

The GDH Program at Jefferson Lab

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Mainz, June 27, 2023



The ABC of GDH

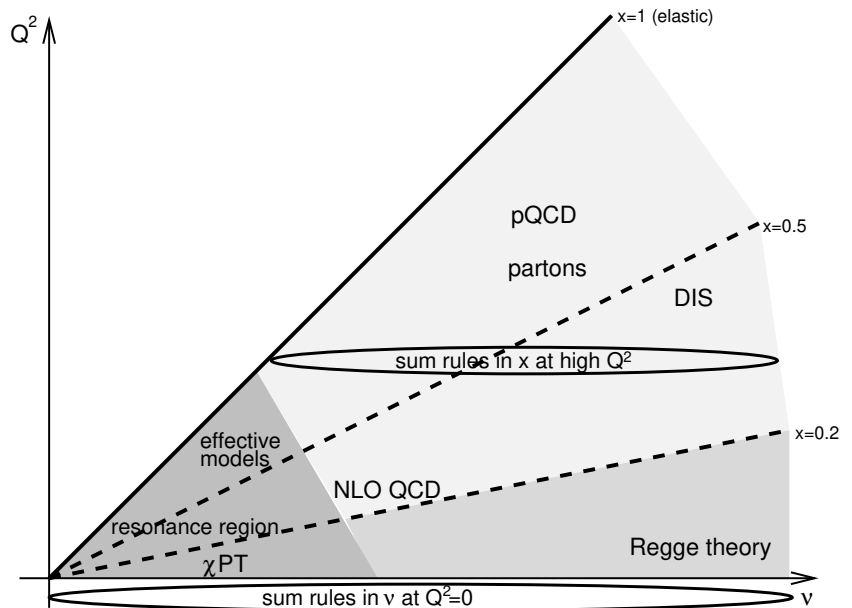
- GDH = Gerasimov, Drell, Hearn (1966)
- Relates difference $\Delta\sigma \equiv \sigma_{3/2} - \sigma_{1/2} \equiv \sigma_P - \sigma_A$ of spin-dependent total photo-production XS to anomalous magnetic moment κ and mass M of arbitrary particle:

$$I_{\text{GDH}} = \int_{\nu_0}^{\infty} \frac{\sigma_{3/2}(\nu) - \sigma_{1/2}(\nu)}{\nu} d\nu = 4\pi^2 \alpha S \frac{\kappa^2}{M^2}$$

- Fundamental QFT statement; valid for any spin S ... but:

- ▷ RHS for proton/ neutron known to ~ 8 digits: $I_{\text{GDH}}^p \approx 205 \mu\text{b}$, $I_{\text{GDH}}^n \approx 232 \mu\text{b}$
- ▷ $\Delta\sigma$ for p (n) known at few % level, but only to $\nu = E_\gamma \approx 2.9 \text{ GeV}$ (2 GeV)
- ▷ $\Delta\sigma$ at large ν unknown; domain of Regge theory
- ▷ $1/\nu$ weight emphasizes threshold region, $\nu_0 \geq m_\pi(1 + m_\pi/2M_N)$ for p/n, thus sum rule saturated by $\nu \approx 3 \text{ GeV}$ (?)

Drechsel, Tiator, Annu. Rev. Nucl. Part. Sci. 54, 69 (2004)



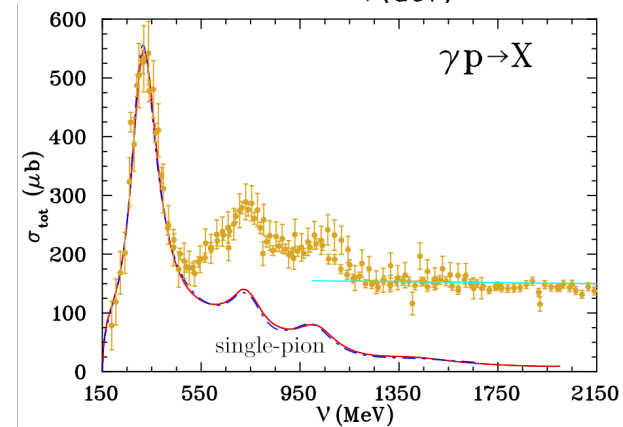
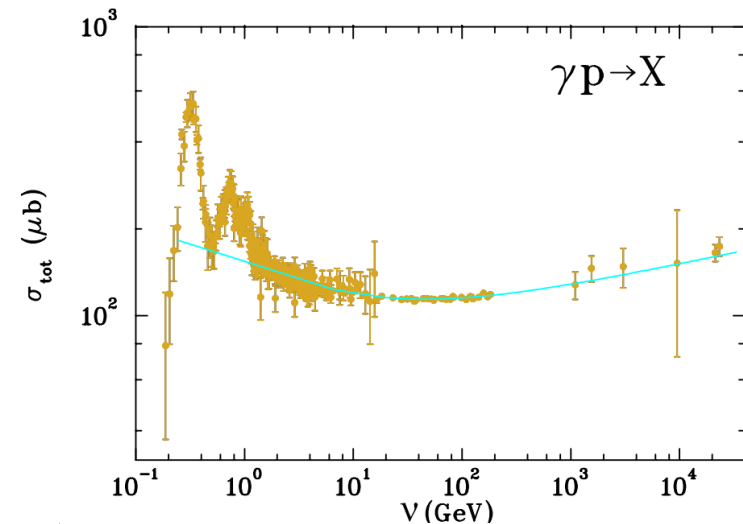
GDH: why the question mark

- Unpolarized “sum rule” (for $\sigma_{\text{tot}} \equiv \sigma_{3/2} + \sigma_{1/2} \equiv \sigma_P + \sigma_A$ on p/n):

$$\int_{\nu_0}^{\infty} (\sigma_{3/2}(\nu) + \sigma_{1/2}(\nu)) d\nu = -\frac{\pi\alpha}{M_N}$$

- ▷ LHS > 0, RHS < 0 (?)
- ▷ Divergent integrand (?)
- ▷ Pomeron exchange (1961)
Regge parameterization of the XS,
good up to $s = M_N(M_N + 2\nu) \approx (250 \text{ GeV})^2$:
 $\sigma_{\text{tot}} = (129 s^{-0.4545} + 67.7 s^{0.08}) \mu\text{b}$
- ▷ If $\int \sigma_{\text{tot}}(\nu) d\nu$ is divergent, what are the implications for the convergence of $\int (\Delta\sigma(\nu)/\nu) d\nu$ and asymptotic behaviour of $\Delta\sigma(\nu)$?
- ▷ \exists several considerations why the sum rule may need to be modified

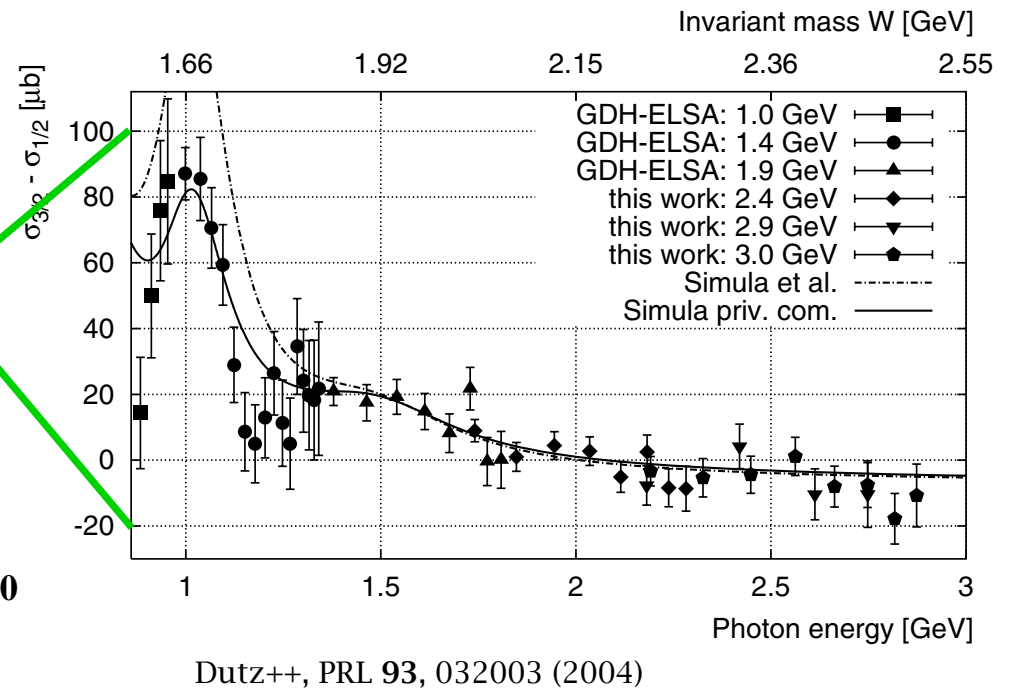
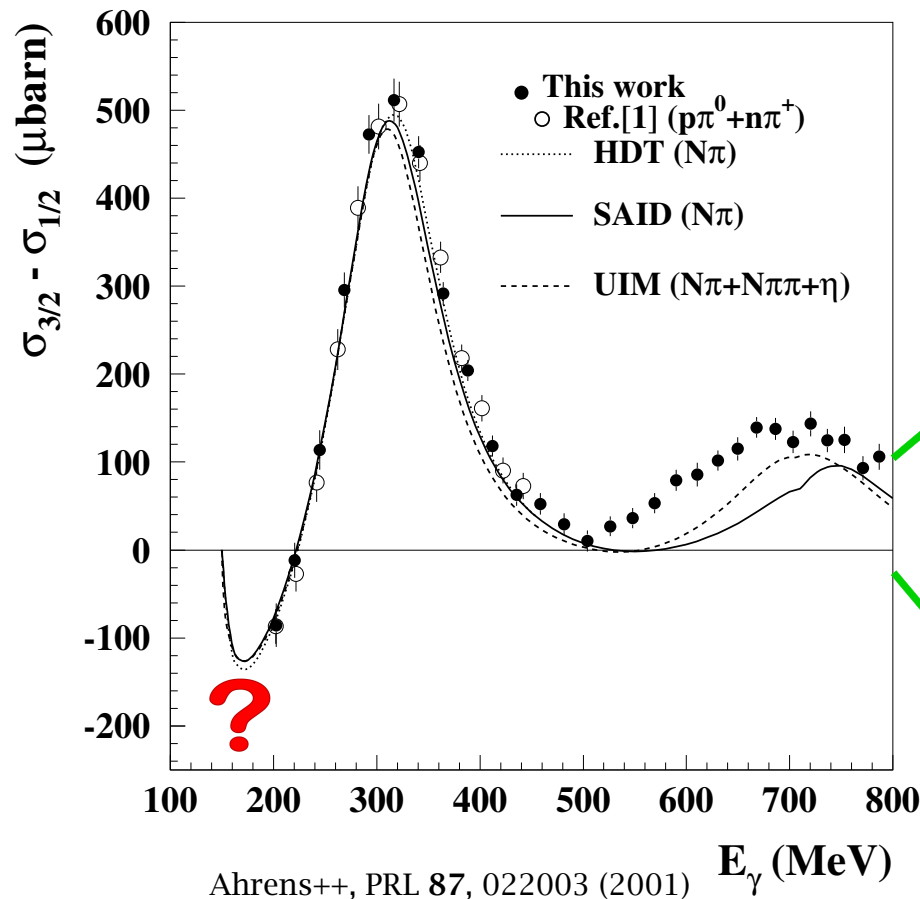
Pantförder, arXiv:hep-ph/9805434



Strakovsky++, PRC 105, 045202 (2022)

Measurements of $\Delta\sigma$

- \neq evaluations of the GDH integral
 - ▷ need extrapolation to π threshold / phenomenological input for high- ν
 - MAMI, ELSA: $0.2 \text{ GeV} \leq \nu \leq 2.9 \text{ GeV}$ (p), $0.2 \text{ GeV} \leq \nu \leq 1.8 \text{ GeV}$ (n)
- “Typical results” (proton) + typical problem near threshold:

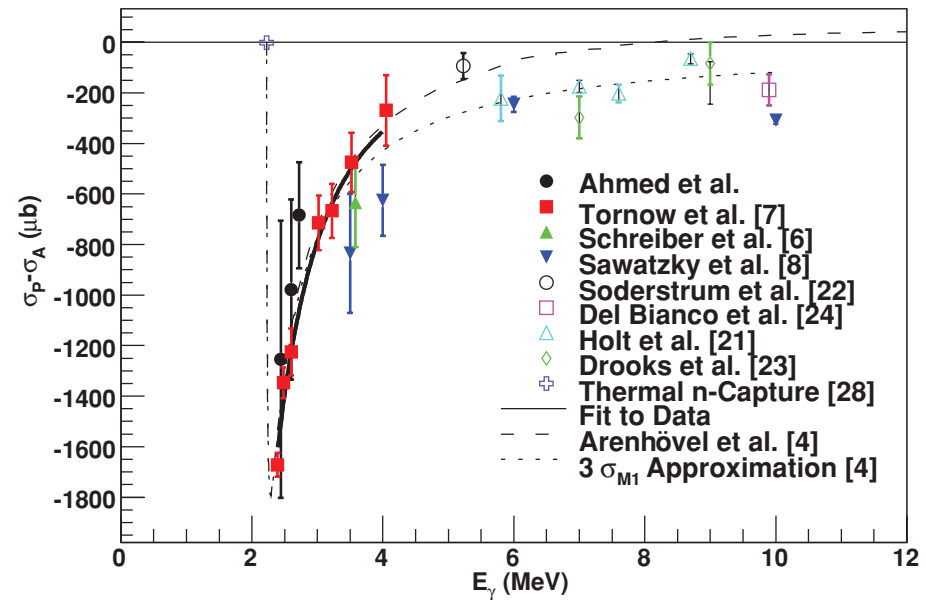
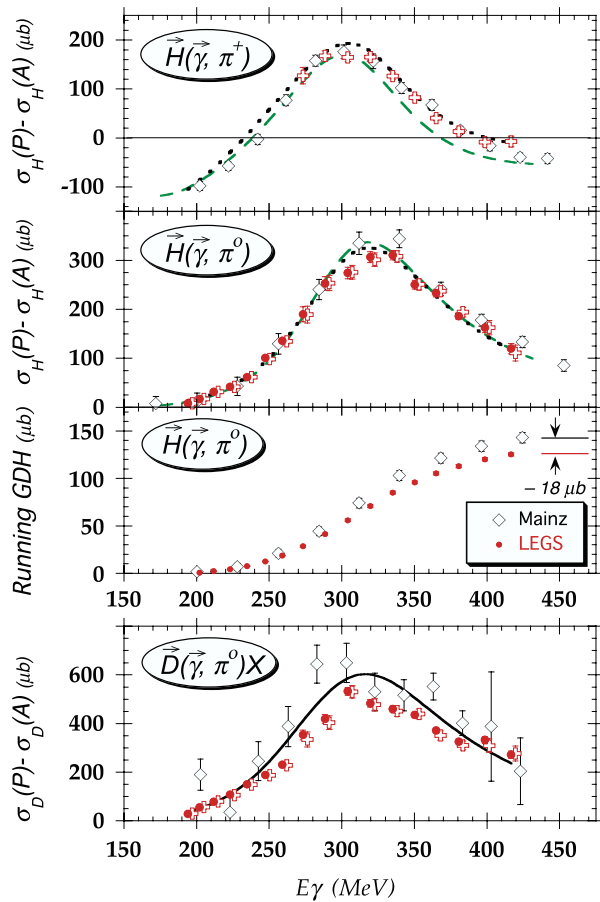


Measurements of $\Delta\sigma$

The **threshold region** is very important due to $1/\nu$ weight

\Rightarrow Use models like MAID/SAID: both give $I_{\text{GDH}}^p(\nu \leq 0.2 \text{ GeV}) \approx -28 \mu\text{b}$

- Low- ν accessible at facilities like LEGS (BNL): $0.2 \text{ GeV} \leq \nu \leq 0.4 \text{ GeV}$...
- ... or TUNL (e. g. deuteron with huge $\Delta\sigma$ just above the photo-disintegration threshold):



Ahmed++, PRC 77, 044005 (2008)

- (Precise) low- ν data is also crucial for extrapolations (guiding threshold models)

Hoblit++, PRL 102, 172002 (2009)

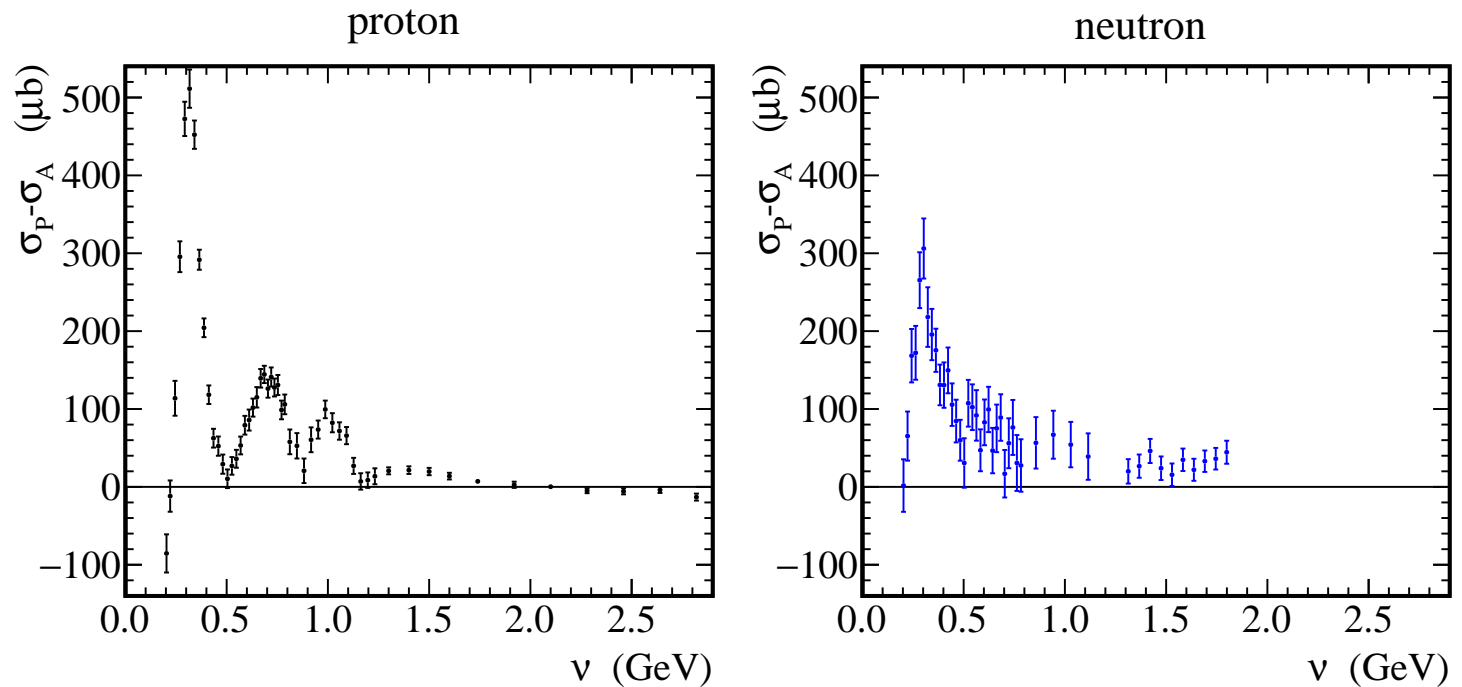
Measurements of $\Delta\sigma(\nu)$, the grand total

Other measurements exist, e. g. CLAS g9 (JLab @ 6 GeV): 1- π contrib up to 2 GeV, 2- π contrib up to 3 GeV, under analysis, *etc. etc.*

Extractions of the neutron $\Delta\sigma$ from d, ^3He etc. require subtractions depending on the target, e.g. LiD: $\Delta\sigma^{d,n}(\nu) = \text{corr}(\nu)\Delta Y^{\text{LiD}} - g^{d,n}\Delta\sigma^p(\nu)$ and involve theoretical assumptions

The (unmeasured) **high- ν region** is interesting in its own way **in spite of** the $1/\nu$ weight ... more on this later

All experiments combined and rebinned



Generalization of the GDH sum rule to $Q^2 \neq 0$

Based on the ν -expansion of the VVCS amplitude in the dispersion relation

$$\text{Re } A_{\text{VVCS}}(\nu, Q^2) = \frac{1}{\pi} P \int_{-\infty}^{\infty} \frac{\text{Im } A_{\text{VVCS}}(\nu', Q^2)}{\nu' - \nu} d\nu'$$

- **LO: generalized GDH**

$$\Delta\sigma \equiv -2\sigma_{TT}$$

$$I_{TT}(Q^2) = \frac{M^2}{4\pi^2\alpha} \int_{\nu_0}^{\infty} \frac{K_{y^*} \sigma_{TT}}{\nu} d\nu = \frac{2M^2}{Q^2} \int_0^{x_0} \left[g_1(x, Q^2) - \frac{4M^2}{Q^2} x^2 g_2(x, Q^2) \right] dx$$

$$\frac{8\pi^2\alpha}{M^2} I_{TT}(0) = - \int_{\nu_0}^{\infty} \frac{\Delta\sigma(\nu)}{\nu} d\nu = - \frac{2\pi^2\alpha\kappa^2}{M^2} = -I_{\text{GDH}}$$

- **NLO: forward spin polarizability: Gell-Mann-Goldberger-Thirring SR:**

$$\gamma_0(Q^2) = \frac{1}{2\pi^2} \int_{\nu_0}^{\infty} \frac{K_{y^*} \sigma_{TT}}{\nu^3} d\nu = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} x^2 \left[\dots \text{ as above } \dots \right] dx$$

$$\gamma_0 = - \frac{1}{4\pi^2} \int_{\nu_0}^{\infty} \frac{\Delta\sigma(\nu)}{\nu^3} d\nu \equiv I_{\text{GGT}}$$

Details of the formalism, conventions etc.:
Deur++, Rep. Prog. Phys. **82** (2019) 076201

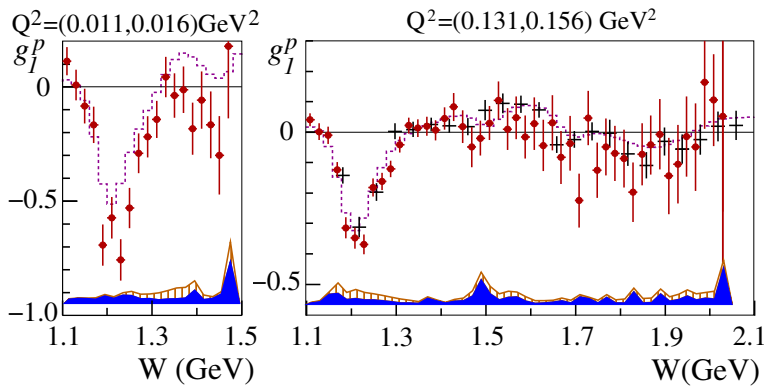
(Some) JLab experiments on spin SRs, spin polarizabilities etc.

- Hall B: EG1a
 g_1^p down to $Q^2 = 0.15$
- Hall A: E94-010 (Cates, Chen, Mezziani)
 $g_1^{3\text{He}}(x, Q^2), g_2^{3\text{He}}(x, Q^2), \Gamma_1^{3\text{He}}(Q^2), \dots$
 $\Rightarrow n$
- Hall A: E97-110 (Chen, Deur, Garibaldi) — “small-angle GDH/n”
 $\Gamma_1^{3\text{He}}(Q^2), I_{TT}^{3\text{He}}(Q^2), \gamma_0^{3\text{He}}(Q^2), \dots$
 $\Rightarrow n$
- Hall B: EG4 / E03-006 (Ripani, Battaglieri, Deur, de Vita) — “small-angle GDH/p”
 $\Gamma_1^p(Q^2), I_{TT}^p(Q^2), \gamma_0^p(Q^2), \dots$ at low Q^2
- Hall B: EG4 / E05-111 (Deur, Dodge, Ripani, Slifer)
 $\Gamma_1^d(Q^2), I_{TT}^d(Q^2), \gamma_0^d(Q^2), \dots$ at low Q^2
 $\Rightarrow n$
- Hall A: E08-027 (Camsonne, Chen, Crabb, Slifer)
 $g_1^p(x, Q^2), g_2^p(x, Q^2), I_{TT}^p(Q^2), \dots$ at low Q^2 (only one Q^2 point for I_{TT}^p)

$$\Gamma_1^p(Q^2) = \int_0^{1^-} g_1^p(x, Q^2) dx \rightarrow -\frac{Q^2 K_p^2}{8M^2} \text{ as } Q^2 \rightarrow 0$$

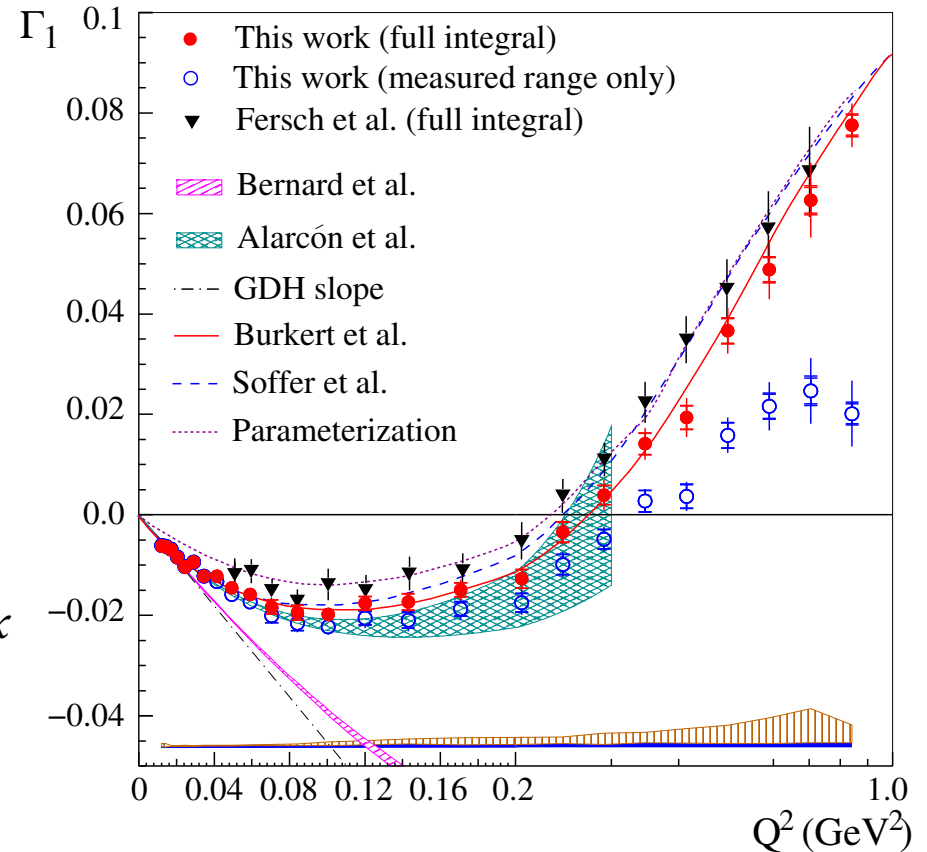
- GDH sum given by the slope of $\Gamma_1^p(Q^2)$ at $Q^2 = 0$
- Proton target, very low Q^2 :

proton



- ▷ $W \geq 1.15$ GeV (avoid elastic tail)
- ▷ Used parameterization of previous data to evaluate contributions from the low- x region (down to $x \approx 10^{-3}$) and the high- x region (from W_{thr} up to 1.15 GeV)
- ▷ Offers unique test of χ EFT

Zheng++, Nat. Phys. 17, 736 (2021)



The slope of $\Gamma_1^p(Q^2) \rightarrow$ the value of $I_{TT}^p(Q^2)$ at $Q^2 = 0$

Recall:

$$\frac{8\pi^2 \alpha}{M^2} I_{TT}(0) = -\frac{2\pi^2 \alpha \kappa^2}{M^2} = -I_{\text{GDH}}$$

- EG4 result on proton:

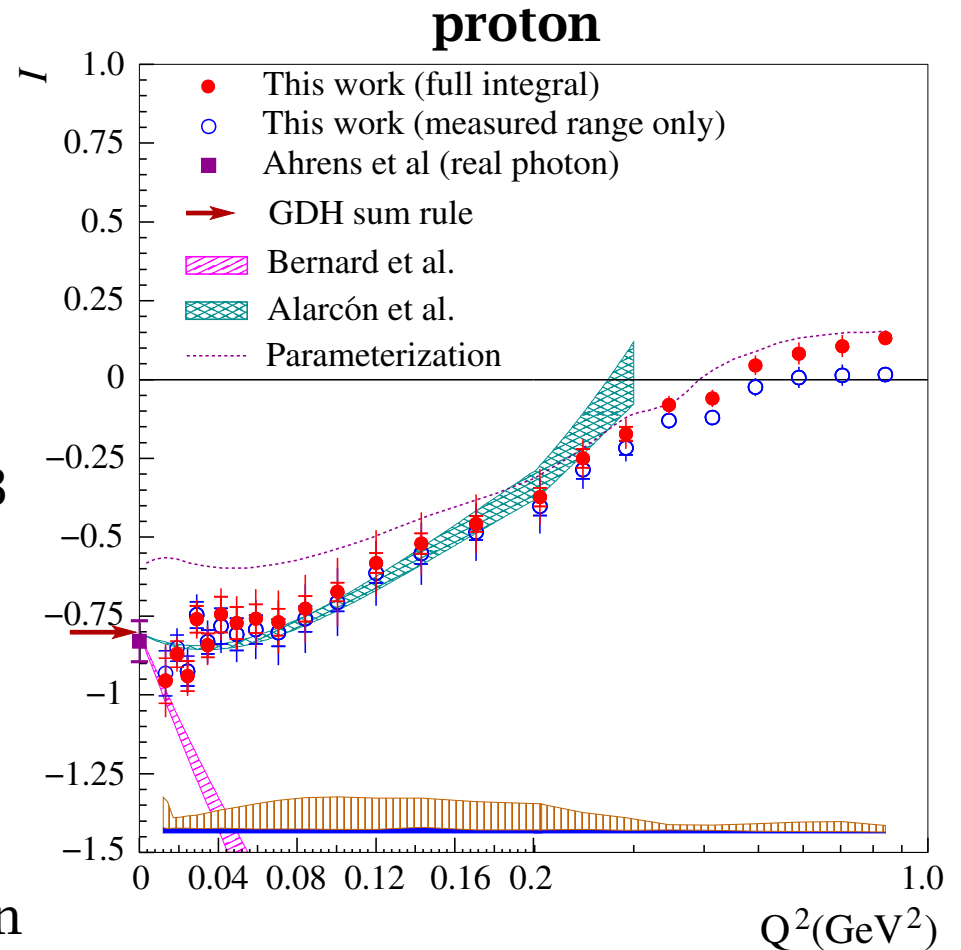
$$I_{TT}^{p,\text{EG4}}(0) = -0.798 \pm 0.042$$

$$I_{TT}^p(\text{GDH}) = -\frac{1}{4}\kappa_p^2 = -0.804 \dots$$

$$I_{TT}^p(\text{MAMI}) = -0.832 \pm 0.023 \pm 0.063$$

(from photo-production)

- Issue of $Q^2 \rightarrow 0$ extrapolation:
Manifestly Lorentz-invariant B χ PT
vs. heavy-baryon frameworks
- Even more pertinent (and drastic) in
the case of generalized longitudinal
spin polarizability



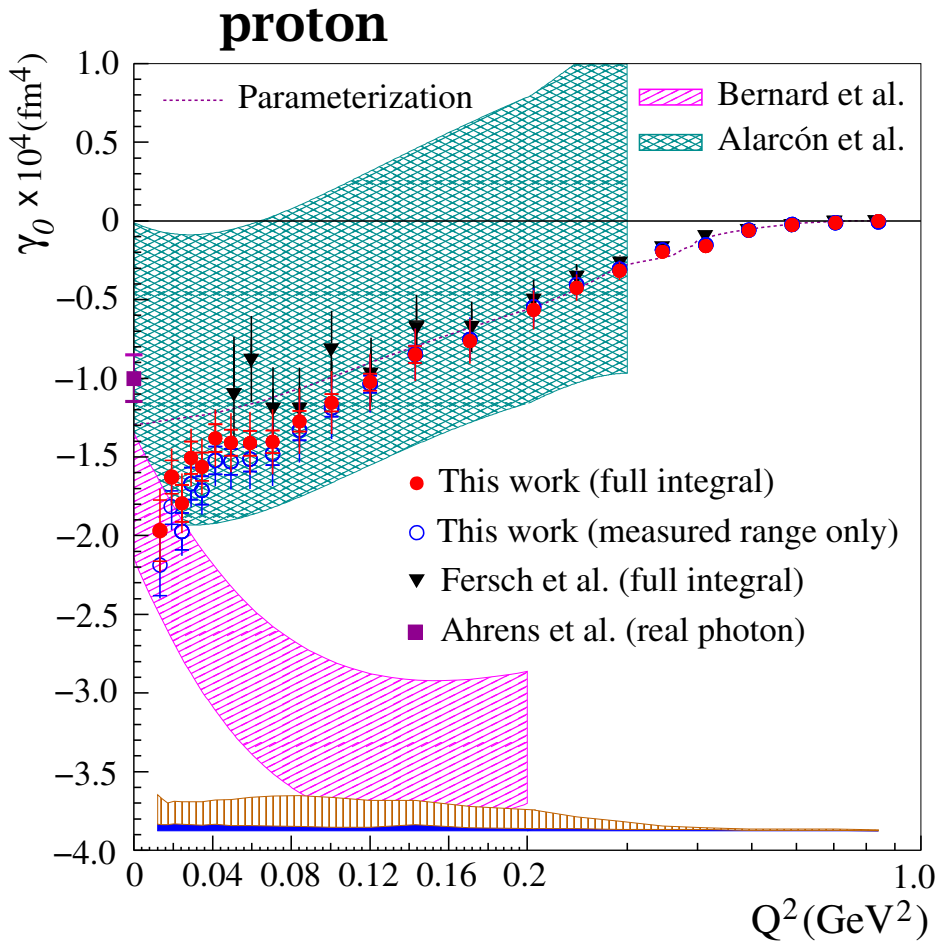
Zheng++, Nat. Phys. **17**, 736 (2021)

Alarcon++, PRD **102**, 114026 (2020)

Spin polarizability γ_0 , proton

$$\gamma_0(Q^2) = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} x^2 g_1(x, Q^2) dx$$

(if $x^2 g_2(x, Q^2)$ contribution neglected)

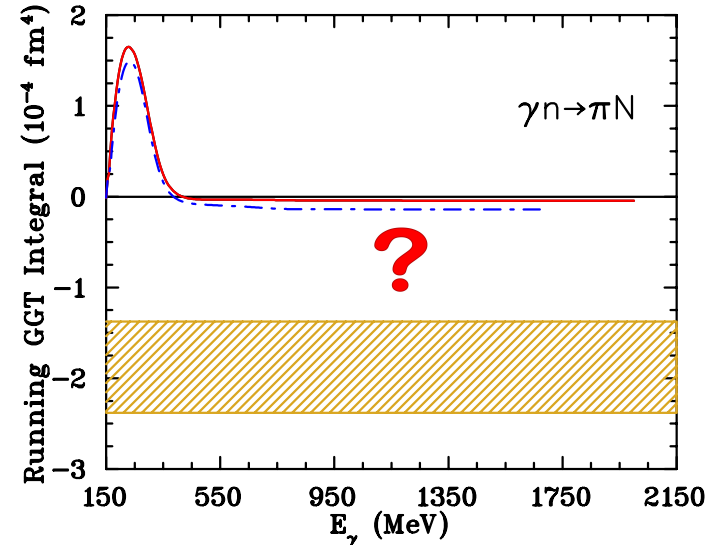
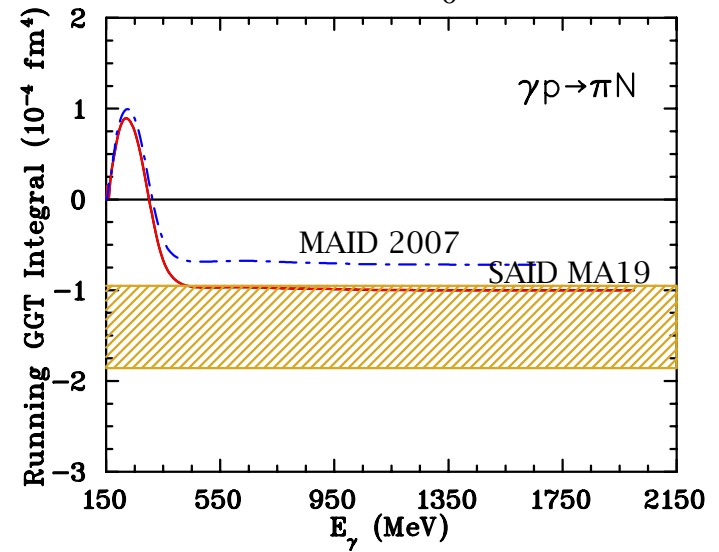


Zheng++, Nat. Phys. 17, 736 (2021)

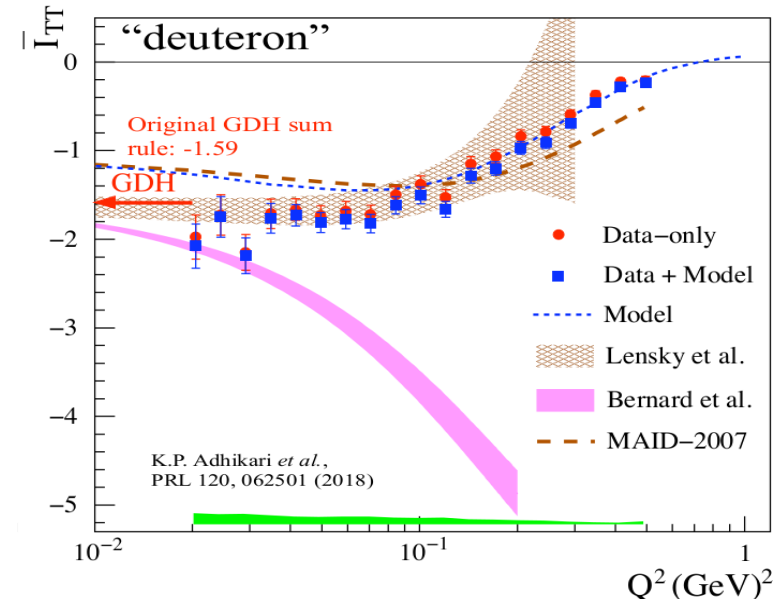
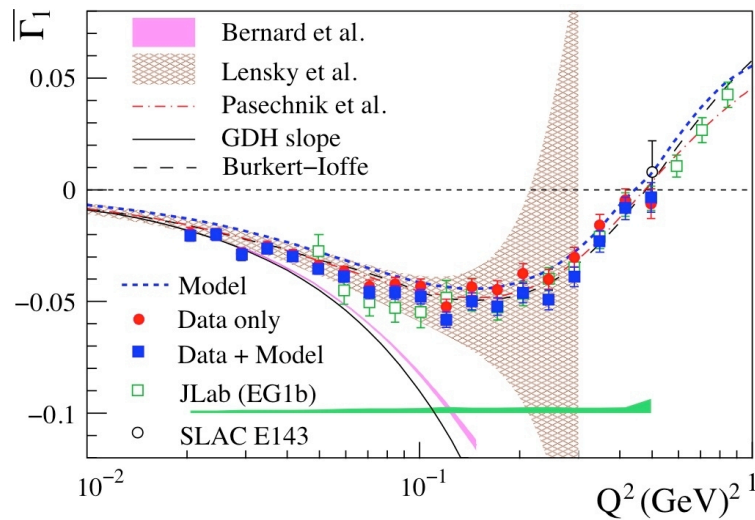
Strakovsky++, PRC 105, 045202 (2022)

... compare to single- π contribution to the “running” GGT integral

$$I_{\text{GGT}}(\nu) = -\frac{1}{4\pi^2} \int_{\nu_0}^{\nu} \frac{\Delta\sigma(\nu')}{\nu'^3} d\nu'$$



Same exercise, deuteron ...



- Photo-disintegration part excluded
 \Rightarrow “deuteron” \approx p+n ($I_{TT}^d = I_{TT}^p + I_{TT}^n$)

$$I_{TT}^{d,EG^4}(0) = -1.724 \pm 0.027 \pm 0.050$$

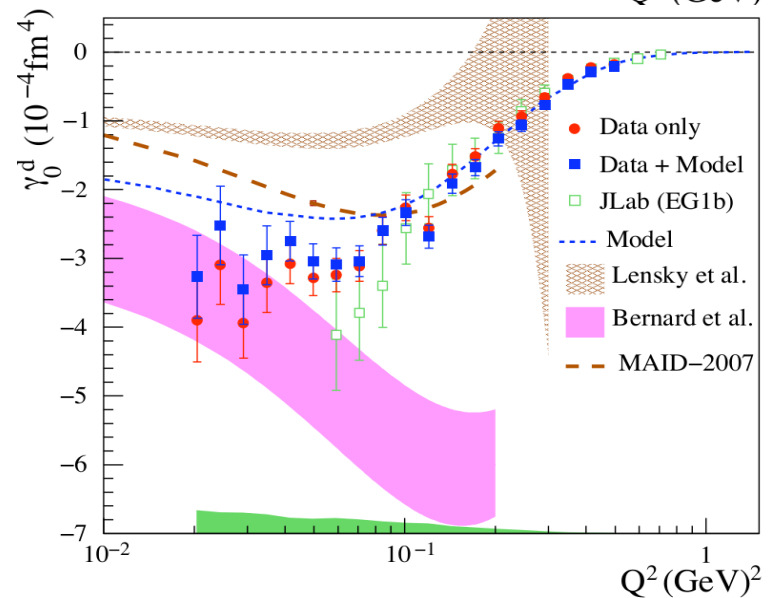
$$I_{TT}^d(\text{GDH}) = -1.59 \dots$$

\Rightarrow extracted neutron information:

$$I_{TT}^{n,EG^4}(0) = -0.955 \pm 0.040 \pm 0.113$$

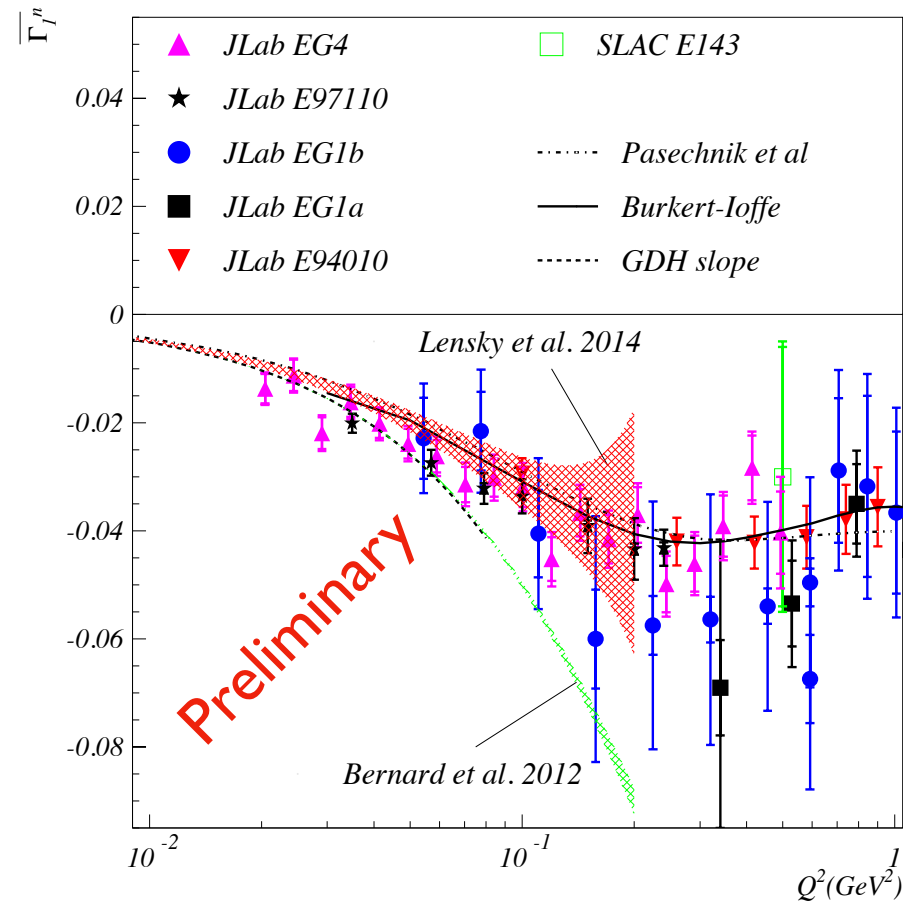
$$I_{TT}^n(\text{GDH}) = -0.803 \dots$$

(agreement not so good ...)



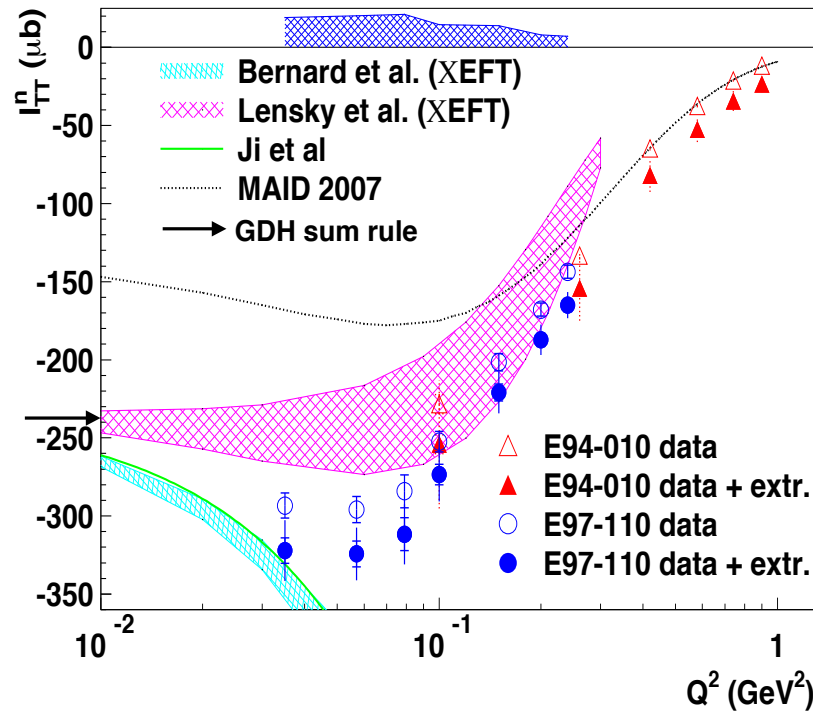
Results on $\Gamma_1^n(Q^2)$ from E97-110 (^3He) and EG4 (d)

$$\Gamma_1^n = 2\Gamma_1^d / (1 - 1.5\omega_D) - \Gamma_1^p, \quad \Gamma_1^p = \int_0^{1-} g_1^p(x, Q^2) dx$$

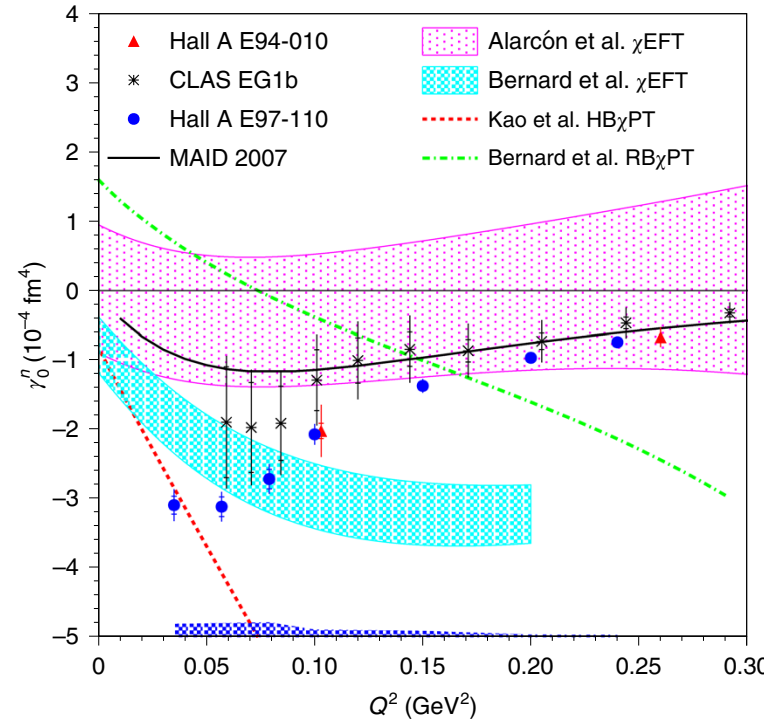


- Good mutual agreement E97-110 \iff EG4
- Good description in terms of NLO χ PT at lowest Q^2

$I_{TT}^n(Q^2)$ and γ_0^n from E97-110 alone



Sulkosky++, PLB 805, 135428 (2020)

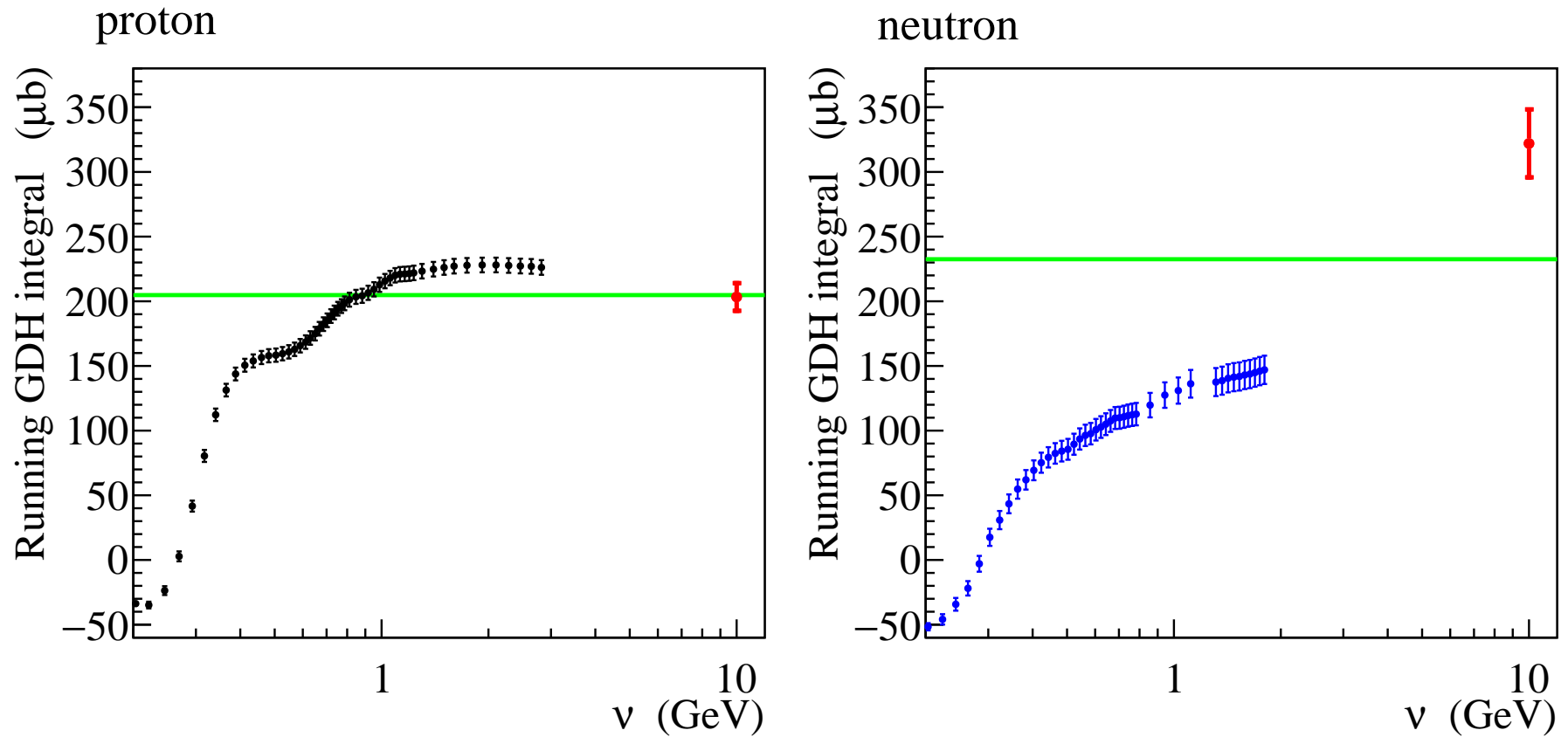


Sulkosky++, Nat. Phys. 17, 687 (2021)

- Agreement with older data (E94-010, EG1b) at larger Q^2
- Poor match to either of the competing NLO χPT calculations
- Disagreement with MAID

Running GDH integral

$$\int_{\nu_0}^{\nu} \frac{\Delta\sigma(\nu')}{\nu'} d\nu'$$



Contributions below 0.2 GeV: $\approx -28 \mu\text{b}$ (proton), $\approx -41 \mu\text{b}$ (neutron)

Red points (not really at $\nu = 10!$): from generalized GDH integral at $Q^2 \rightarrow 0$

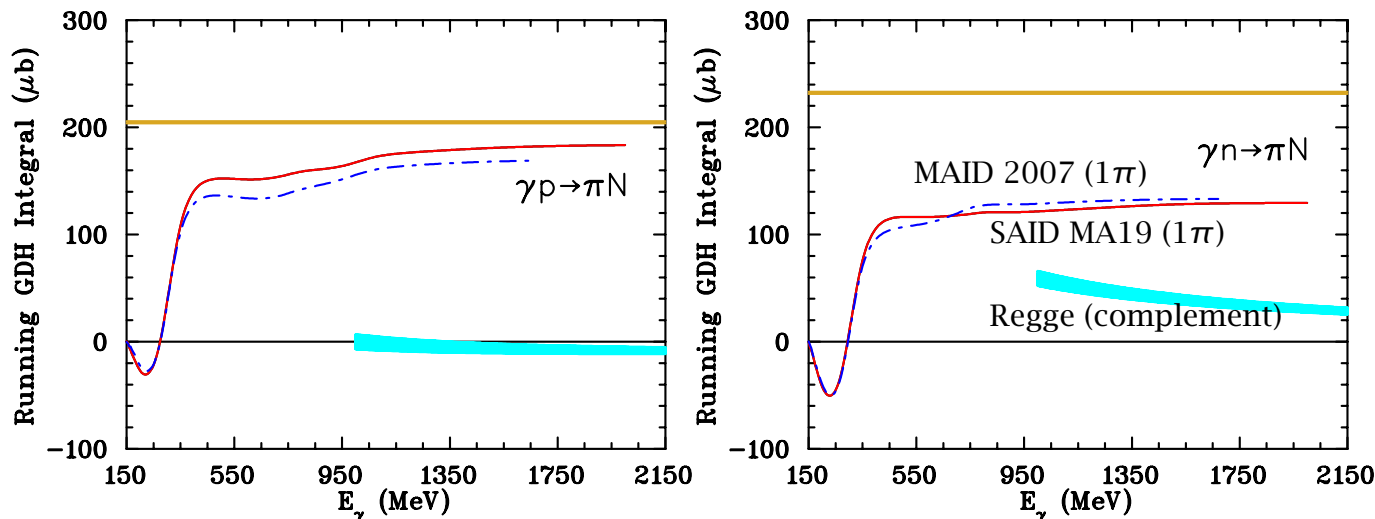
Individual contributions to the running GDH integral

TABLE 2 The contribution of various decay channels to the GDH integral I and the forward spin polarizability γ_0 . The integration extends to $\nu_{\max} = 1.67$ GeV ($W_{\max} = 2$ GeV) except that the two-pion contribution is integrated only up to $\nu_{\max} = 800$ MeV

Reference	Proton	I_p	γ_0^p	Neutron	I_n	γ_0^n
(34)/(49)	$\pi^0 p$	157/142	-1.46/-1.40	$\pi^0 n$	145/147	-1.44/-1.44
(34)/(49)	$\pi^+ n$	7.5/44	0.82/0.55	$\pi^- p$	-21/-13	1.53/1.36
(54)	ηp	-9.0	0.01	ηn	-5.9	0.01
(55)	$\pi\pi N$	28	-0.07	$\pi\pi N$	19	-0.05
(53)	$K\Lambda, K\Sigma$	-4.0	<0.01	$K\Lambda, K\Sigma$	2.0	<0.01
(53)	$\omega p, \rho N$	-3.0	<0.01	$\omega n, \rho N$	2.1	<0.01
(44)/(45)*	Regge	-25/-9	<0.01	Regge	31/16	<0.01

p , contribution below ν_0 is of EM origin & suppressed by $\kappa_{\text{QED}}/\kappa_p \approx 10^{-3}$ ($\kappa_{\text{QED}} = \alpha/2\pi =$ Schwinger correction)

Drechsel, Walcher, Annu. Rev. Nucl. Part. Sci. **54**, 69 (2004)



Strakovsky++, PRC **105**, 045202 (2022)

The GDH integrand in the Regge framework

s -dependence of real/virtual polarized photo-absorption:

$$\Delta\sigma = \left[I c_1 s^{\alpha_{a_1}-1} + c_2 s^{\alpha_{f_1}-1} + c_3 \frac{\log s}{s} + \frac{c_4}{\log^2 s} \right] F(s, Q^2)$$

$I = \pm 1 = p/n$ isospin factor, $\alpha_{a_1}, \alpha_{f_1} =$ intercepts of a_1 and f_1 Regge trajectories

For $Q^2 = 0$, log terms negligible, $F(s, Q^2)$ simplifies to a constant \rightarrow absorb in $c_1, c_2 \Rightarrow$

$$\underline{\Delta\sigma = I c_1 s^{\alpha_{a_1}-1} + c_2 s^{\alpha_{f_1}-1}}$$

$$c_1 = (-34.1 \pm 5.7) \mu\text{b}, \alpha_{a_1} = 0.42 \pm 0.23, c_2 = (209.4 \pm 29.0) \mu\text{b}, \alpha_{f_1} = -0.66 \pm 0.22$$

Decompose κ_p, κ_n into iv/is components, $\kappa_p = (\kappa_s + \kappa_v)/2, \kappa_n = (\kappa_s - \kappa_v)/2$

$$\Rightarrow \kappa_{p,n}^2 = \frac{1}{4}\kappa_s^2 \pm \frac{1}{2}\kappa_v\kappa_s + \frac{1}{4}\kappa_v^2$$

Split the GDH sum rule accordingly ($I_{\text{GDH}}^{\text{SS}}, I_{\text{GDH}}^{\text{VV}}$, and $I_{\text{GDH}}^{\text{VS}}$)

$$\Rightarrow I_{\text{GDH}}^{\text{VS}} = \int_{E_y^{\text{thr}}}^{\infty} (\sigma_{3/2}^{\text{VS}} - \sigma_{1/2}^{\text{VS}}) \frac{dE_y}{E_y} = \frac{1}{2}\kappa_v\kappa_s \frac{2\pi^2\alpha}{M^2}$$

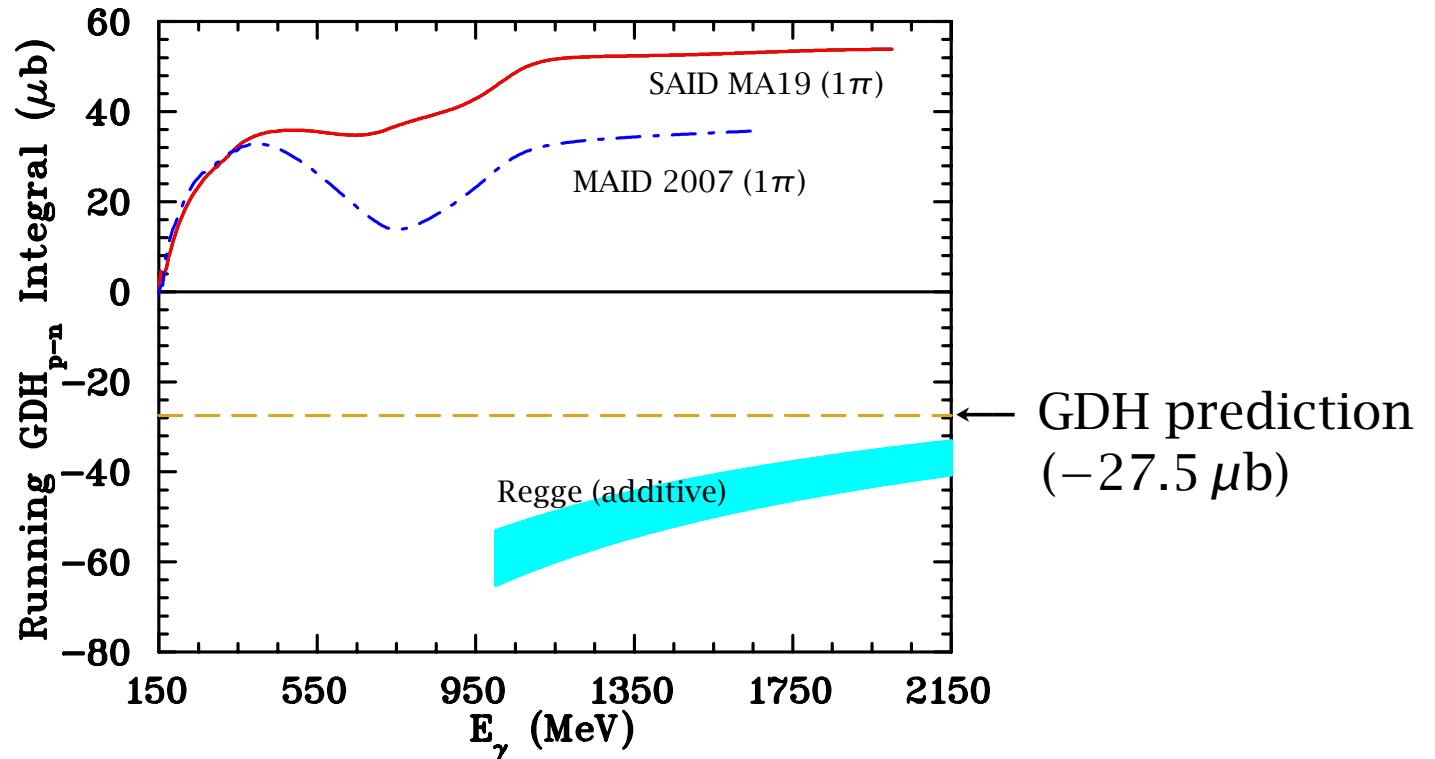
Since $\kappa_p^2 - \kappa_n^2 = \kappa_v\kappa_s$, the isovector GDH sum rule amounts to

$$\underline{\int_{E_y^{\text{thr}}}^{\infty} \frac{\Delta\sigma_{p-n}}{E_y} dE_y = 2I_{\text{GDH}}^{\text{VS}} \approx -27.5 \mu\text{b}}$$

Isvector GDH sum rule à la Regge

In Regge theory, $\Delta\sigma_{p-n}$ is driven by the a_1 trajectory alone:

$$\Delta\sigma_{p-n}^{\text{Regge}} = 2c_1 s^{\alpha_{a_1}-1}$$



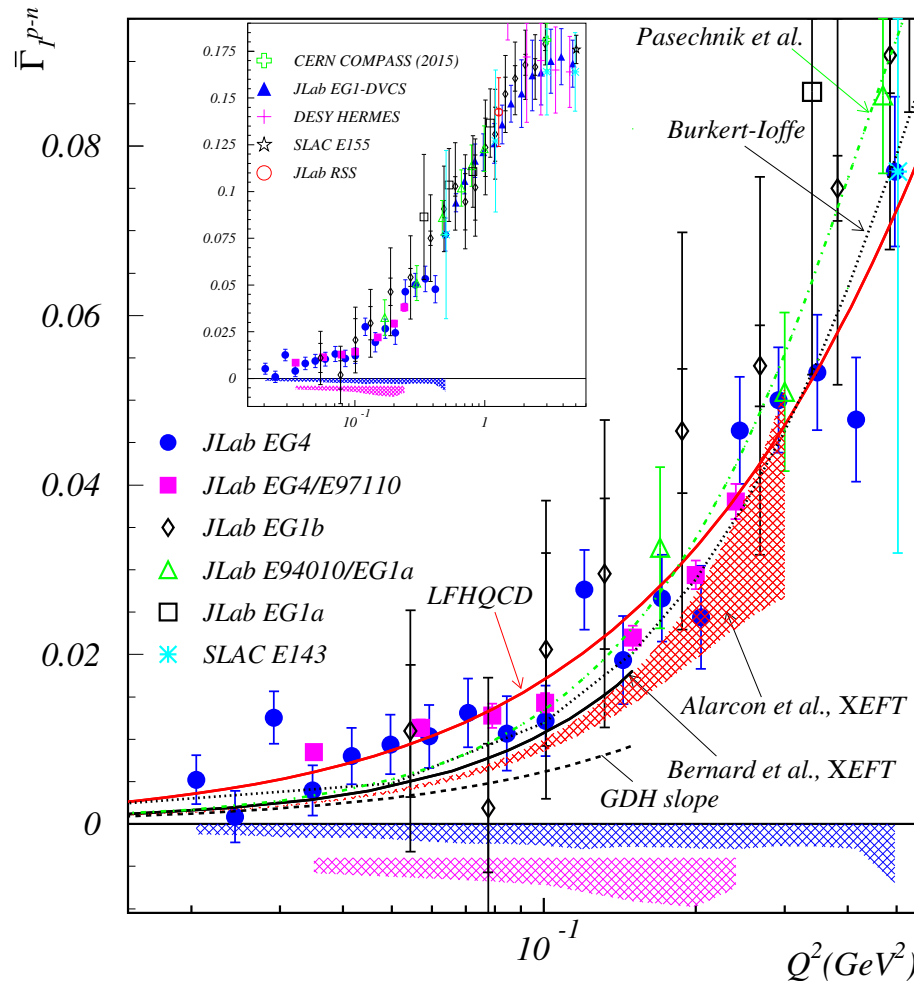
Strakovsky++, PRC 105, 045202 (2022)

⇒ Understanding the magnitude and sign of α_{a_1} is important

⇒ “REGGE” — JLab Experiment E12-20-011

Isovector GDH sum rule vs. Bjorken sum at very low Q^2

$$\bar{\Gamma}_1^{p-n}(Q^2) \Big|_{Q^2 \rightarrow 0} = \frac{Q^2}{8} \left(\frac{\kappa_n^2}{M_n^2} - \frac{\kappa_p^2}{M_p^2} \right)$$



Best fit of the world data on $\bar{\Gamma}_1^{p-n}(Q^2)$ (full integral, with low- x contribution) using a fit function $bQ^2 + cQ^4$. The fit is performed up to $Q^2 = 0.244 \text{ GeV}^2$. The “*uncor*” uncertainty designates the point-to-point uncorrelated uncertainty. It is the quadratic sum of the statistical uncertainty and a fraction of the systematic uncertainty determined so that $\chi^2/n.d.f = 1$ for the best fit, see Appendix. The “*cor*” uncertainty is the correlated uncertainty estimated from the remaining fraction of the systematic uncertainty. Also listed are results of fits applied to the predictions from χ EFT and models.

Data set	$(b \pm \text{uncor} \pm \text{cor}) [\text{GeV}^{-2}]$	$c \pm \text{uncor} \pm \text{cor} [\text{GeV}^{-4}]$
World data	$0.182 \pm 0.016 \pm 0.034$	$-0.117 \pm 0.091 \pm 0.095$
GDH Sum Rule [17]	0.0618	-
χ EFT Bernard et al. [13]	0.07	0.3
χ EFT Alarc3n et al. [15]	0.066(4)	0.25(12)
Burkert-Ioffe [29]	0.09	0.3
Pasechnik et al. [30]	0.09	0.4
LFHQCD [35]	0.177	-0.067

\Rightarrow only marginal agreement with χ EFT (somewhat surprising as contribution of $\Delta(1232)$ suppressed in this observable)

EG4 (p, d), E97-110 (^3He)
 Deur++, PLB **825**, 136878 (2022)

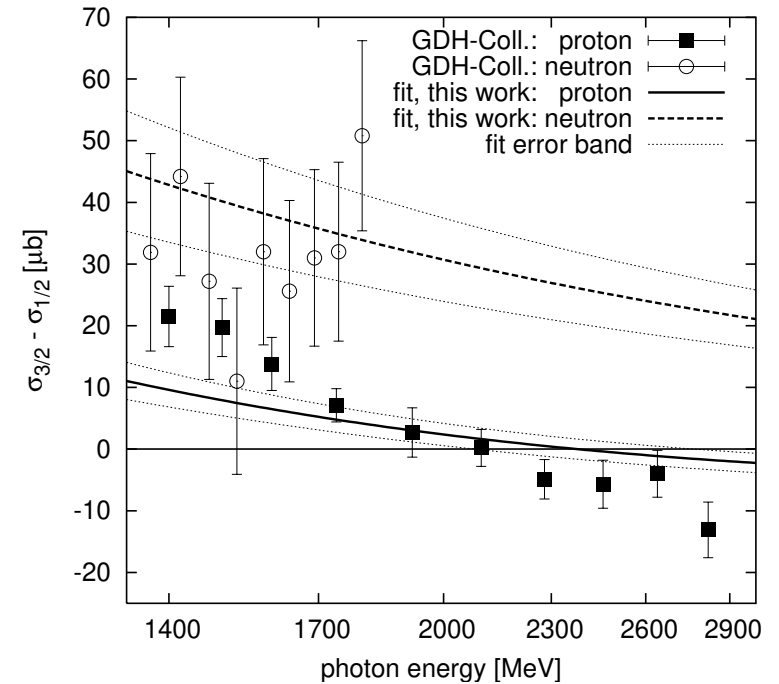
New GDH effort: “REGGE” — JLab Experiment E12-20-011

(M. M. Dalton, A. Deur, SŠ, J. Stevens)

- $\Delta\sigma$ at high ν unknown
- High ν = domain of Regge theory
- If the GDH sum rule failed, it would happen at high ν (not in the low- ν region, even if it dominates in the sum)

Strategy:

- ▷ Measure on both **proton** and **neutron** (deuteron) to allow for isospin separation
Regge: is/iv contributions to $\Delta\sigma$ come from different meson families: $f_1(1285)/a_1(1260)$
- ▷ Extend energy coverage: $3 < \nu < 12 \text{ GeV}$
- ▷ Hall D @ JLab ideally suited for this study
cross-check with MAMI/ELSA at $\nu < 3 \text{ GeV}$ would be nice, but invasive to other Halls
- ▷ Measure yield difference $\Delta Y(\nu) = N^+ - N^-$
 - make sure $\Delta\sigma(\nu)/\nu$ decreases rapidly enough
 - investigate the power-law behavior of $\Delta\sigma(\nu)$, i.e. establish b in $\Delta\sigma(\nu) = a\nu^b$
- (▷ Determine absolute $\Delta\sigma(\nu)$: later)



“REGGE” — JLab Experiment E12-20-011

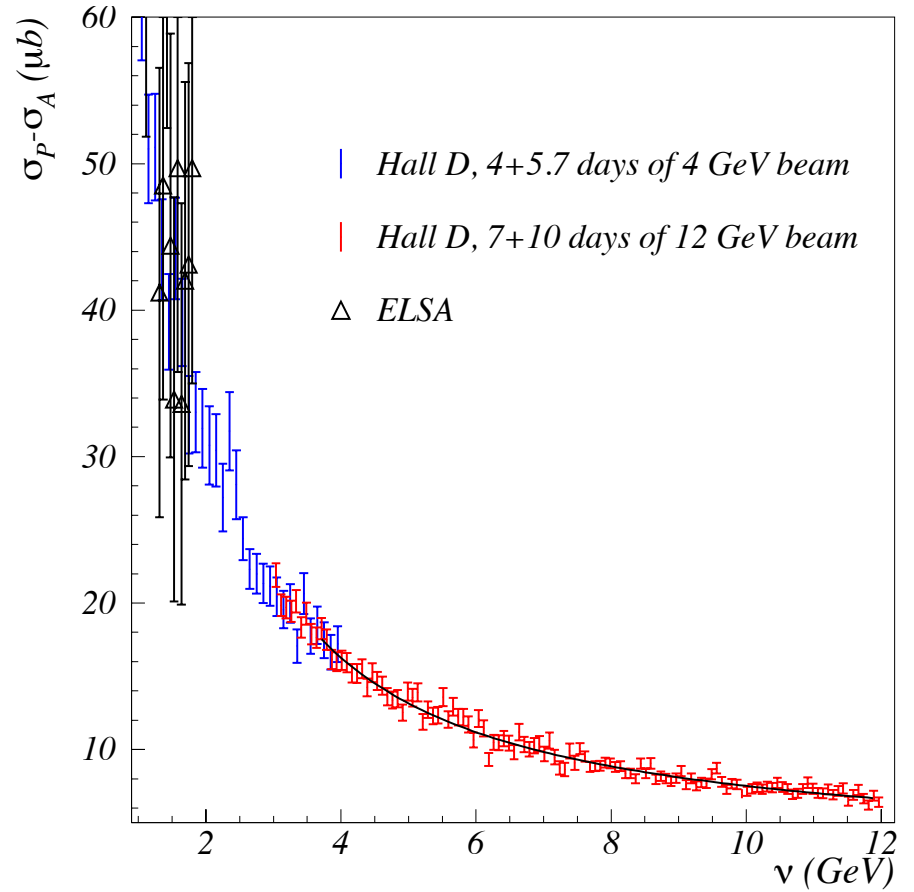
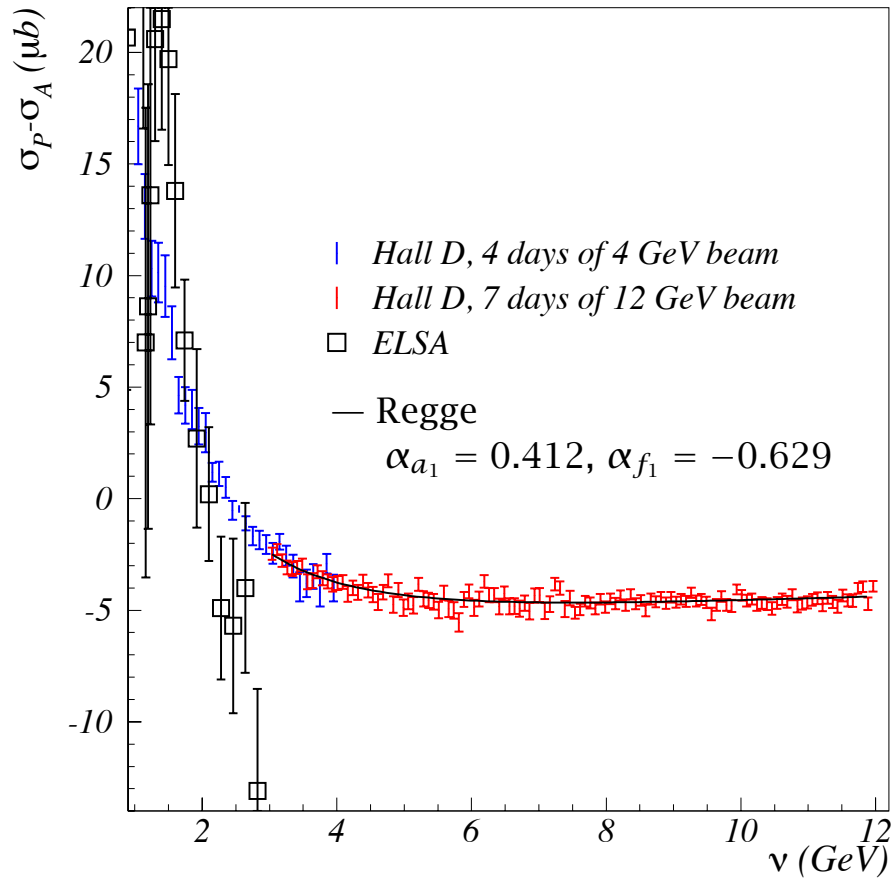
Setup:

- **Circularly polarized tagged photon beam** ✓
Generated by electrons from CEBAF with $P_e \approx 80\%$ on amorphous radiator
Increasing P_e at large ν compensates the decrease in bremsstrahlung flux and XS
- **Longitudinally polarized target: (a new) FROST**
Chosen against HDice (= does not allow extension to polarization of heavier nuclei)
Dynamical nuclear polarization on butanol (C_4H_9OH), p and d polarizations up to 90%
Desired sustainable flux: $\approx 10^8/s$ or more
Dilution (and other unpolarized backgrounds) cancel:
 $(N^+ + N^0) - (N^- + N^0) = N^+ - N^-$
- **Large solid angle detector** ✓
FCal (with $PbWO_4$ upgrade), BCal: 0.4° to 145° polar, 2π azimuthal coverage
Unpolarized XS $\approx 120 \mu b \Rightarrow$ DAQ rate ≈ 33 kHz on H-butanol, ≈ 40 kHz on D-butanol
+ target window + EM backgrounds
- Note: solely to establish the fall-off of $\Delta\sigma(\nu)/\nu$, the ν -independent normalization factors (flux, ρ_t , P_e , P_t , $\int \Delta\Omega$) are **irrelevant**

“REGGE” — Expected results

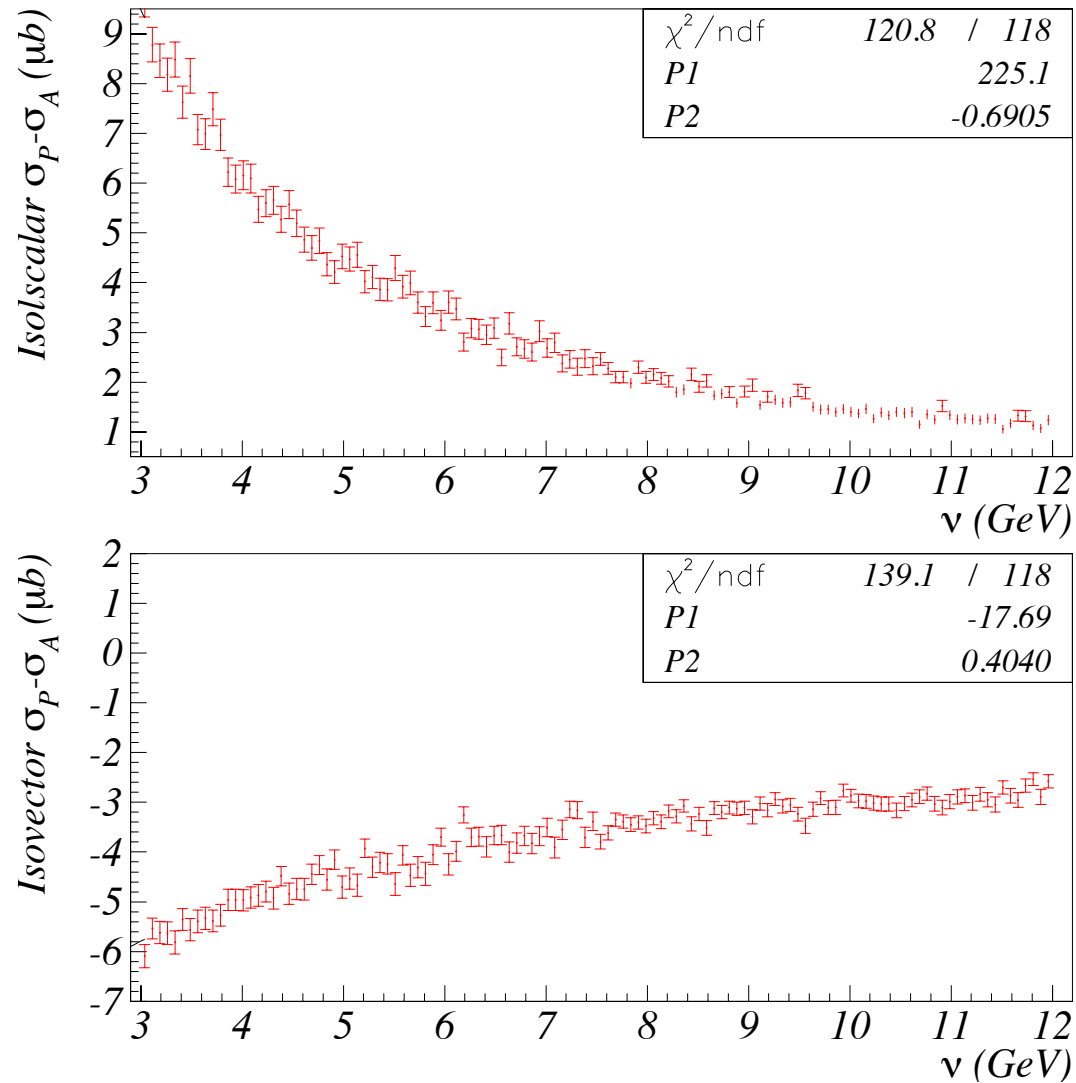
proton

neutron (from deuteron)



“REGGE” — Isospin decomposition

Based on the subtraction $\Delta\sigma_n = \Delta\sigma_d/(1 - 1.5\omega_D) - \Delta\sigma_p$



(Select) motivation for “REGGE”

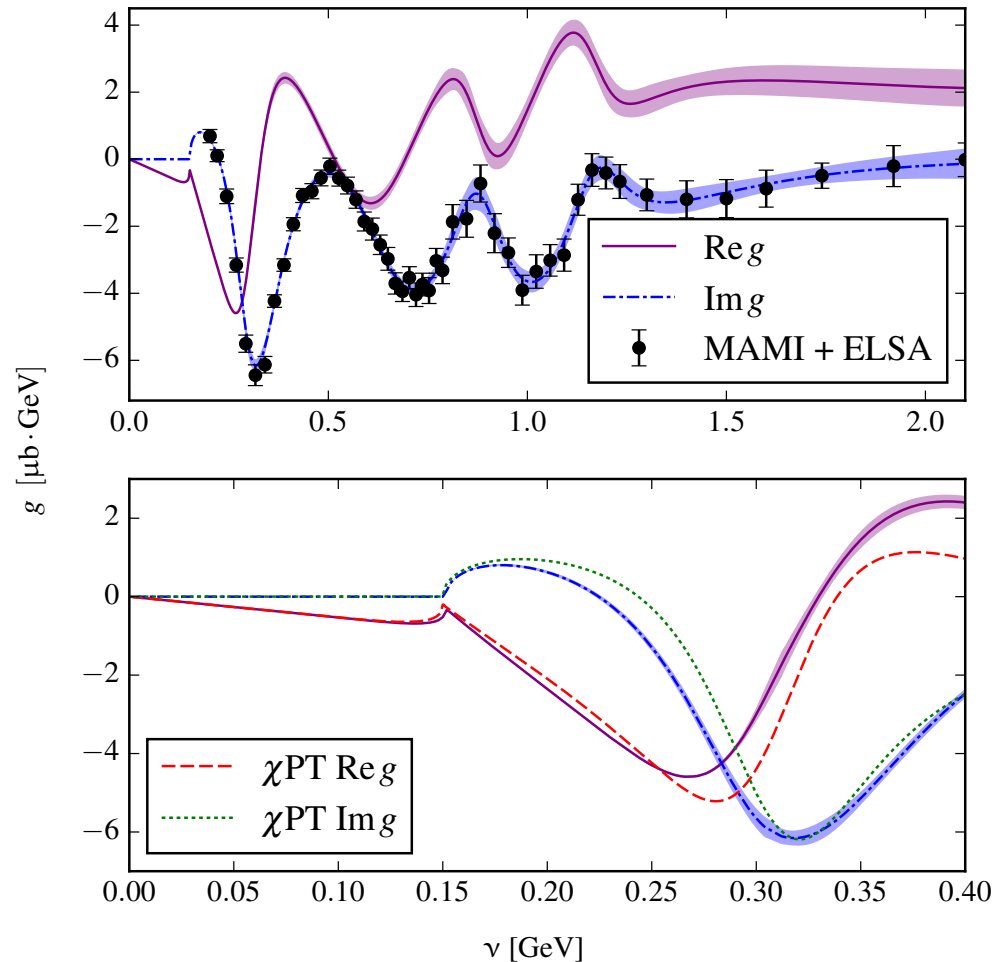
- Access Compton physics without resorting to dedicated Compton setup
- Relation of $\Delta\sigma$ to spin-dependent Compton amplitude g :

$$\text{Im } g(\varepsilon) = \frac{\varepsilon}{8\pi} (\sigma_{3/2} - \sigma_{1/2})$$

- Access to the real part via DR:

$$\text{Re } g(\nu) = \frac{2\nu}{\pi} P \int_0^\infty \frac{\text{Im } g(\varepsilon)}{\varepsilon^2 - \nu^2} d\varepsilon$$

⇒ Extend $\text{Re } g - \text{Im } g$ “symbiosis” cross-check to beyond 10 GeV (sixfold energy range)



Hagelstein++, Prog. Part. Nucl. Phys. **88**, 29 (2016)

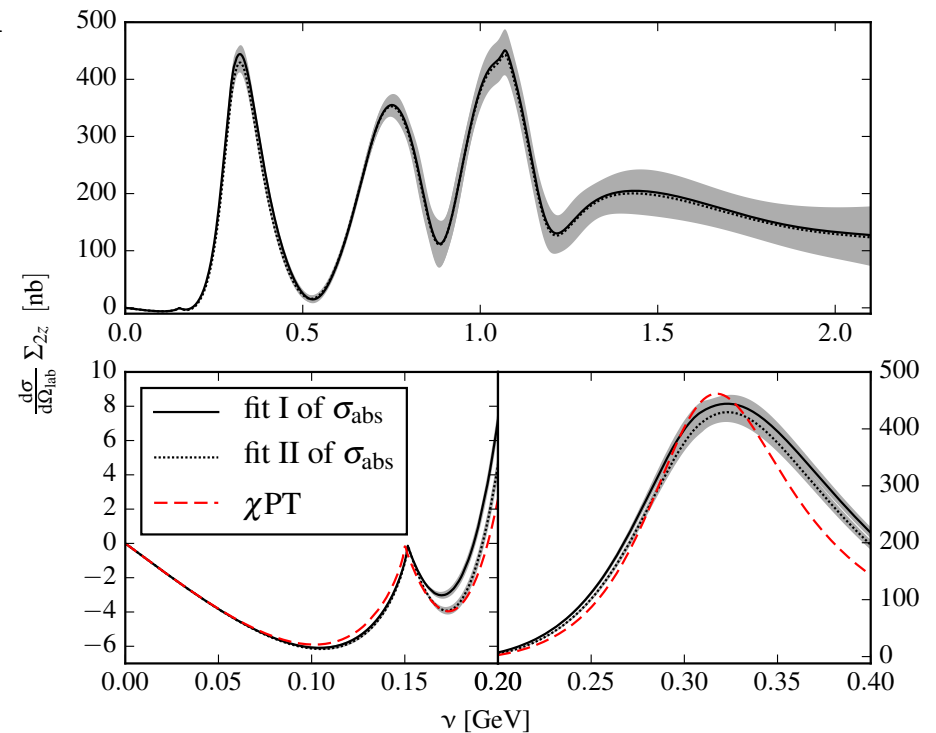
(Select) motivation for “REGGE”

- If both $\text{Re } g$ and $\text{Im } g$ are known precisely enough (and given f , the unpolarized amplitude, which is well measured), one can determine the differential XS and the beam-target asymmetry in the fwd direction:

$$\left. \frac{d\sigma}{d\Omega} \right|_{\theta=0} = |f|^2 + |g|^2, \quad \Sigma_{2z}|_{\theta=0} = -\frac{2\text{Re}(fg^*)}{|f|^2 + |g|^2}$$

- $\Sigma_{2z} = \Delta\sigma / \sigma_{\text{tot}}$ provides information on (all four) spin polarizabilities; very sensitive to chiral loops

⇒ Reduce uncertainties of Σ_{2z} by precise measurements of $\Delta\sigma(\nu)$ at high ν



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(Select) motivation for “REGGE”

- Regge: $\Delta\sigma_{p-n}$ driven by the a_1 trajectory:

$$\Delta\sigma_{p-n}^{\text{Regge}} = 2c_1 s^{\alpha_{a_1}-1}$$

- Conflicting determinations:

	α_{a_1}
DIS fit (approx. values)	0.45
Photo/electro-production fit	0.31 ± 0.04
Regge expectation	-0.34

- Problem: $a_1(1260)$ is the only $I^G(J^{PC}) = 1^-(1^{++})$ meson to form a “trajectory”, while the second candidate, the $a_1(1640)$, has been omitted from the PDG Summary Tables (needs confirmation)

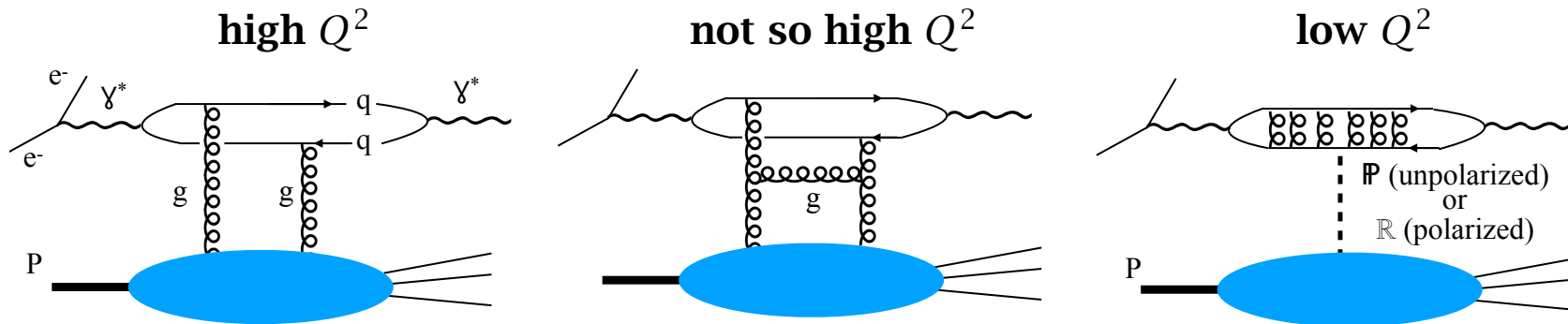
⇒ A precise measurement of $\Delta\sigma$ at high ν for both proton and neutron targets would help to remove this uncertainty. → Note: the intercept is given by

$$\alpha_{a_1} = 1 - \alpha' m_{a_1}^2$$

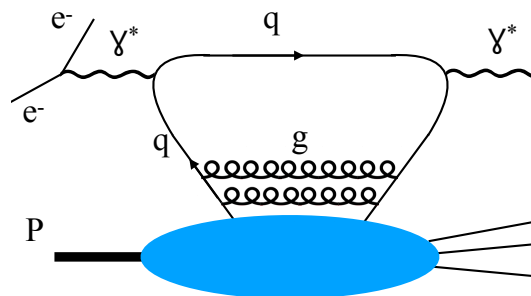
where $\alpha' = 1/(2\pi\sigma) \approx 0.88 \text{ GeV}^{-2}$ and σ is the string tension

(Select) motivation for “REGGE”

- Explore transition between polarized DIS and diffraction regimes
- Diffractive scattering \Leftrightarrow diquark picture



- Other mechanisms exist, connecting to DIS parton model, e. g.



- Doubly-polarized $\vec{e}-\vec{p}$ scattering filters out \mathbb{P} exchanges to reveal non-singlet \mathbb{R} exchange \Rightarrow relevant to EIC

(Select) motivation for “REGGE”

- Polarizability correction to hyperfine splitting in hydrogen

$$E_{\text{HFS}}(nS) = [1 + \Delta_{\text{QED}} + \Delta_{\text{weak}} + \Delta_{\text{structure}}] E_{\text{Fermi}}(nS)$$

$$\Delta_{\text{structure}} = \Delta_Z + \Delta_{\text{recoil}} + \Delta_{\text{pol}}$$

Relative uncertainties of the three terms: 140 ppm, 0.8 ppm, 86 ppm, respectively vs. precision of forthcoming PSI measurement of E_{HFS} : 1 ppm

“REGGE” can contribute to the uncertainty reduction of Δ_{pol} :

$$\Delta_{\text{pol}} = \frac{\alpha m_{e/\mu}}{2\pi(1 + \kappa)M} [\delta_1 + \delta_2]$$

$$\delta_1 = 2 \int_0^\infty \frac{dQ}{Q} \left(\{ \dots \} + \frac{8M^2}{Q^2} \int_0^{x_0} dx g_1(x, Q^2) \{ \dots \} \right)$$

The GDH integrand at general values of ν and Q^2 :

$$\Delta\sigma(\nu) = -\frac{8\pi^2\alpha}{MK_{y^*}} \left(g_1(\nu, Q^2) - \frac{Q^2}{\nu^2} g_2(\nu, Q^2) \right)$$

→ see also next talk by D. Ruth

Work in progress: “REGGEon” — JLab LOI12-23-004

(M. M. Dalton, A. Deur, SŠ, J. Stevens)

REGGEon == REGGE on Nuclei

Magnetic moment of particle with charge e_0Q , mass M and spin \vec{S} :

$$\vec{\mu} = \frac{e_0}{M}(Q + \kappa)\vec{S}$$

Dirac anomalous

For a nucleus of mass $M \approx AM_p$ and charge Ze_0 :

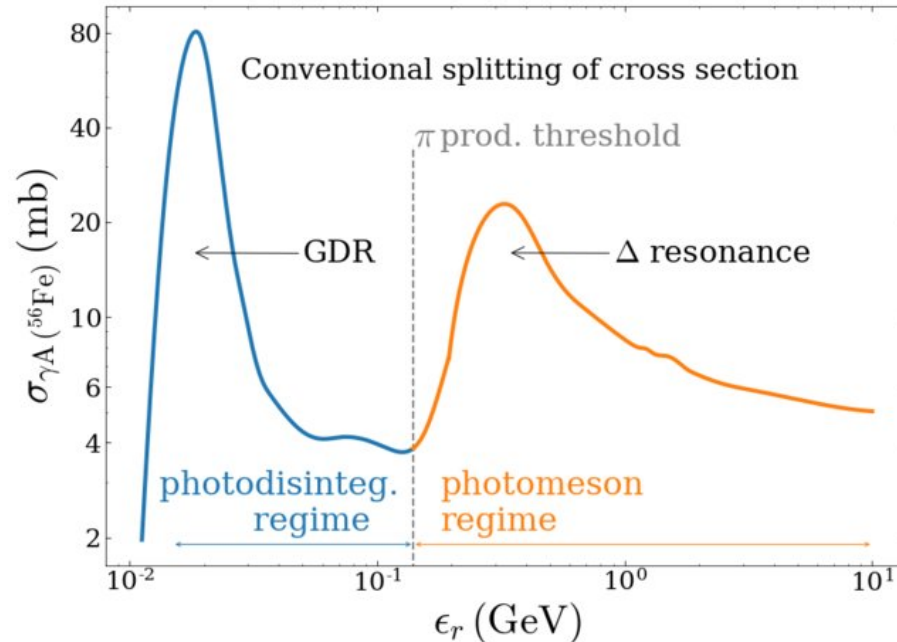
$$\vec{\mu} \approx \frac{e_0}{AM_p}(Z + \kappa)\vec{S} \quad \Rightarrow \quad \kappa = \frac{A}{2|\vec{S}|} \frac{\mu}{\mu_N} - Z$$

⇒ Compute κ for all stable nuclei with non-zero spin

⇒ Compute the static part of the GDH sum

“REGGEON” — Photo-disintegration vs. photo-production

The GDH integral for a **nucleus** has contributions from the whole photo-absorption spectrum:



(Note: no data on the polarized XS, $\Delta\sigma$, exist for $A > 3$!)

Region below π threshold: dominated by properties of *nucleus*

Region above it: dominated by properties of *nucleons*

(coherent photo-production: small)

Example: ${}^7\text{Li}$ ($J^P = \frac{3}{2}^-$): polarization carried by single $1p_{3/2}$ nucleon

$$I_{\text{GDH}}^{p*} \approx 270 \mu\text{b}, I_{\text{GDH}}^p = 204.78 \mu\text{b}, I_{\text{GDH}}^{7\text{Li}} = 83.4 \mu\text{b}$$

“REGGEoN” — Modification of properties of bound nucleons

A nucleon in the nuclear medium will be modified

⇒ modification of **both sides** of the *nucleon* sum rule

Bass, Acta Phys. Pol. B **52**, 42 (2021)

Bass++, arXiv:2212.04795 [nucl-th]

Static side: guidance for κ^* , M^* from QMC model:

$$\frac{M_N^*}{M_N} \approx \frac{M_\Delta^*}{M_\Delta} \approx \left(1 - 0.2 \frac{\rho}{\rho_0}\right), \quad \frac{\kappa_N^*}{\kappa_N} \approx \left(1 + 0.1 \frac{\rho}{\rho_0}\right), \quad \rho \ll \rho_0$$

Typical QMC predictions (depending on bag radius):

$$\frac{M_N^*(\rho_0)}{M_N} \approx \mathbf{0.9}, \quad \frac{\kappa_N^*(\rho_0)}{\kappa_N} \approx \mathbf{1.05} \quad \Rightarrow \quad \frac{\left(\frac{\kappa^*(\rho_0)}{M_N^*(\rho_0)}\right)^2}{\left(\frac{\kappa}{M_N}\right)^2} \approx \mathbf{1.3}$$

Saito++, Prog. Part. Nucl. Phys. **58**, 1 (2007)

Saito++, arXiv:2212.04795 [nucl-th]

Dynamic (integral) side: modification of the integral due to in-medium shifts of resonance masses “probed” by the $1/\nu$ factor in the integrand

- ▷ “large” effect for $\Delta(1232)$, $1/\nu \leftrightarrow 1/M_\Delta^*$
- ▷ small effect for $D_{13}(1520)$, $S_{11}(1535)$, ... (?)
- ▷ **3rd resonance region + Regge domain:** situation unclear:
+18 μb – 15 μb for proton vs. **+16 μb – 89 μb** for neutron

Recall the decades of FF-medium-modification efforts!

An example: p recoil polarization components in $^{12}\text{C}(\vec{e}, e' \vec{p})$:

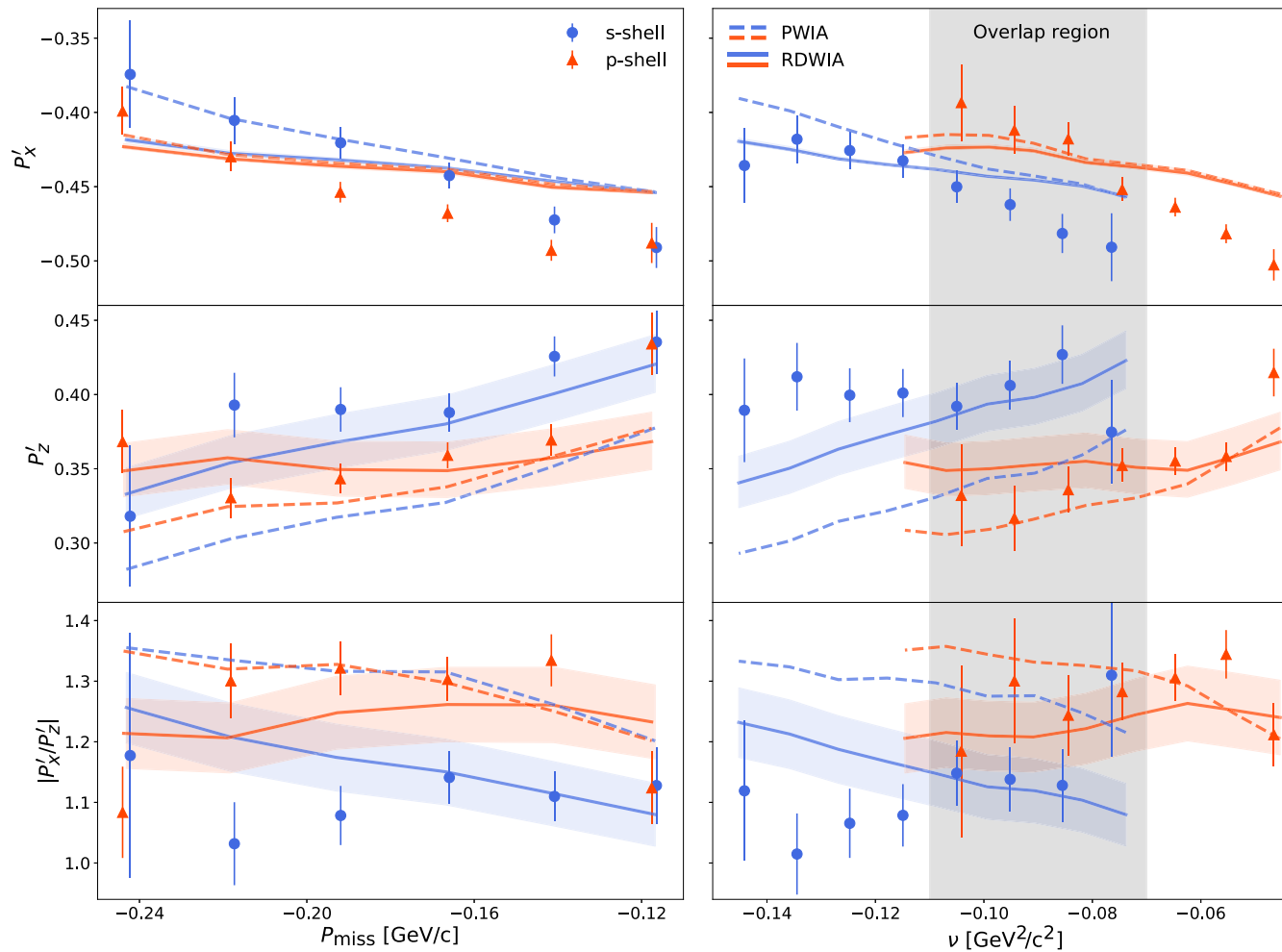


Fig. 3. The measured polarization components P'_x (top), P'_z (middle), and their ratio P'_x/P'_z (bottom) as a function of missing momentum (left) and virtuality (right). Shown are statistical uncertainties only. The lines represent RDWIA and PWIA calculations for the corresponding shell obtained using a slightly modified program from [2] (see text). The shaded colored regions correspond to RDWIA calculations with the form-factor ratio, G_E/G_M , modified by $\pm 5\%$.

Kolar++, PLB 811, 135903 (2020)

“REGGEoN” — Candidate nuclei

	J^π	μ	κ	M	I_{GDH}
^1H	$\frac{1}{2}^+$	2.793	1.793	0.9383	204.8
^2H	1^+	0.857	-0.1426	1.875	0.6484
^3He	$\frac{1}{2}^+$	-2.128	-8.383	2.808	499.9
^7Li	$\frac{3}{2}^-$	3.256	4.598	6.532	83.39
^{13}C	$\frac{1}{2}^-$	0.702	3.131	12.11	3.753
^{17}O	$\frac{5}{2}^+$	-1.894	-14.44	15.83	233.4
^{19}F	$\frac{1}{2}^+$	2.628	40.94	17.69	300.5

- Choice will depend on target feasibility / FOM / other considerations
- The strongest candidate is ^7Li :
 - ▷ Also the subject of unpolarized (E12-10-008) and polarized (E12-14-001: $Q^2 > 1 \text{ GeV}^2$) EMC experiments at JLab
 - ▷ A GDH measurement will provide the $Q^2 \rightarrow 0$ limit ...
 - ▷ ... and help to establish which of the two competing explanations of the EMC effect (MF or SRC) is most likely
- **Low- ν part (up to $\approx 3 \text{ GeV}$) at ELSA? \exists interest in collaboration?**

Conclusions

- Running GDH integral sort-of converges for proton ...
... but not at all convincingly for neutron
 - ▷ Threshold (low- ν) issues
 - ▷ High- ν (“Regge”) concerns
 - ▷ Imbalance of sum rule saturation in terms of
single- π vs. all other channels (p vs. n, GDH vs. GGT)
- Reasonable agreement of real- γ results with extractions
from e -scattering experiments extrapolated to $Q^2 = 0$
 - ▷ Understanding of $I_{\text{GDH}}(Q^2 \rightarrow 0)$, $\gamma_0(Q^2 \rightarrow 0)$, $\Gamma_1(Q^2 \rightarrow 0)$ etc.
not at the same level
- New approved experiment: REGGE in Hall D @ JLab
to study the high- ν behavior of $\Delta\sigma$
- JLab Letter of Intent (June 2023): REGGEoN (= REGGE on Nuclei)