson, William M. Campbell, Aaron Quiskamp, Jeremy F. Bourhill, Benjamin T. McAllister, Eugene N. Ivanov and Maxim Goryachev



ADMX and ORGAN (purple) with current tuning locus (blue);

0.6-1.2 GHz for ADMX and 15.2 to 16.2 GHz for ORGAN

Symmetry, vol. 14, no. 10, 2165, 2022 Prof. Konstantin Zioutas



arXiv:2409.03019 Schnabel and Korobko

$$\theta_a = g_{a\gamma\gamma} a \sim h_g$$

$$SNR = \frac{1}{2\pi} \int_{-\infty}^{\infty} \frac{\Theta_a(j\omega)^2}{S_{\theta_N}(\omega)} d\omega = 4 \int_0^{\infty} \frac{\Theta_a(f)^2}{S_{\theta_N}^+(f)} df$$

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# MAGE

### Excluding PBH Binaries





#### General Relativity and Quantum Cosmology

[Submitted on 4 Jun 2025]

### Experimental Exclusion of Planetary Mass Primordial Black Hole Mergers

William M. Campbell, Leonardo Mariani, Michael E. Tobar, Maxim Goryachev

The multi-mode acoustic gravitational wave experiment (MAGE) is a high-frequency gravitational wave detection experiment featuring cryogenic quartz bulk acoustic wave resonators operating as sensitive strain antennas in the MHz regime. After 61 days of non-continuous data collection, we present bounds on the observable merger rate density of primordial black hole binary systems of chirp mass  $1.2 \times 10^{-4} M_{\odot} < \mathcal{M} < 1.7 \times 10^{-9} M_{\odot}$ . The maximum achieved limit on the merger rate density is  $\mathcal{R} > 1.3 \times 10^{18} \text{ kpc}^{-3} \text{yr}^{-1}$  which corresponds to constraining yearly mergers to a distance of reach on the order of the solar system, or  $1.0 \times 10^{-6}$  kpc during the observational period. In addition, we exclude significantly rare and strong events similar to those observed in previous predecessor experiments as non-gravitational background signals, utilising coincident analysis between multiple detectors.





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### Quartz Bulk Acoustic Wave Resonators

• Acoustic analogue to a Optical Fabry-Perot cavity.



### \* RESEARCH WITH ACOUSTIC RESONATORS @ UWA

- \* Search for High frequency GWs
- \* Detection of a Graviton
- \* Search for Scalar DM:
- \* Search for Lorentz invariance violations
- \* Improved constraints on minimum length models or Generalized Uncertainty Principle (GUP)

Scientific Reports Vol. 3, 2132 (2013)







# The Experiment

### Complex DAQ Chain.



# What does the data look like ?

 $v_{\rm s}(t) = V_{\rm s} \exp\left[-\beta_1 t\right] \sin \omega_0 t \,,$ 

We expect GWs to drive an acoustic mode -> decaying sinusoidal



$$p_{\rm s}(t) = \frac{V_{\rm s}}{\sqrt{2}} \frac{\beta_2}{\beta_2 - \beta_1} (\exp\left[-\beta_1 t\right] - \exp\left[-\beta_2 t\right]) \cos\phi,$$

$$q_{\rm s}(t) = \frac{V_{\rm s}}{\sqrt{2}} \frac{\beta_2}{\beta_2 - \beta_1} (\exp\left[-\beta_1 t\right] - \exp\left[-\beta_2 t\right]) \sin \phi,$$



- FPGAs mimics 32 lockin-amps, Phase is time dependent and equal to 2Hz
- Sampled at a frequency of 238 Hz
- -> data streams, broken into  $20 \times 2^{14}$  samples segments ~ 23 minutes of data

- Detector 1 Fourier Transforms
- Channel 0 is 4.993 MHz
- Channel 1 is 5.08 MHz

# What does the signal look like ?

Innermost Stable Circular Orbit PBH merger ring-up to some frequency fISCO  $4 \times 10^{-19}$  $f_{\rm ISCO} = 4400 \,{\rm Hz} \, \frac{M_{\odot}}{m_1 + m_2} \,, \quad (\hat{f}_{\rm use})_{2 \times 10^{-19}}$ For PBH of mass: 1\*10<sup>-4</sup> solar masses  $1 \times 10^{-19}$ Produces a strain h<sub>o</sub> proportional to the merger mass M and distance D  $h_0 \approx \frac{2}{D} \left(\frac{G\mathcal{M}}{c^2}\right)^{5/3} \left(\frac{\pi f}{c}\right)^{2/3}$ 10<sup>5</sup>  $10^{6}$  $10^{4}$  $10^{7}$ 1000 Reduced mass of binary system

# Be careful of signal duration



$$N_{\rm cycles} = \frac{f^2}{\dot{f}} \simeq 2.2 \times 10^6 \left(\frac{f}{\rm GHz}\right)^{-5/3} \left(\frac{m_{\rm PBH}}{10^{-9} \,\rm M_{\odot}}\right)^{-5/3},$$

$$\tau(f) \approx 83 \sec\left(\frac{m_{\rm PBH}}{10^{-12} \,{\rm M}_{\odot}}\right)^{-5/3} \left(\frac{f}{{\rm GHz}}\right)^{-8/3}$$

# MAGE operates in narrow bands in the MHz spectrum

Signal may only pass through detector band for a VERY brief moment in time.

# Introduce characteristic strain

Dimensionless quantity introduced to account for the frequency evolution of a strain signals. It is more convenient to use than strain  $h_{0.}$ 

The characteristic strain,  $h_c$ , excluded by the detector can be related to the strain amplitude  $h_0$  of a PBH in-spiral of binary chirp mass M by;

$$h_c^2 = (2f\tilde{h}(f))^2 = 2h_0^2 N_{\text{cycles}}(\mathcal{M}, f)$$

$$h_0 \approx \frac{2}{d} \left(\frac{G\mathcal{M}}{c^2}\right)^{5/3} \left(\frac{\pi f}{c}\right)^{2/3}$$

# Searching for a signal in a noisy detector output

Well known / solved problem in the case of stationary gaussian noise -> optimal / matched filter.

$$\underline{s(t)} = \underline{h(t)} + \underline{n(t)}$$

We wish to still be able to detect a signal in the case where the noise is larger than the signal contribution

$$|h(t)| \ll |n(t)|$$

# Matched filter

Introduce some filter function K(t)

It is critical we know / assume the form of our signal h(t)

$$\hat{s} = \int_{-\infty}^{\infty} dt \, s(t) K(t)$$

Then ask: "what is the form of K(t) that maximises the ratio of our signal expectation value to the noise"

The signal-to-noise ratio (in amplitude) is defined as S/N, where S is the expected value of  $\hat{s}$  when the signal is present, and N is the rms value of  $\hat{s}$  when the signal is absent. Since  $\langle n(t) \rangle = 0$ , we have

$$S = \int_{-\infty}^{\infty} dt (s(t)) K(t) \qquad N^{2} = [\langle \hat{s}^{2}(t) \rangle - \langle \hat{s}(t) \rangle^{2}]_{h=0} \\ = \int_{-\infty}^{\infty} dt \underline{h(t)} K(t) \qquad = \langle \hat{s}^{2}(t) \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \langle n(t)n(t') \rangle \qquad (7.4) \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0} \\ = \int_{-\infty}^{\infty} dt dt' K(t) K(t') \int_{-\infty}^{\infty} df df' e^{2\pi i f t - 2\pi i f' t'} \langle \tilde{n}^{*}(f) \tilde{n}(f') \rangle_{h=0}$$

# Matched filter

We have:

$$\frac{S}{N} = \frac{\int_{-\infty}^{\infty} df \, \tilde{h}(f) \tilde{K}^*(f)}{\left[\int_{-\infty}^{\infty} df \, (1/2) \underbrace{S_n(f)}_{\mathsf{N}} |\tilde{K}(f)|^2\right]^{1/2}} \,.$$

What is the K(f) that gives maximum S/N for a given h(t) ?

$$\tilde{K}(f) = \text{const.} \frac{\tilde{h}(f)}{S_n(f)}$$

Filter effectively weights the noisier detector regions

$$\left(\frac{S}{N}\right)^2 = 4 \int_0^\infty df \, \frac{|\tilde{h}(f)|^2}{S_n(f)}$$

Substitute K(f) back in to get this equation for the most optimal SNR

# Determining detector strain



# Implementing the matched filter.

#### def optimal\_filter(data, template, Fs, NFFT):

```
fft = np.fft.fft(data) # fourier transformed data
zero_pad = np.zeros(data.size - template.size) # zero pad template to match data size
template_pad = np.append(template, zero_pad)
fft_template = np.fft.fft(template_pad) # fourier transformed padded template
plt.plot()
power_dat, freq_PSD = plt.psd(data, Fs=Fs, NFFT = NFFT, visible = True)
freq_dat = np.fft.fftfreq(data.size)*Fs #fourier frequencies corresponding to data partition
power spec = np.interp(freq dat, freq PSD, power dat)
```

```
val_cal = np.max(template)
OF = np.fft.ifft(fft_template*fft_template.conjugate()/power_spec).real
K = val_cal/np.amax(OF)
```

```
df = np.abs(freq_dat[1] - freq_dat[2])
opt_filter = K * fft * fft_template.conjugate() / power_spec #optimal filter
dat_filt = np.fft.ifft(opt_filter) #revert to time domain for filter output
```

```
sigmasq = 2*(K**2 * fft_template * fft_template.conjugate() / power_spec).sum() * df
sigma = np.sqrt(np.abs(sigmasq))
SNR = np.abs(2*dat_filt) / (sigma)
return SNR, dat_filt
signal = 5e-16*np.exp(-t_sig/(tau1))
template = np.exp(-t_sig/(tau1))
```



template = np.exp(-t\_sig/(tau1))
zero\_pad = np.zeros(h.size - signal.size) # zero pad template to match data size
template\_pad = np.roll(np.append(signal, zero\_pad),50000)

h\_inject = template\_pad + np.abs(np.random.normal(0, 1.66\*np.std(h), size = len(h))) h\_inject2 = np.abs(np.random.normal(0, 1.66\*np.std(h), size = len(h)))

# **Determining Candidate Events**



- Transient energy impulses excite the crystal
- Distinguished from other non-Gaussian noise sources by implementing a template bank with multiple values of decay times  $\tau_b = \{\tau_1, ..., \tau_{\lambda}, ..., \tau_i\}$
- Selecting candidate triggers for which  $\rho$  is optimised for  $\tau \sim \tau_\lambda$

FIG. 2. Instantaneous vibrational energy of a single mode is plotted as a histogram for a 23 minute segment of data. The blue (orange) histogram represents the energy distribution before (after) optimal filtering. Both histograms clearly follow an expected  $\chi^2$  distribution, however the effect of optimal filtering greatly reduces the effective temperature at which events can be identified with SNR = 1.



### Applying the optimal filter

- -> SNR as a time series  $\rho(t)$
- -> represents SNR in excess narrowband fluctuations above the thermal Nyquist noise limit of the crystal
- -> SNR fits a thermal distribution
- -> Statistical coincidences of thermal noise



 $\tau = \tau_{\lambda}$ 

# What characteristic strain can be excluded?

$$h_{c,\lambda} > \underbrace{x_{\max,\lambda}}_{(2i\pi f)^2 + \tau_{\lambda}^{-1} + (2\pi f_{\lambda})^2} \Big|^{-1} \frac{f_{\lambda}}{\Delta f_{\lambda}}$$

For a single mode

However, we can exploit the multi-mode nature of MAGE and consider an in spiral signal that passes Through the band of *every* mode in both detectors

$$\rho^2 = 2 \int_0^\infty df \frac{N_{\text{cycles}}(f)h_0^2}{f^2 S_n(f)} \sim \frac{h_0^2}{2} \sum_{\lambda}^{N_\lambda} \frac{\Delta f_\lambda^2 N_{\text{cycles}}(f_\lambda)}{f_\lambda^2 h_n^2(f_\lambda)}$$

Choosing a threshold SNR>3 gives an exclusion to 97.7% confidence on minimum detectable h<sub>0</sub>

This can be converted in a corresponding distance of reach D for a PBH system of some mass M

Lower bounds determined by sampling rate



Binary system of equal PBH mass ~  $4.4 \times 10^{-3}M_{\odot}$  Emits maximal HFGW at f = 5 MHz during its innermost stable circular orbit (ISCO)

Maximum predicted merger rate for 100% PBH dark matter

### **ORGAN (Oscillating Resonant Group AxioN Experiment)**



ORGAN -Q







# Future Detector Networks







### Linkage Infrastructure Equipment and Facilities

Applicants may seek funding for:

- infrastructure, equipment and facility purchases, construction and installation
- salaries directly associated with creating and installing infrastructure, equipment or facilities
- leasing of infrastructure, equipment or facilities
- consortium membership costs, in the case of Australia's participation in the use of significant international-scale or national research facilities
- specialised computing facilities and software compilations, catalogues, clearing houses or bibliographies.

The objectives of the LIEF scheme are to:

- support excellent basic and applied research and research training through the acquisition of research equipment and infrastructure and access to national and international research facilities
- encourage Eligible Organisations to develop collaborative arrangements with other Eligible Organisations and/or Partner Organisations for the acquisition and use of research equipment and infrastructure or access to national and international facilities.

The LIEF scheme provides project funding of a minimum of \$150,000 per year to a maximum of 75% of the total direct cost of the eligible budget items. The grant duration is one year; or one to 5 years if the application is for leasing infrastructure, equipment or facilities, the construction of research infrastructure, or subscription or coordinated access to international facilities and major national facilities.