Tests of µ-e universality

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^{*} Supported by NSF PHY-1812402 and PHY-2113436, and by DOE DE-SC0013941

Outline

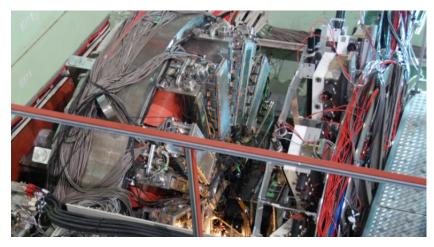
- τ-μ universality
 - B decays
- **μ**-e universality
 - B decays
 - g_μ-2
 - Proton radius puzzle: MUSE
 - Kaon decays: TREK/E36











Limits of lepton universality (until 2021)

- e, μ, and τ: Different masses, same gauge couplings
- Lepton universality has been rather well established at 10⁻³ 10⁻² level
- Summary by A. Pich, arXiv:1201.0537v1 [hep-ph] (2012)

	$\Gamma_{\tau \to \nu_{\tau} e \bar{\nu}_e} / \Gamma_{\mu \to \nu_{\mu} e \bar{\nu}_e}$	$\Gamma_{ au o u_{ au}\pi}/\Gamma_{\pi o \muar{ u}_{\mu}}$	$\Gamma_{\tau \to \nu_{\tau} K} / \Gamma_{K \to \mu \bar{\nu}_{\mu}}$	$\Gamma_{W \to \tau \bar{\nu}_{\tau}} / \Gamma_{W \to \mu \bar{\nu}_{\mu}}$
$ g_{ au}/g_{\mu} $	1.0007 ± 0.0022	0.992 ± 0.004	0.982 ± 0.008	1.032 ± 0.012
	$\Gamma_{\tau \to \nu_{\tau} \mu \bar{\nu}_{\mu}} / \Gamma_{\tau \to \nu_{\tau} e \bar{\nu}_{e}}$	$\Gamma_{\pi \to \mu \bar{\nu}_{\mu}} / \Gamma_{\pi \to e \bar{\nu}_{e}}$	$\Gamma_{K \to \mu \bar{\nu}_{\mu}} / \Gamma_{K \to e \bar{\nu}_{e}}$	$\Gamma_{K \to \pi \mu \bar{\nu}_{\mu}} / \Gamma_{K \to \pi e \bar{\nu}_{e}}$
$ g_{\mu}/g_{e} $	1.0018 ± 0.0014	1.0021 ± 0.0016	0.998 ± 0.002	1.001 ± 0.002
	$\Gamma_{W \to \mu \bar{\nu}_{\mu}} / \Gamma_{W \to e \bar{\nu}_{e}}$		$\Gamma_{ au o u_{ au}\muar{ u}_{\mu}}/\Gamma_{\mu o u_{\mu}ear{ u}_{e}}$	$\Gamma_{W \to \tau \bar{\nu}_{\tau}} / \Gamma_{W \to e \bar{\nu}_{e}}$
$\overline{ g_{\mu}/g_{e} }$	0.991 ± 0.009	$ g_{ au}/g_e $	1.0016 ± 0.0021	1.023 ± 0.011

$$\begin{array}{ll} \textbf{ Couplings to W and Z^0} \\ \textbf{ (LEP-II [PDG 2010])} \end{array} \qquad R_{\tau\ell}^W = \frac{2\,\mathrm{BR}\,(W \to \tau\,\overline{\nu}_\tau)}{\mathrm{BR}\,(W \to e\,\overline{\nu}_e) + \mathrm{BR}\,(W \to \mu\,\overline{\nu}_\mu)} = 1.055(23) \\ \end{array} \qquad \textbf{2.4}\sigma \ \text{dev.}$$

Belle, Babar, LHCb (HFLAV 2019)

$$\mathcal{R}(D^{(*)}) = \mathcal{B}(\overline{B} \to D^{(*)}\tau^{-}\overline{\nu}_{\tau})/\mathcal{B}(\overline{B} \to D^{(*)}\ell^{-}\overline{\nu}_{\ell})$$

3.6σ dev.

LHCb (March 2021)

$$BR(B^+\!\!\to K^+\mu^+\mu^-) \ / \ BR(B^+\!\!\to K^+e^+e^-) = 0.846^{+0.042}_{-0.039}^{} ^{}_{}$$

 3.1σ dev.

■ Muon anomalous mag. moment (Apr 2021) a_µ = 116 592 061(41) × 10⁻¹¹

4.2σ dev.

Proton charge radius puzzle (since 2010)

 $r_e (\mu H) = 0.84087 \pm 0.00039 \text{ fm}, r_e (CODATA2014) = 0.8751 \pm 0.0061 \text{ fm}$

5.6σ dev.

Limits of lepton universality (2023)

- e, μ, and τ: Different masses, same gauge couplings
- Lepton universality has been rather well established at 10⁻³ 10⁻² level
- Summary by A. Pich, arXiv:1201.0537v1 [hep-ph] (2012)

	$\Gamma_{\tau \to \nu_{\tau} e \bar{\nu}_e} / \Gamma_{\mu \to \nu_{\mu} e \bar{\nu}_e}$	$\Gamma_{\tau \to \nu_{\tau}\pi}/\Gamma_{\pi \to \mu \bar{\nu}_{\mu}}$	$\Gamma_{\tau \to \nu_{\tau} K} / \Gamma_{K \to \mu \bar{\nu}_{\mu}}$	$\Gamma_{W \to \tau \bar{\nu}_{\tau}} / \Gamma_{W \to \mu \bar{\nu}_{\mu}}$
$ g_{ au}/g_{\mu} $	1.0007 ± 0.0022	0.992 ± 0.004	0.982 ± 0.008	1.032 ± 0.012
	$\Gamma_{ au o u_{ au}\mu \bar{ u}_{\mu}}/\Gamma_{ au o u_{ au}e \bar{ u}_{e}}$	$\Gamma_{\pi \to \mu \bar{\nu}_{\mu}} / \Gamma_{\pi \to e \bar{\nu}_{e}}$	$\Gamma_{K \to \mu \bar{\nu}_{\mu}} / \Gamma_{K \to e \bar{\nu}_{e}}$	$\Gamma_{K \to \pi \mu \bar{\nu}_{\mu}} / \Gamma_{K \to \pi e \bar{\nu}_{e}}$
$ g_{\mu}/g_{e} $	1.0018 ± 0.0014	1.0021 ± 0.0016	0.998 ± 0.002	1.001 ± 0.002
	$\Gamma_{W \to \mu \bar{\nu}_{\mu}} / \Gamma_{W \to e \bar{\nu}_{e}}$		$\Gamma_{\tau \to \nu_{\tau} \mu \bar{\nu}_{\mu}} / \Gamma_{\mu \to \nu_{\mu} e \bar{\nu}_{e}}$	$\Gamma_{W \to \tau \bar{\nu}_{\tau}} / \Gamma_{W \to e \bar{\nu}_{e}}$
$\overline{ g_{\mu}/g_e }$	0.991 ± 0.009	$ g_{ au}/g_e $	1.0016 ± 0.0021	1.023 ± 0.011

Couplings to W and Z⁰

Couplings to
$$W$$
 and Z^0 (LEP-II [PDG 2010])
$$R_{\tau\ell}^W = \frac{2 \, \text{BR} \, (W \to \tau \, \overline{\nu}_\tau)}{\text{BR} \, (W \to e \, \overline{\nu}_e) + \text{BR} \, (W \to \mu \, \overline{\nu}_\mu)} = 1.055(23) \qquad \textbf{2.4} \sigma \, \, \text{dev.}$$

Belle, Babar, LHCb (Oct 2022+Mar 2023)

$$\mathcal{R}(D^{(*)}) = \mathcal{B}(\overline{B} \to D^{(*)}\tau^{-}\overline{\nu}_{\tau})/\mathcal{B}(\overline{B} \to D^{(*)}\ell^{-}\overline{\nu}_{\ell})$$

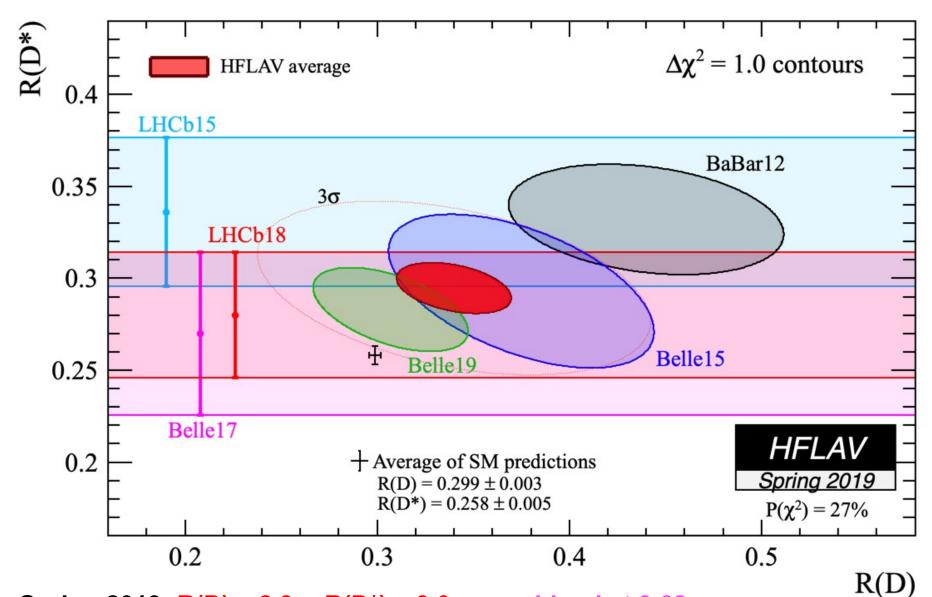
3.2σ dev.

LHCb (Dec 2022) $R(K^{(+,*)}) \sim 1.0$; dR $\sim 0.05-0.10$

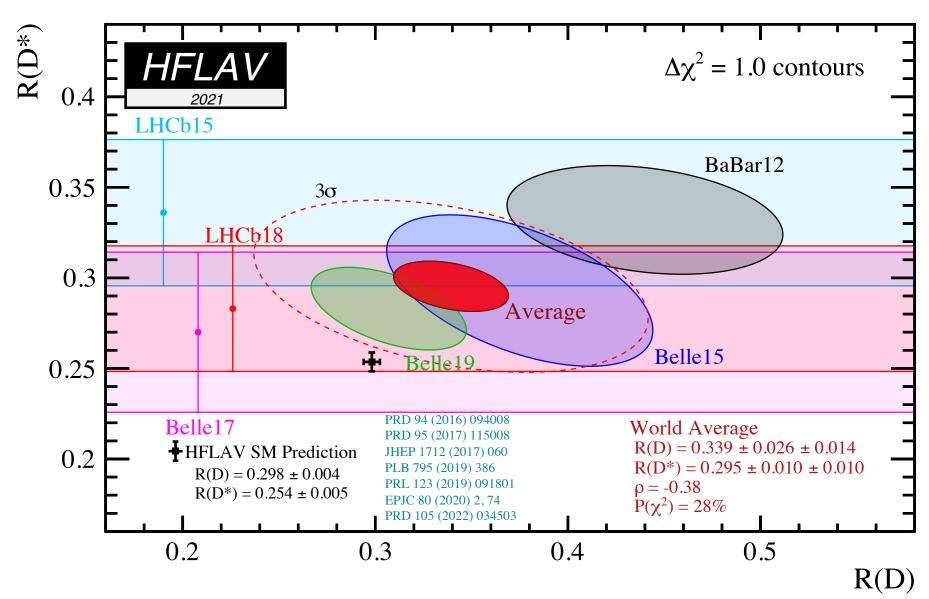
<1σ dev.

- Muon anomalous mag. moment (Apr 2021) $a_{\mu} = 116592061(41) \times 10^{-11}$ 4.2σ dev.
- Proton charge radius puzzle (June 2021) $r_e (\mu H) = 0.84087 \pm 0.00039 \text{ fm}, r_e (CODATA2018) = 0.8414(19) \text{ fm}$

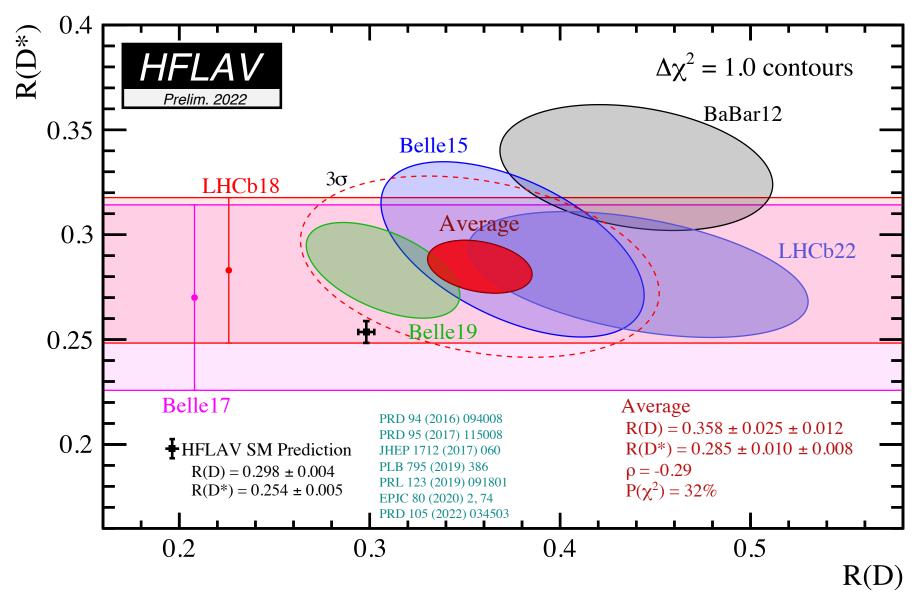
? 5.6σ dev. ?



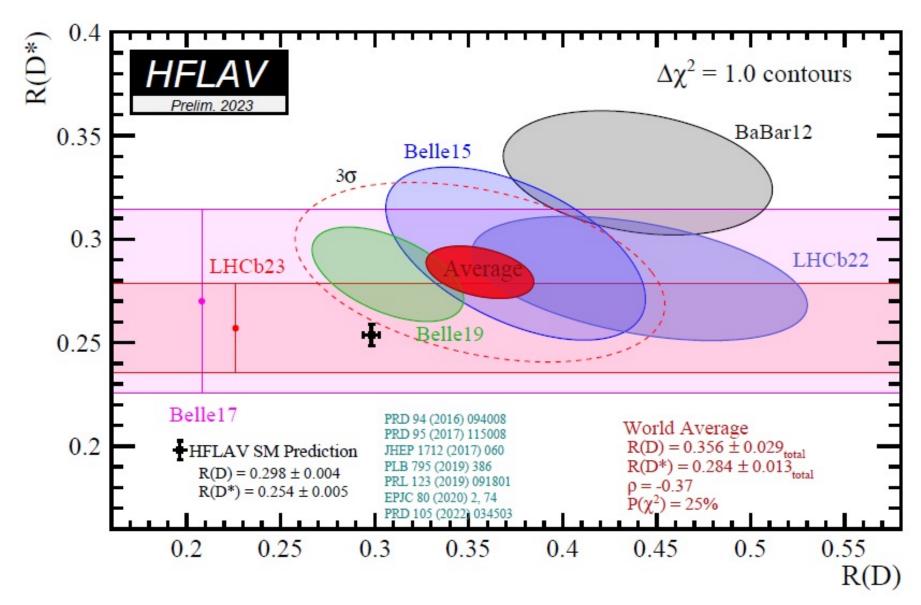
Spring 2019: R(D) ~ 2.3σ, R(D*) ~ 3.0σ; combined at 3.62σ



2021: R(D), R(D*) ~ combined at 3.3σ

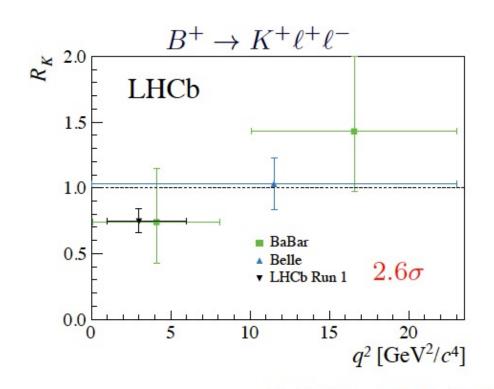


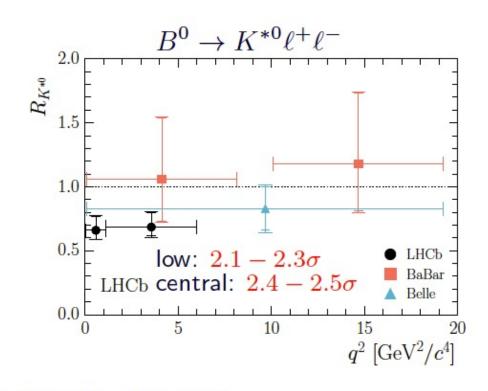
Oct. 2022: R(D), R(D*) ~ combined at 3.2σ



2023: R(D), R(D*) incl. hadronic-τ decays ~ combined at 3.2σ

- LHCb: $R(K^{(+,*)}) = \Gamma(B^{(+,0)} \rightarrow K^{(+,*)} \mu^+ \mu^-) / \Gamma(B^{(+,0)} \rightarrow K^{(+,*)} e^+ e^-)$
- Summer 2018: R(K^(+,*)) different from SM at the 2.5σ level





[LHCb, PRL 113 (2014) 151601] [LHCb, JHEP 08 (2017) 055] [BaBar, PRD 86 (2012) 032012] [Belle, PRL 103 (2009) 171801]

Challe R(K+) = $\Gamma(B^+ \rightarrow K^+ \mu^+ \mu^-) / \Gamma(B^+ \rightarrow K^+ e^+ e^-)$

Spring 2021: R(K+) different from SM at 3.1σ level

BaBar 0.1<\$q^2\$<8.12 \text{ GeV}^2\$/\$c^4 [PRD86032012]

[LHCb, PRL 113 (2014) 151601]

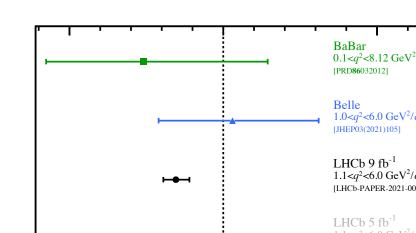
[BaBar, PRD 86 (2012) 032012]
[Belle, PRL 103 (2009) 171801]

LHCb 9 \text{ fb}^-1 \\
1.1<\$q^2\$<6.0 \text{ GeV}^2\$/\$c^4 [LHCb-PAPER-2021-004]

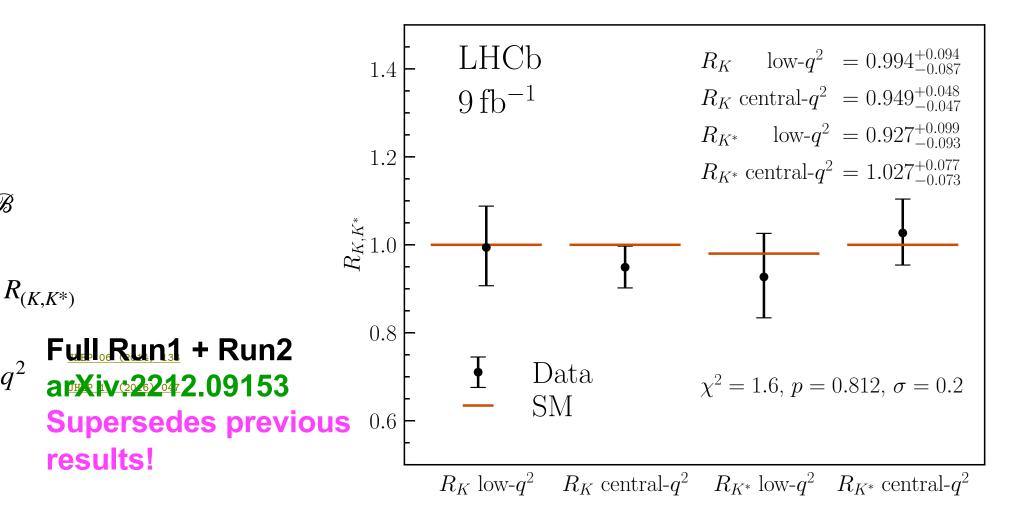
ith full Run 1 and Run 2 LHCb data

easured value of R_K is:

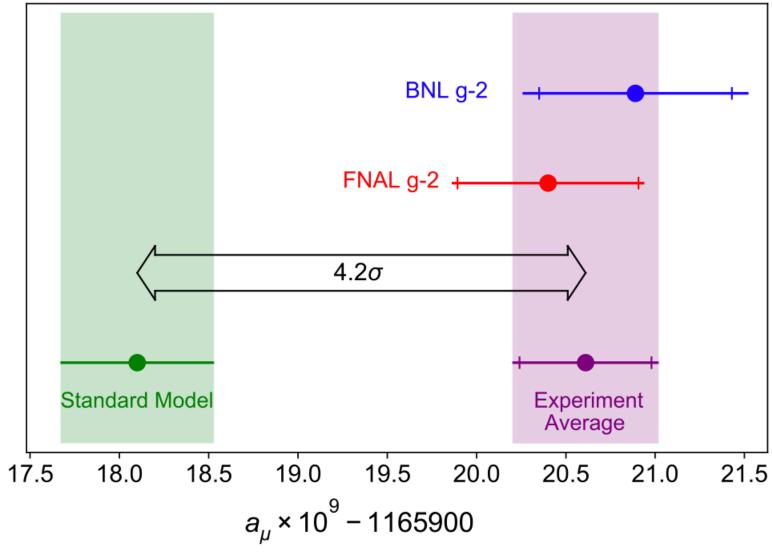
$$\kappa = 0.846^{+0.042}_{-0.039} \text{ (stat.)} ^{+0.013}_{-0.012} \text{ (syst.)}$$



- LHCb: $R(K^{(+,*)}) = \Gamma(B^{(+,0)} \rightarrow K^{(+,*)} \mu^+ \mu^-) / \Gamma(B^{(+,0)} \rightarrow K^{(+,*)} e^+ e^-)$
- December 2022: R(K(+,*)) consistent with Standard Model



Lepton non-universality: Muon g-2



The Muon g-2 Collaboration, Measurement of the Positive Muon Anomalous Magnetic Moment to 0.46 ppm, arXiv: 2104.03281

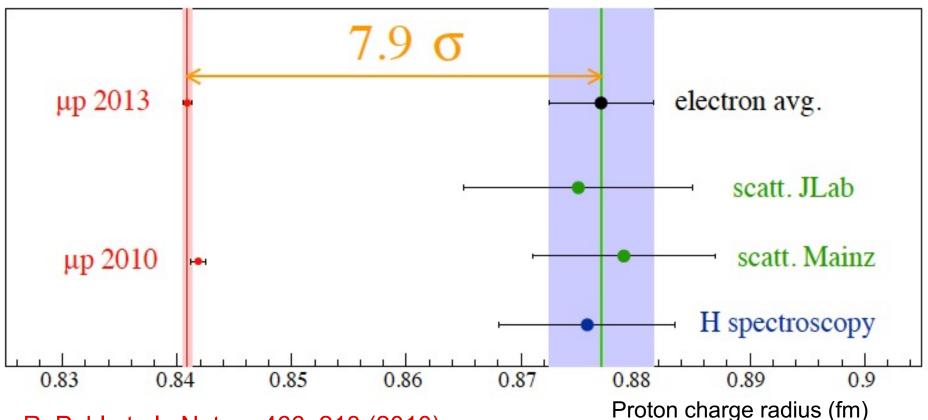
Blinded analysis. Expect smaller errors in the future. Huge theory effort: Hadr. vac. pol., light-by-light scatt.; Lattice QCD

The proton radius puzzle in 2010/2013

The proton rms charge radius measured with

electrons: 0.8770 ± 0.0045 fm (CODATA2010+Zhan et al.)

muons: $0.8409 \pm 0.0004 \text{ fm}$



R. Pohl et al., Nature 466, 213 (2010)

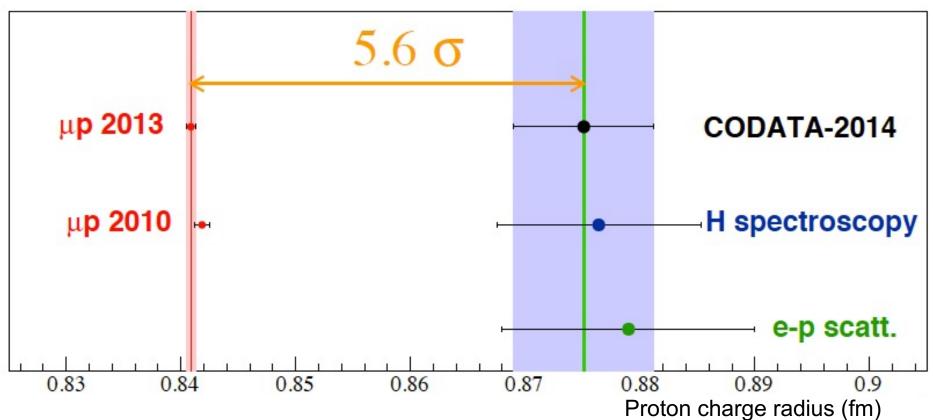
A. Antognini et al., Science 339, 417 (2013)

The proton radius puzzle in 2016

The proton rms charge radius measured with

electrons: (0.8751 ± 0.0061) fm (CODATA2014)

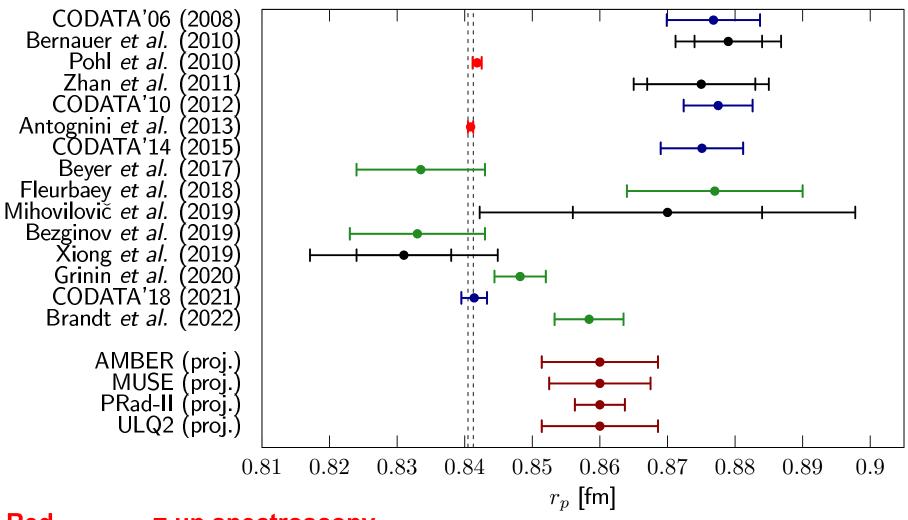
muons: (0.8409 ± 0.0004) fm



R. Pohl et al., Nature 466, 213 (2010)

A. Antognini et al., Science 339, 417 (2013)

The proton radius puzzle in 2023



Red = μp spectroscopy

Black = ep scattering

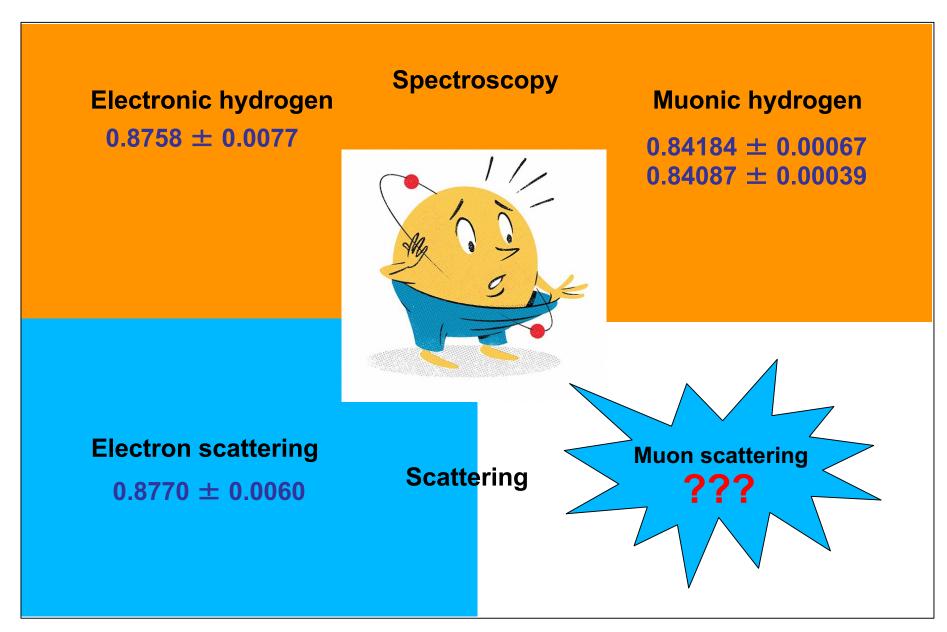
Green = ep spectroscopy

Blue = CODATA

Dark-red = Future scattering

Plot: courtesy by J. Bernauer

Motivation for µp scattering



Idea for MUSE developed by R. Gilman, G. Miller, and M.K. at PINAN2011, Morocco

MUSE timeline and status

- Proton radius puzzle not solved in 2023 13 years later
- Lepton non-universality in the center of beyond-SM effects
- MUSE first proposed in 2012, PAC-approved in 2013
- R&D program with NSF, BSF, and DOE support 2014 2016
- Technical design report November 2015
- Collaborative funding proposal to NSF in Nov 2015: Mid-scale
- NSF technical review February 2016
- Target conceptual design March 2016
- MOU with PSI April 2016
- Project management review May 2016 → award recommendation!
- Funding for construction has begun in fall 2016
- Construction and commissioning of MUSE 2016-2022
- Initial scattering data collected in Fall 2021 and Fall 2022
- Data taking for 12 calendar months 5 months in 2023 ongoing

MUSE experiment layout

- Beam particle tracking
- Liquid hydrogen target
- Scattered lepton detected

Measure e[±]p and μ[±]p elastic scattering

p = 115, 153, 210 MeV/c

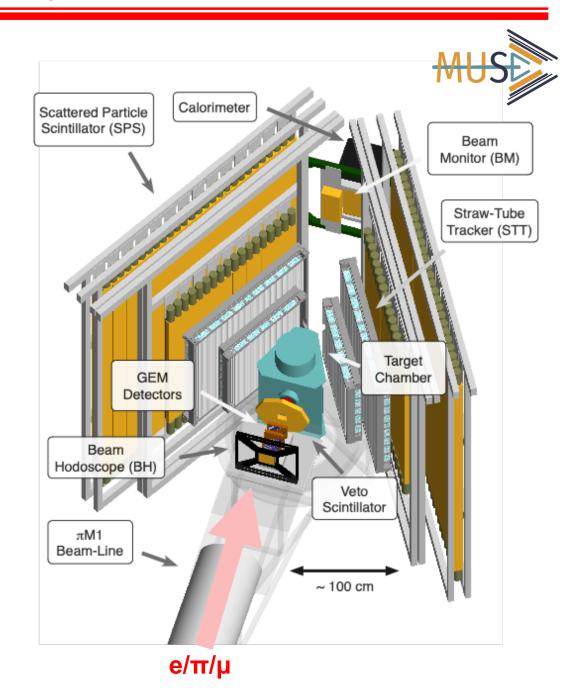
 $\theta = 20^{\circ} \text{ to } 100^{\circ}$

 $Q^2 = 0.002 - 0.07 (GeV/c)^2$

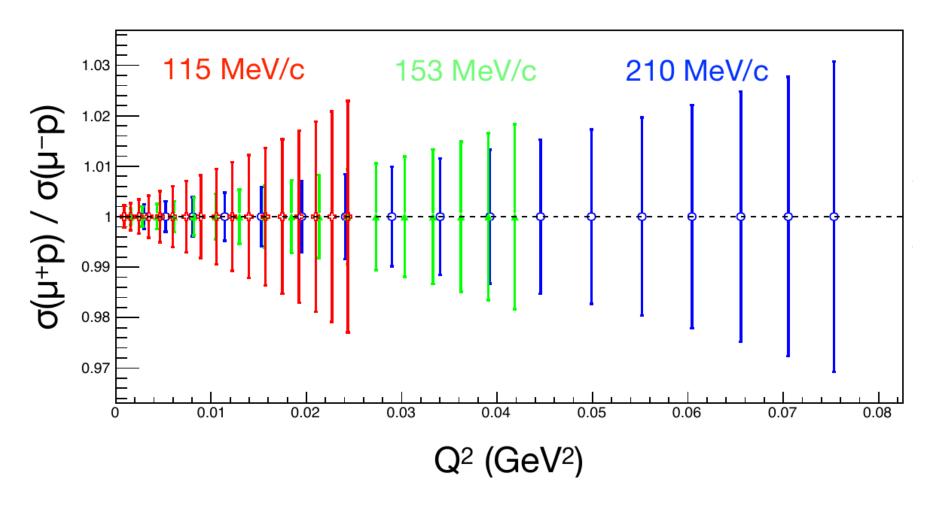
 $\varepsilon = 0.256 - 0.94$

Challenges

- Secondary beam with π background – PID in trigger
- Non-magnetic spectrometer
- Background from Møller scattering and muon decay in flight

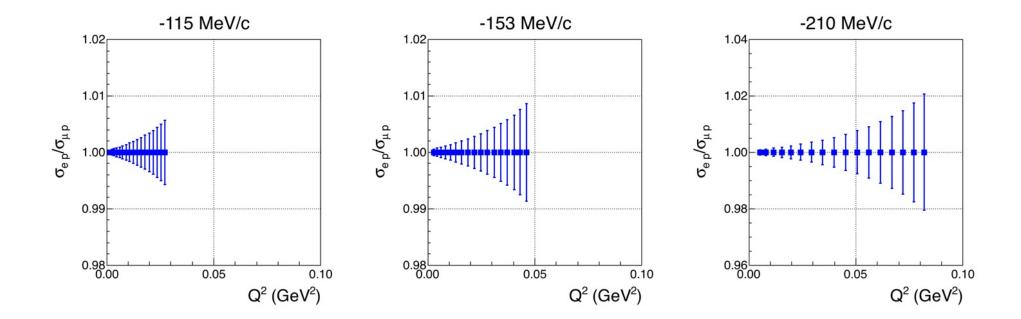


MUSE: expected precision for TPE (muons)



- Investigation of e+/e-, μ+/μ-
- Direct measurement of 2-photon effects
- TPE for muons could be sizable; for e+/e- expect sub-percent

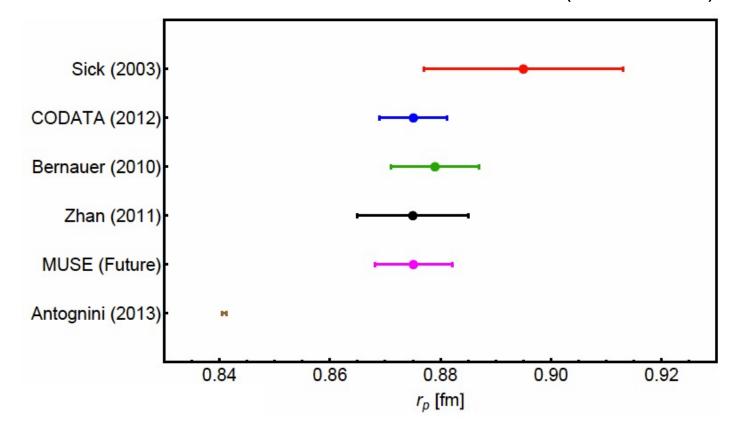
MUSE: expected precision for LU ratio



- Comparison of ep and µp cross section statistical uncertainty, systematic better than 0.5%
- The MUon Scattering Experiment at PSI (MUSE),
 MUSE Technical Design Report, arXiv:1709.09753 [physics.ins-det]

MUSE: expected precision for charge radius

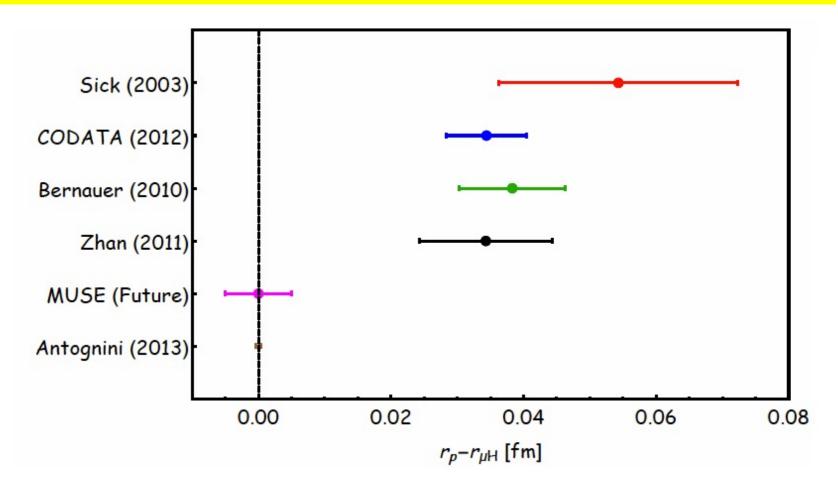
- Cross sections to <1% stat. for backward μ, <<1% for e and forward μ
 Absolute 2%, point-to-point relative uncertainties few x10⁻³
- Individual radius extractions from e[±], µ[±] each to 0.010 fm
- Compare e[±]p and μ[±]p for TPE. Charge-average to eliminate TPE.
- From e/μ xsec ratios: extract e-μ radius difference with minimal truncation error to 0.0045 fm or ~8σ (1st-order fits)
- If no difference, extract combined radius to 0.007 fm (2nd-order fit)



MUSE: expected precision for radius diff.

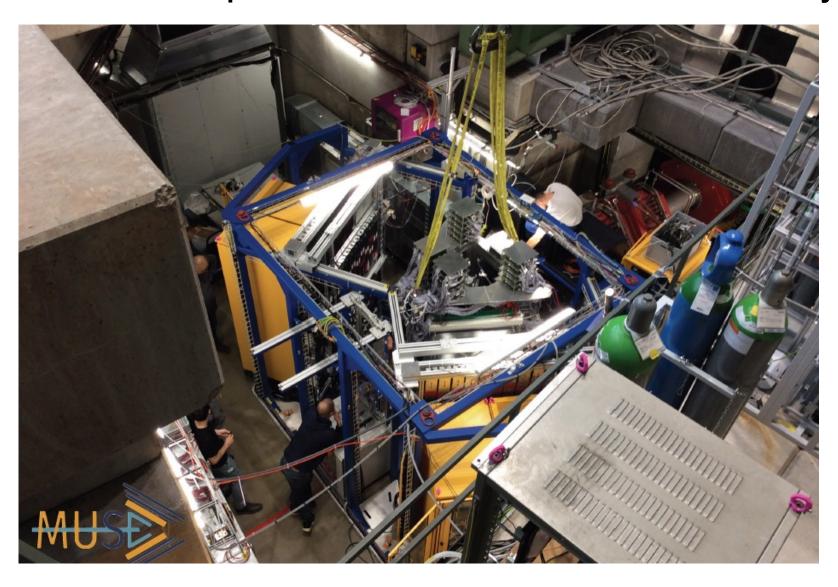
- Charge radius extraction limited by systematics, fit uncertainties
- Many uncertainties are common to all extractions in the experiment: Cancel in e+/e-, μ+/μ-, and μ/e comparisons
- $R_e R_\mu = 0.034 \pm 0.006 \text{ fm } (5.6\sigma), \text{ MUSE: } \delta(R_e R_\mu) = 0.0045 \text{ fm } (7.6\sigma)$

MUSE suited to verify 5.6σ effect (CODATA2014) with 7.6σ significance



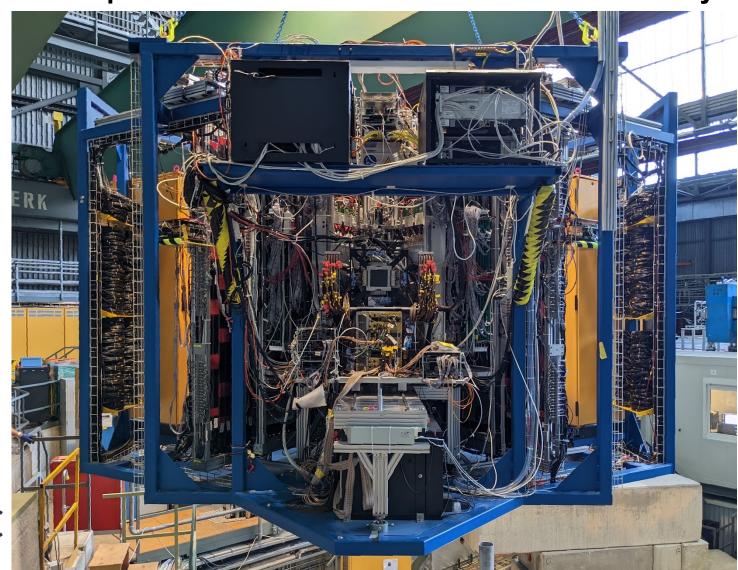
2018-2022 installation and commissioning

Dec. 2018: Assembly complete; Summer/fall 2019: Initial commissioning Fall 2020/Spring 2021: Commissioning cont'd under Covid-19 constraints From Fall 2022: Start production data for 12 beam months over ~2 years



2023-2025: production data taking

Dec. 2018: Assembly complete; Summer/fall 2019: Initial commissioning Fall 2020/Spring 2021: Commissioning cont'd under Covid-19 constraints From Fall 2022: Start production data for 12 beam months over ~2 years





72 MUSE collaborators from 25 institutions in 5 countries:

- A. Afanasev, A. Akmal, A. Atencio, J. Arrington, H. Atac, C. Ayerbe-Gayoso, F. Benmokhtar, K. Bailey,
- N. Benmouna, J. Bernauer, W.J. Briscoe, T. Cao, D. Cioffi, E. Cline, D. Cohen, E.O. Cohen, C. Collicott,
- K. Deiters, J. Diefenbach, S. Dogra, E.J. Downie, I. Fernando, A. Flannery, T. Gautam, D. Ghosal,
- R. Gilman, A. Golossanov, R. Gothe, D. Higinbotham, J. Hirschman, D. Hornidge, Y. Ilieva,
- N. Kalantarians, M.J. Kim, M. Kohl, O. Koshchii, G. Korcyl, K. Korcyl, B. Krusche, I. Lavrukhin, L. Li,
- J. Lichtenstadt, W. Lin, A. Liyanage, W. Lorenzon, K.E. Mesick, Z. Meziani, P. M. Murthy, J. Nazeer,
- T. O'Connor, P. Or, T. Patel, E. Piasetzky, R. Ransome, R. Raymond, D. Reggiani, H. Reid,
- P.E. Reimer, A. Richter, G. Ron, P. Roy, T. Rostomyan, P. Salabura, A. Sarty, Y. Shamai, N. Sparveris,
- S. Strauch, N. Steinberg, V. Sulkosky, A.S. Tadepalli, M. Taragin, and N. Wuerfel

PAUL SCHERRER INSTITUT





George Washington University, Montgomery College, Argonne National Lab, Temple University, Duquesne University, Stony Brook University, Rutgers University, Hebrew University of Jerusalem, Tel Aviv University, University of Basel, Paul Scherrer Institute, Johannes Gutenberg-Universität, Hampton University, University of Michigan, University of South Carolina, Jefferson Lab, Massachusetts Institute of Technology, Technical University of Darmstadt, St. Mary's University, Soreq Nuclear Research Center, Weizmann Institute, Old Dominion University (April 2020)

- Lepton non-universality?
- TREK Program
 - E06: Search for Time Reversal Symmetry Violation
 - E36: Test of Lepton Universality
 - Search for Heavy Neutrinos
 - Search for Light Bosons

Lower intensity

TREK Apparatus





Status

http://trek.kek.jp

TREK (E36/E06) collaboration

~30 collaborators

Spokespeople: M.K., S. Shimizu

CANADA

University of British Columbia

Department of Physics and Astronomy

TRIUMF

USA

University of South Carolina

Department of Physics and Astronomy

University of Iowa

Department of Physics

Hampton University

Department of Physics

JAPAN

Osaka University

Department of Physics

Chiba University

Department of Physics

Rikkyo University

Department of Physics

High Energy Accelerator Research Organization (KEK)

Institute of Particle and Nuclear Studies

RUSSIA

Russian Academy of Sciences (RAS)

Institute for Nuclear Research (INR)

Timeline of TREK E06 and E36

- 2006: E06 (T-violation) Proposal (PAC1)
- 2009: J-PARC PS and HF start operating
- 2010: E36 (LFU/HNS) Proposal (PAC10)
- 2011: E36 stage-1 recommended (PAC11)
- 2012: E36 stage-1 approved (PAC15)
- 2013: E36 stage-2 recommended (PAC17)
- 2014: E36 stage-2 approved (PAC18)
- Detector preparation November 2014 April 2015
- First commissioning run April 8 (24) May 7, 2015
- Second commissioning run June 3 26, 2015
- Implemented improvements in summer 2015
- Production run October 14 November 24, 2015
- Run extended until December 18, 2015
- 2016-2023: Analysis in progress and first results

Lepton universality in Standard Model K₁₂

Standard Model:

$$\Gamma(K_{l2}) = g_l^2 \frac{G^2}{8\pi} f_K^2 m_K m_l^2 \left(1 - \frac{m_l^2}{m_K^2} \right)^2$$

$$K^{+}$$

• In the ratio of $\Gamma(K_{e2})$ to $\Gamma(K_{\mu 2})$, hadronic form factors are cancelled

$$g_e=g_\mu$$
?

 V_e,V_μ

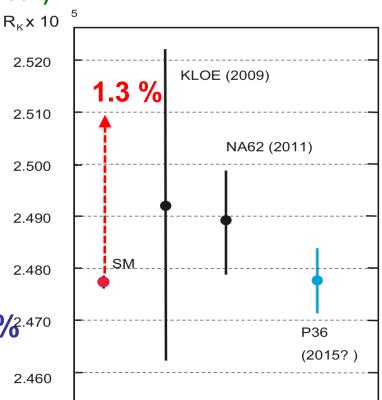
$$\begin{array}{ccc} \blacksquare & R_K^{SM} & = & \frac{\Gamma(K^+ \to e^+ \nu)}{\Gamma(K^+ \to \mu^+ \nu)} = \frac{m_e^2}{m_\mu^2} \left(\frac{m_K^2 - m_e^2}{m_K^2 - m_\mu^2}\right)^2 \underbrace{(1 + \delta_r)}_{\mbox{\it radiative correction (Internal Brems.)}}$$

- Strong helicity suppression of the electronic channel enhances sensitivity to effects beyond the SM
- Highly precise SM value

$$R_K^{\rm SM}$$
= (2.477 ± 0.001) x 10⁻⁵ with δ_r = -0.036; ($\rightarrow \delta R_K/R_K$ =0.04%) V. Cirigliano, I. Rosell, Phys. Rev. Lett. 99, 231801 (2007)

Experimental status of R_{K}

- Highly precise SM value $R_{\rm K} = (2.477 \pm 0.001) \times 10^{-5}$ (with $\delta_r = -0.036$), $\delta R_{\rm K}/R_{\rm K} = 0.04\%$ V. Cirigliano, I. Rosell, Phys. Rev. Lett. 99, 231801 (2007)
- KLOE @ DAΦNE (in-flight decay) $R_{\rm K} = (2.493 \pm 0.025 \pm 0.019) \times 10^{-5}$ F. Ambrosino et al., Eur. Phys. J. C64, 627 (2009)
- NA62 @ CERN-SPS (in-flight decay) $R_{\rm K}$ = (2.488 \pm 0.007 \pm 0.007) \times 10⁻⁵ C. Lazzeroni et al., PLB719, 105 (2013)
- World average (2012) $R_{\rm K} = (2.488 \pm 0.009) \times 10^{-5}, \, \delta R_{\rm K}/R_{\rm K} = 0.4\%^{.470}$
- Dominant systematics:
 - In-flight-decay experiments: kinematics overlap
 - E36 stopped K⁺: detector acceptance and target
 - E36 complementary to in-flight experiments
- E36 orig. goal: $\delta R_K/R_K = \pm 0.2\%$ (stat) $\pm 0.15\%$ (sys) [0.25% tot.]



The TREK apparatus for E36

End View Side View Iron Pole Cryostat **GSC** Cryostat **PGC** GSC Iron Pole TOF1, SFT Lead AC Shield TOF2 вс **TGT** K⁺ TOF1, SFT Degrader 0.5 1.0 m

Stopped K+

- •K1.1BR beamline
- Fitch Cherenkov
- •*K*⁺ stopping target (TGT)

Modest upgrade of KEK-PS E246

Tracking (π,μ,e)

- •MWPC (C2, C3, C4)
- Spiral Fiber Tracker (SFT)
- •TGT, TOF1,2, TTC

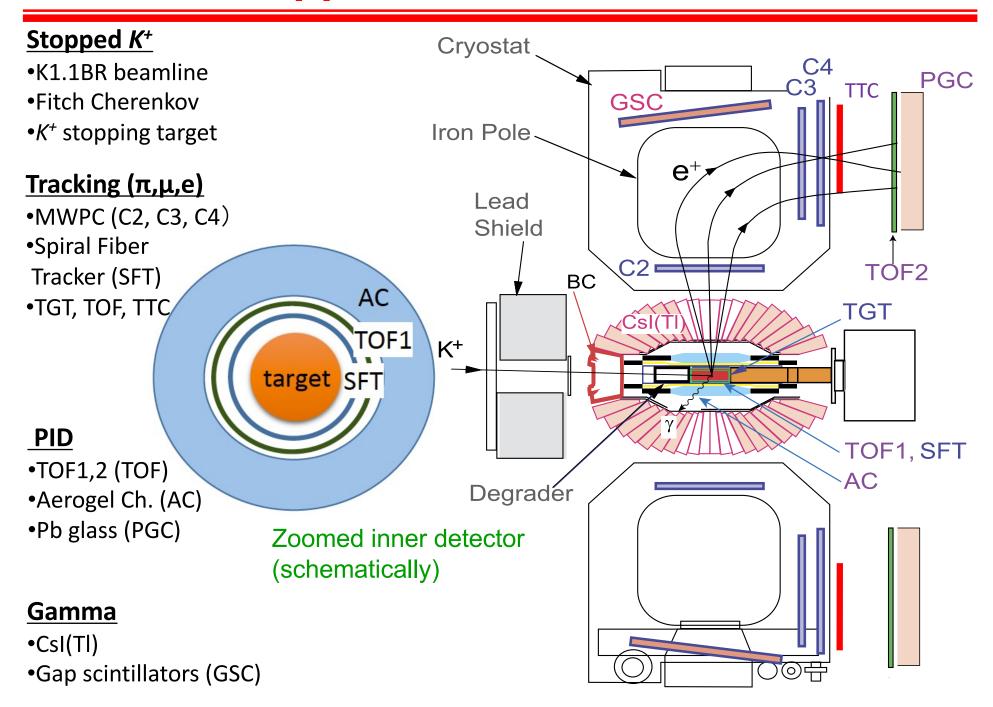
PID

- •TOF2-TOF1 (TOF)
- •Aerogel Ch. (AC)
- •Pb glass (PGC)

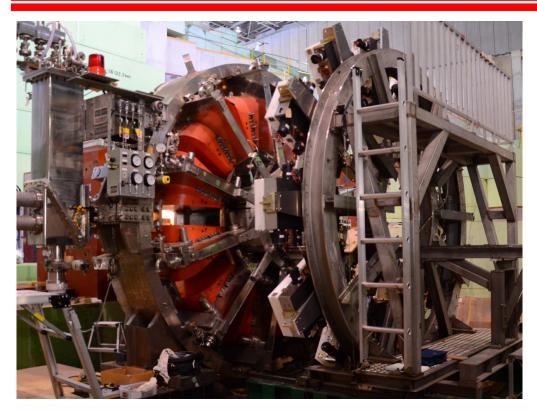
Gamma

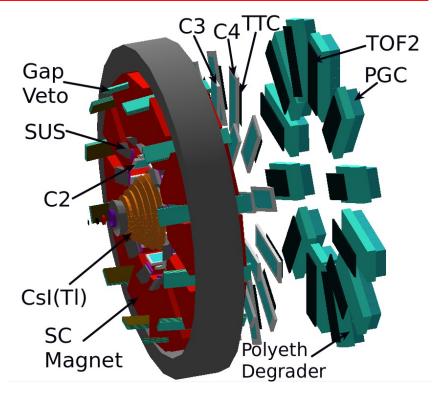
- CsI(TI)
- •Gap scintillators (GSC)

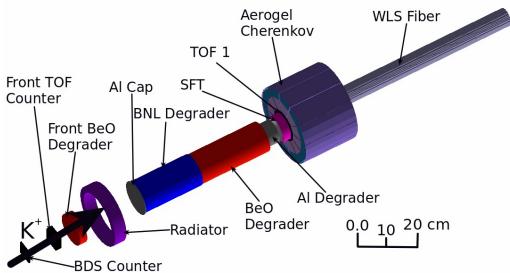
The TREK apparatus for E36

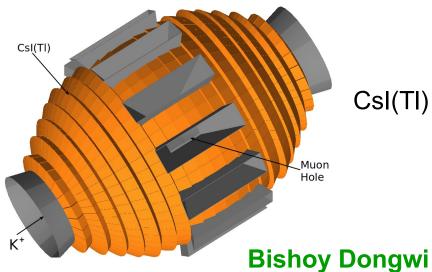


Geant4 description of TREK/E36





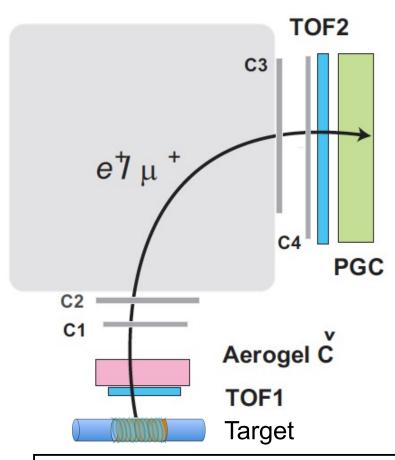




μ⁺/e⁺ identification (designed)

PID with:

- TOF
- Aerogel Č
- Lead glass

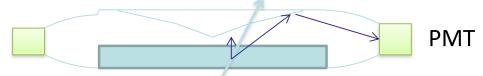


TOF

Flight length 250 cm
Time resolution <100 ps
Mis-ID probability 7x 10⁻⁴

Aerogel Č counter

Radiator thickness
Refraction index
e⁺ efficiency
Mis-ID probability
4.0 cm
1.08
>98%
3%



Lead glass (PGC)

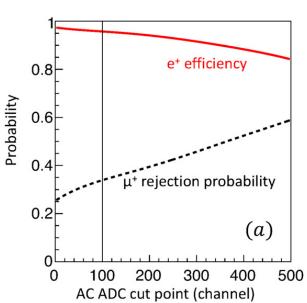
Material SF6W
Refraction index 1.05
e+ efficiency 98%
Mis-ID probability 4%

 P_{mis} (total) = P_{mis} (TOF) x P_{mis} (AČ) x P_{mis} (LG) = 8 x 10⁻⁷ < $O(10^{-6})$

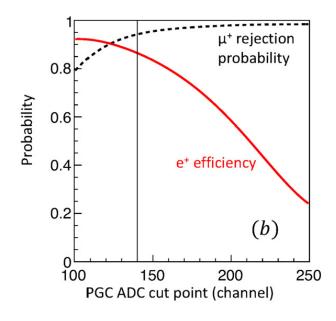
μ⁺/e⁺ identification (typical performance)

- Redundant PID to maximize e⁺ efficiency and minimize µ⁺ mis-ID
- PID with:

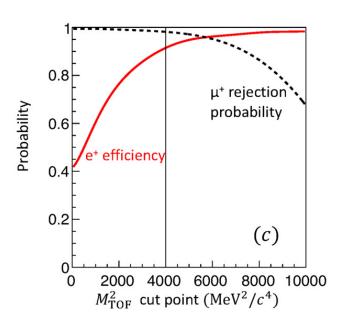




Leadglass (PGC)



Time of flight (TOF)

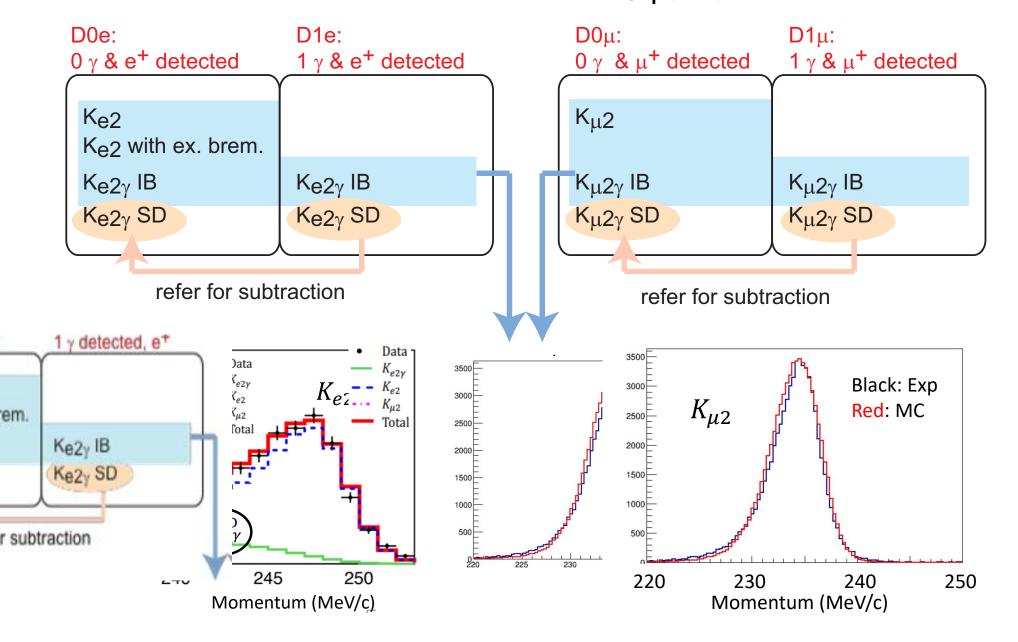


H. Ito et al., PLB 826, 136913 (2022)

PID performance limitation requires subtraction of residual muon background

Toward $R_K = Br(K_{e2(y)}) / Br(K_{\mu 2(y)})$

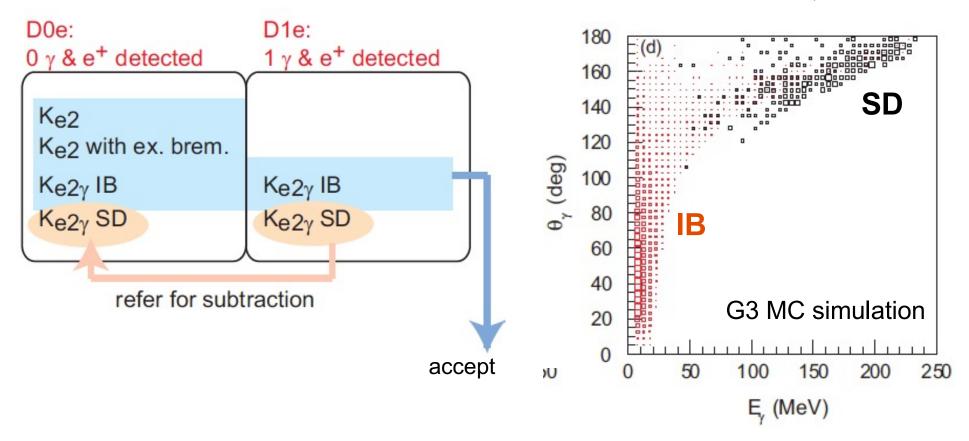
Subtraction of structure dependent K_{e2y} (SD) required



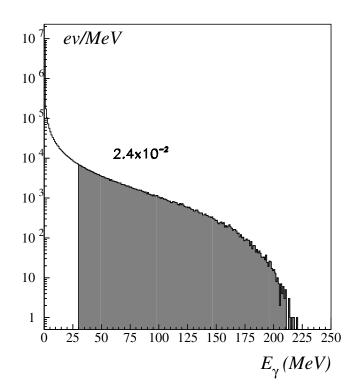
Extraction of $K_{e2y}(SD)$ and $K_{e2(y)}$

- Subtraction of structure dependent K_{e2v} (SD) required
- Internal bremsstrahlung (IB) to be included in K_{e2}: "K_{e2(y)}"
- E36 and KLOE can measure the SD events
- K_{e2y} (SD) is important input for NA62 analysis ($\delta R_K/R_K=0.4\%$)

K. Horie, S. Shimizu



MC prescription by Gatti



C. Gatti, Eur. Phys. J. C 45, 417 (2006)

Example spectrum

Fig. 1. Energy spectrum for $K^0 \to \pi e \nu \gamma$ MC decays. 2.4% of the events have $E_{\gamma} > 30 \,\text{MeV}$

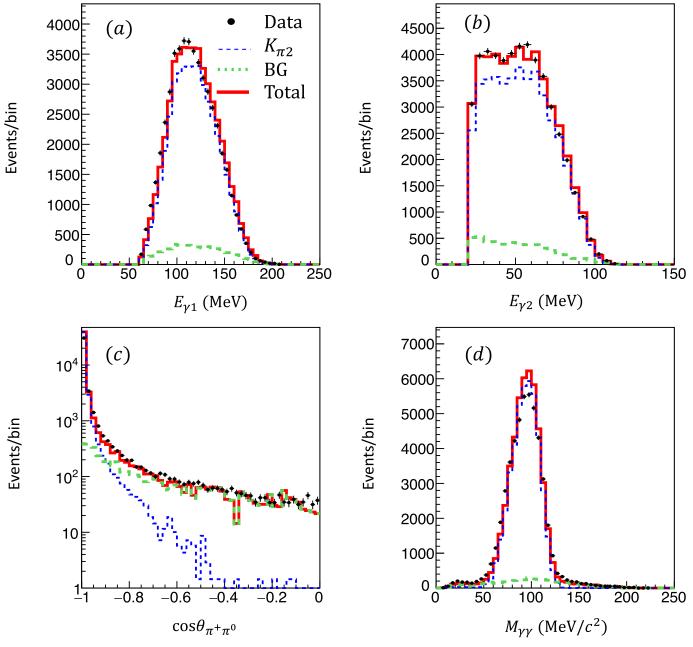
Analytic expressions for IB

$$\frac{\mathrm{d}\Gamma_{\mathrm{incl}}}{\mathrm{d}E_{\gamma}} = \Gamma_0 b \frac{E_{\gamma}^{b-1}}{M^b} = \frac{\mathrm{d}\Gamma_{\mathrm{Brem}}}{\mathrm{d}E_{\gamma}} \left(\frac{E_{\gamma}}{M}\right)^b$$

$$b = -\frac{1}{8\pi^2} \sum_{m,n} \eta_m \eta_n e_m e_n \beta_{mn}^{-1} \ln \frac{1 + \beta_{mn}}{1 - \beta_{mn}}$$
$$\frac{d\Gamma_{\text{Brem}}}{dE_{\gamma}} = \Gamma_0 \frac{b}{E_{\gamma}}$$

- Works also for differential decay widths
- Simple implementation in MC generators

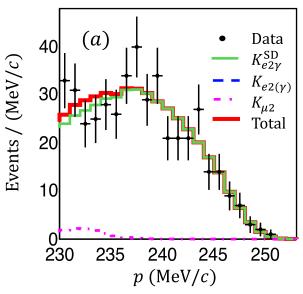
Csl(TI) calibration and accidental bg.



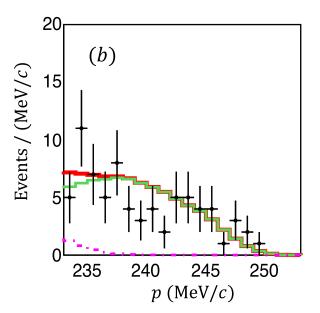
- K_{π2} (K⁺ → π⁺π⁰)
 recon. 2-cluster
 events
- Accidental bg: K_{μ2} + 1-cluster (~19%) exp. acc. spect.
- Mixing exp. acc. with simulated
 1-cluster K_{π2} for acc. background in 2-cluster evts.

Extraction of $K_{e2y}(SD)$ and $K_{e2(y)}$

- Positron momentum spectrum
- PID applied with AC, PGC, TOF
- Decomposition of $K_{e2(\gamma)}$, $K_{e2\gamma}^{SD}$, $K_{\mu 2}$, K_{e3} yields
- Internal bremsstrahlung (IB) effect included in $K_{e2(y)}$



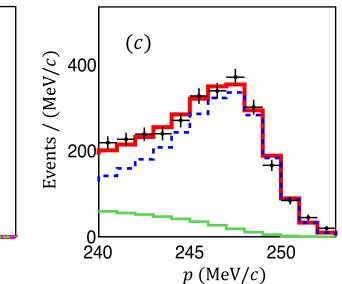




Csl: 2-cluster

H. Ito et al., PLB 826, 136913 (2022)

C. Gatti, EPJC 45, 417 (2006)



Csl: any cluster

E36 (CsI) result for K_{e2y} (SD): BR(K_{e2y}^{SD})/BR($K_{e2(y)}$) = 1.12 \pm 0.07 stat. \pm 0.04 sys.

Comparison of $K_{e2v}(SD)$ w/ KLOE & Theory

E36: $BR(K_{e2v}^{SD})/BR(K_{e2(v)}) = 1.12 \pm 0.07 \text{ stat.} \pm 0.04 \text{ sys.}$

H. Ito et al., PLB 826, 136913 (2022)

Comparison with KLOE: convert E36 ratio, reduce phase space

$$\frac{Br(K_{e2\gamma}^{\text{SD}^{+}})}{Br(K_{\mu 2})} = \frac{Br(K_{e2\gamma}^{\text{SD}^{+}})}{Br(K_{e2(\gamma)})} \times \frac{Br(K_{e2(\gamma)})}{Br(K_{\mu 2})} = \frac{Br(K_{e2\gamma}^{\text{SD}^{+}})}{Br(K_{e2(\gamma)})} \times R_{K}^{\text{SM}}$$

$$R_{\gamma} = \frac{Br(K_{e2\gamma}^{SD^{+}}, \ p > 200 \ \text{MeV}/c, \ E_{\gamma} > 10 \ \text{MeV})}{Br(K_{\mu 2})}$$

E36:
$$R_{\gamma} = (1.85 \pm 0.11_{\text{stat}} \pm 0.07_{\text{syst}}) \times 10^{-5}$$

KLOE:
$$R_{\gamma} = (1.483 \pm 0.066_{\text{stat}} \pm 0.013_{\text{syst}}) \times 10^{-5}$$

F. Ambrosino et al., Eur. Phys. J. C64, 627 (2009)

Lattice-QCD: $R_{\gamma} = (1.74 \pm 0.21) \times 10^{-5}$

R. Frezzotti, et al., Phys. Rev. D 103, 053005 (2021)

ChPT:

 $R_{\gamma}=1.477\times 10^{-5}$ J. Bijnens, G. Ecker, J. Gasser, Nucl. Phys. B 396, 81 (1993)

E36: Agree with Lattice (\sim 1 σ), disagree with ChPT (\sim 3 σ)

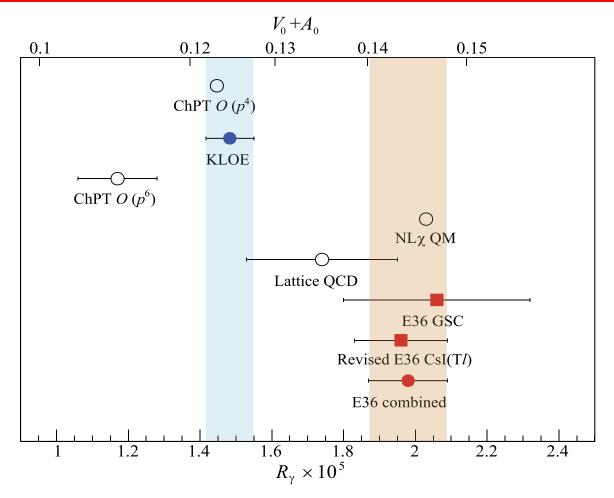
New extraction of $K_{e2v(v)}(SD)$

- Caveat: IB correction was only applied to $K_{e2(\gamma)}$, not to $K_{e2\gamma}$ (SD) Narrow e⁺ momentum interval requires accounting for acceptance loss due to hard photon IB tail
- Similarly, acceptance of $K_{e^{2\gamma(\gamma)}}$ (SD) affected by hard photon radiation, too
- Implementation: Following prescription by Gatti, using radiative MC generators for both K_{e2(γ)} and K_{e2γ(γ)} (SD)
 C. Gatti, Eur. Phys. J. C 45, 417 (2006)
- E36: Additional E36 data from Gap Scintillation Counters (GSC)
 → New E36 result for Csl(Tl) + GSC:

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Previously: BR(K_{e2\gamma})/BR(K_{e2(\gamma)}) = 1.12 \pm 0.07 stat. \pm 0.04 sys. H. Ito et al., Phys. Lett. B 826, 136913 (2022)
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BR(K_{e2\gamma(\gamma)}^{SD})/BR(K_{e2(\gamma)}) = 1.25 ± 0.14 stat. ± 0.08 sys. – GSC BR(K_{e2\gamma(\gamma)}^{SD})/BR(K_{e2(\gamma)}) = 1.19 ± 0.07 stat. ± 0.04 sys. – CsI(TI) [+6%] Error-weighted mean: 1.20 ± 0.07 \rightarrow R<sub>γ</sub> = (1.98±0.11) x 10<sup>-5</sup> Agree with Lattice (~1σ), disagree with ChPT (~4σ) A. Kobayashi et al., Phys. Lett. B 843, 138020 (2023) - 10 August, online June 14, 2023
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New extraction of $K_{e2y(y)}(SD)$



BR($K_{e2\gamma(\gamma)}^{SD}$)/BR($K_{e2(\gamma)}$) = 1.25 ± 0.14 stat. ± 0.08 sys. – GSC BR($K_{e2\gamma(\gamma)}^{SD}$)/BR($K_{e2(\gamma)}$) = 1.19 ± 0.07 stat. ± 0.04 sys. – CsI(TI) [+6%] Error-weighted mean: 1.20 ± 0.07 \rightarrow R_γ = (1.98±0.11) x 10⁻⁵ Agree with Lattice (~1σ), disagree with ChPT (~4σ)

A. Kobayashi et al., Phys. Lett. B 843, 138020 (2023) - 10 August, online June 14, 2023

Summary

- Lepton universality is challenged (BaBar, Belle, LHCb; g_μ-2; PRP)
 However: Most recent LHCb result on μ-e universality agrees with SM
- Muon g-2 and proton radius puzzle are so far largest hints for μ-e LUV
- MUSE: plays key role for testing of μ-e universality and solving PRP







TREK/E36:

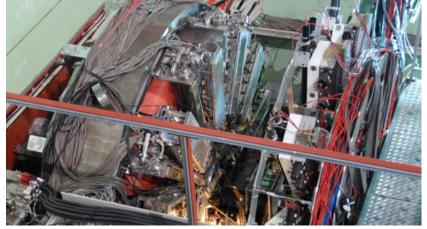
Measurement of $R_K = BR(K_{e2(\gamma)})/BR(K_{\mu 2(\gamma)})$ – test of μ -e universality

Extraction of R_K underway

Measured structure-dep. $BR(K_{e2\gamma}(SD))$







Backup

Systematics

Table 2 Summary of the systematic uncertainties for the $Br(K_{e2\gamma}^{\rm SD^+})/Br(K_{e2(\gamma)})$ ratio determination.

Source	Systematic uncertainty
Hole size of CsI(Tl) calorimeter	0.017
CsI(Tl) misalignment	< 0.001
Imperfect reproducibility of photon angular	< 0.001
distribution	
Accidental backgrounds in CsI(Tl)	0.004
Photon energy threshold of CsI(Tl)	0.007
Photon energy calibration of CsI(Tl)	< 0.001
Photon timing window	0.009
CsI(Tl) detection efficiency	0.012
AC detection(PID) efficiency	0.007
PGC detection(PID) efficiency	0.007
TOF detection(PID) efficiency	0.019
$K_{\mu 2}$ background subtraction	0.015
$K_{e2\nu}^{\mathrm{SD}^{+}}$ form factor	0.011
K^{+} stopping distribution	0.003
Material thickness in the central parts	< 0.001
Positron momentum resolution	0.002
Magnetic field	0.002
In-flight kaon decay	0.002
Total	0.036