

# Towards High-Precision Spectroscopy of the $1S-2S$ Transition in $\text{He}^+$

Jorge Moreno

Fabian Schmid

Akira Ozawa

Johannes Weitenberg

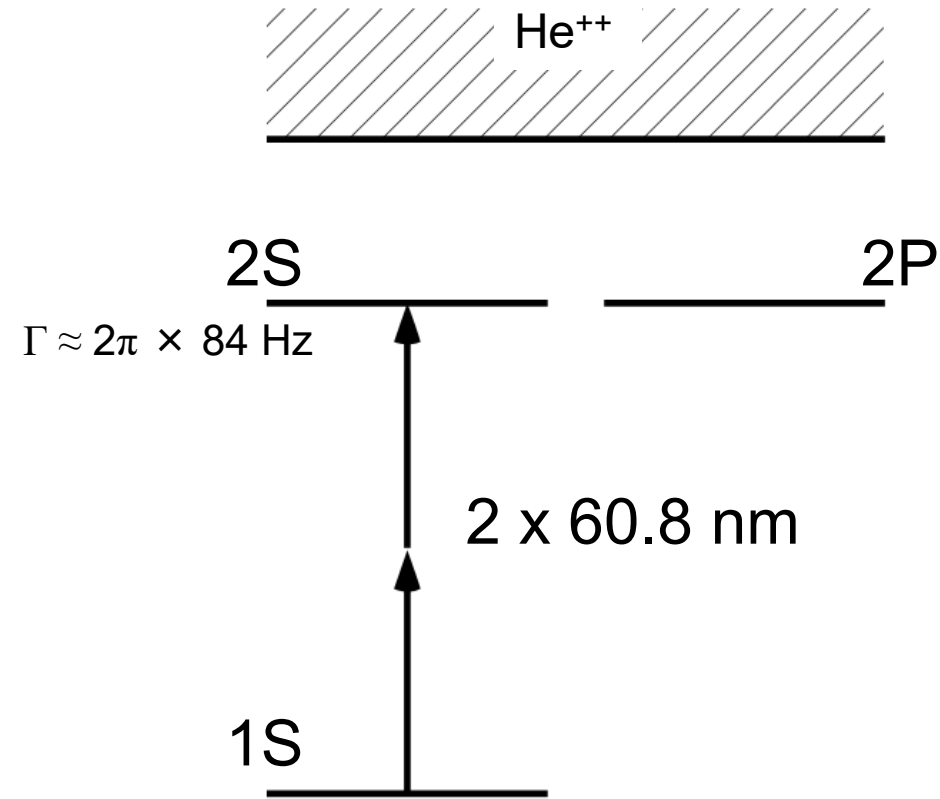
Theodor. W. Hänsch

Thomas Udem

Max Planck Institute of Quantum Optics, Germany



# Spectroscopy of the 1S–2S Transition in He<sup>+</sup>



Difference from Hydrogen spectroscopy:

- Trapped and cooled target → smaller systematics
- QED test for Z=2 system
- Frequency comb spectroscopy in XUV (extreme ultraviolet) wavelength

# QED for He<sup>+</sup>

$$E_{nlj} = R_{\infty} f_{nlj} \left( \alpha, \frac{m_N}{m_e}, \frac{r}{\lambda_C} \right)$$

State energy in SI units (m<sup>-1</sup>)      Rydberg constant      Fine structure constant      Nucleus/electron mass ratio      Normalized nuclear charge radius

Parameters		Contribution to <b>Uncertainty</b> (He <sup>+</sup> 1S2S)
Rydberg constant	$R_{\infty}$	<b>2x10<sup>-12</sup></b> (19 kHz)
Nuclear charge radius	$\frac{r}{\lambda_C}$	<b>6x10<sup>-12</sup></b> (61 kHz)
Nucleus/electron mass	$\frac{m_N}{m_e}$	5x10 <sup>-15</sup> (45 Hz)
Fine structure constant	$\alpha$	2x10 <sup>-14</sup> (166 Hz)

← Hydrogen spectroscopy  
μ-H + H (1s-2s), CODATA2018

← μ-He spectroscopy  
J. Krauth et al. Nature (2021)

← Mass ratio measurements  
in Penning trap

← Atomic recoil (atom interferometer)  
g-2 measurement

**45% larger uncertainty**  
**In Pachucki et al.**  
**arXiv (2023)**

# Uncertainty due to QED theory for He<sup>+</sup> 1S-2S transition

[1] Yerokhin. A and Shabaev V. M , Phys. Rev. A 93, 062514 (2016).

[2] Karshenboim, S. G et al. , Physics Letters B 795, 432–437 (2019)

[3] Karshenboim, S. G et al. , Phys. Rev. A 100, 032515 (2019).

[4] Karshenboim, S. G et al. , Phys. Rev. A 98, 022522 (2018)

[5] V. Yerokhin et al. , Annalen der Physik 531, 1800324 (2019).

[6] A.Czarnecki et al. , Phys. Rev. A 94, 060501 (2016).

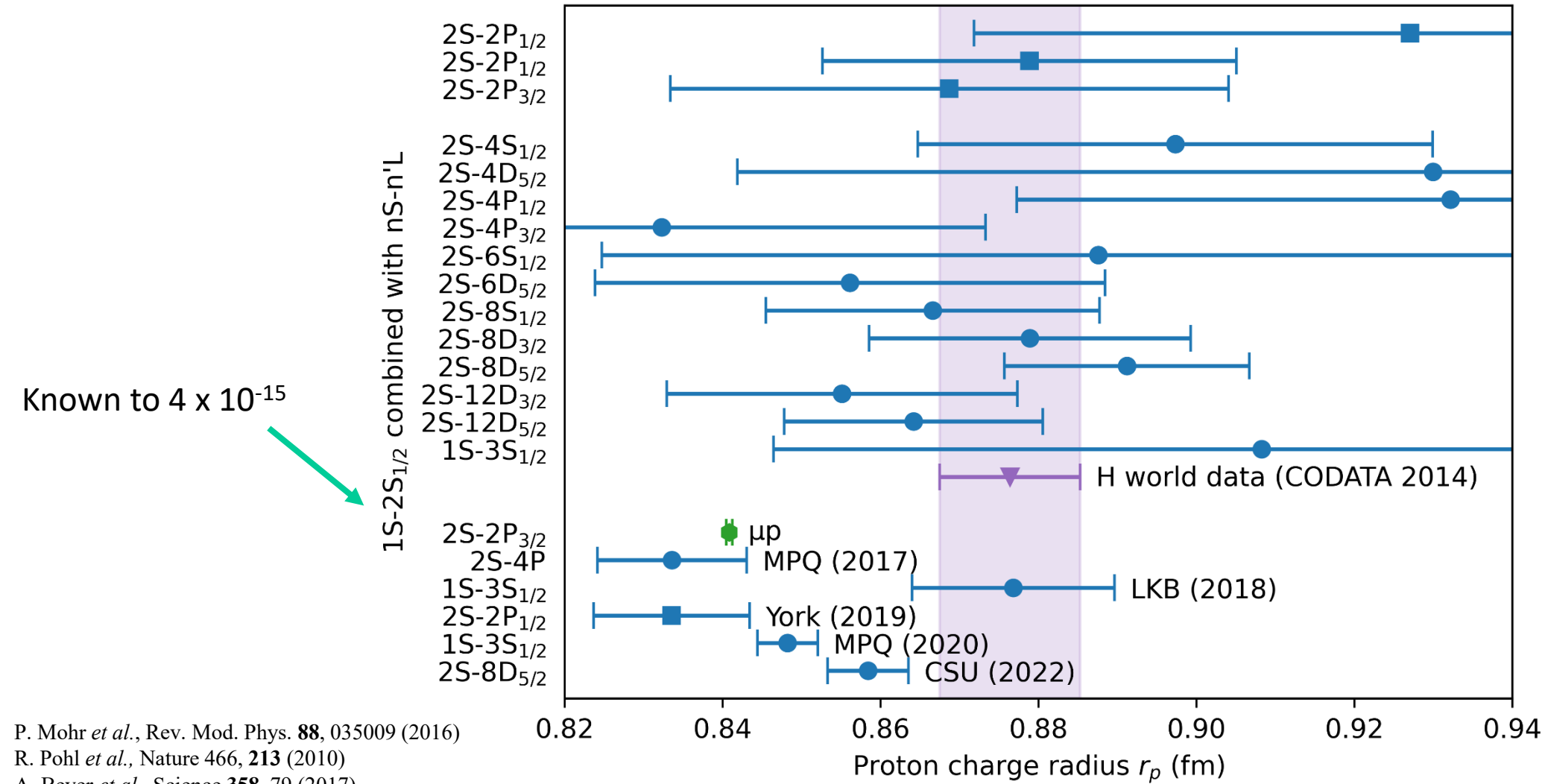
[7] S. Laporta, Physics Letters B 800, 135137 (2020).

[8] Karshenboim, S. G and Shelyuto V. A. , Phys. Rev. A 100, 032513 (2019)

Contribution	Uncertainty (in kHz)	
Relativistic Recoil	0	[1]
Nuclear Polarizability	3	
Self Energy	0	
Vacuum Polarization	1	
Two Photon Corrections	32	[2-6]
Three Photon Corrections	9.5	[2,3]
Four Photon Corrections	0	[7]
Nuclear Size Correction to Self Energy	0	
Nuclear Size Correction to Vacuum Polarization	0	
Radiative Recoil	12	[8]
Nuclear Self Energy	0.6	
<b>Total</b>	<b>~36 kHz</b>	

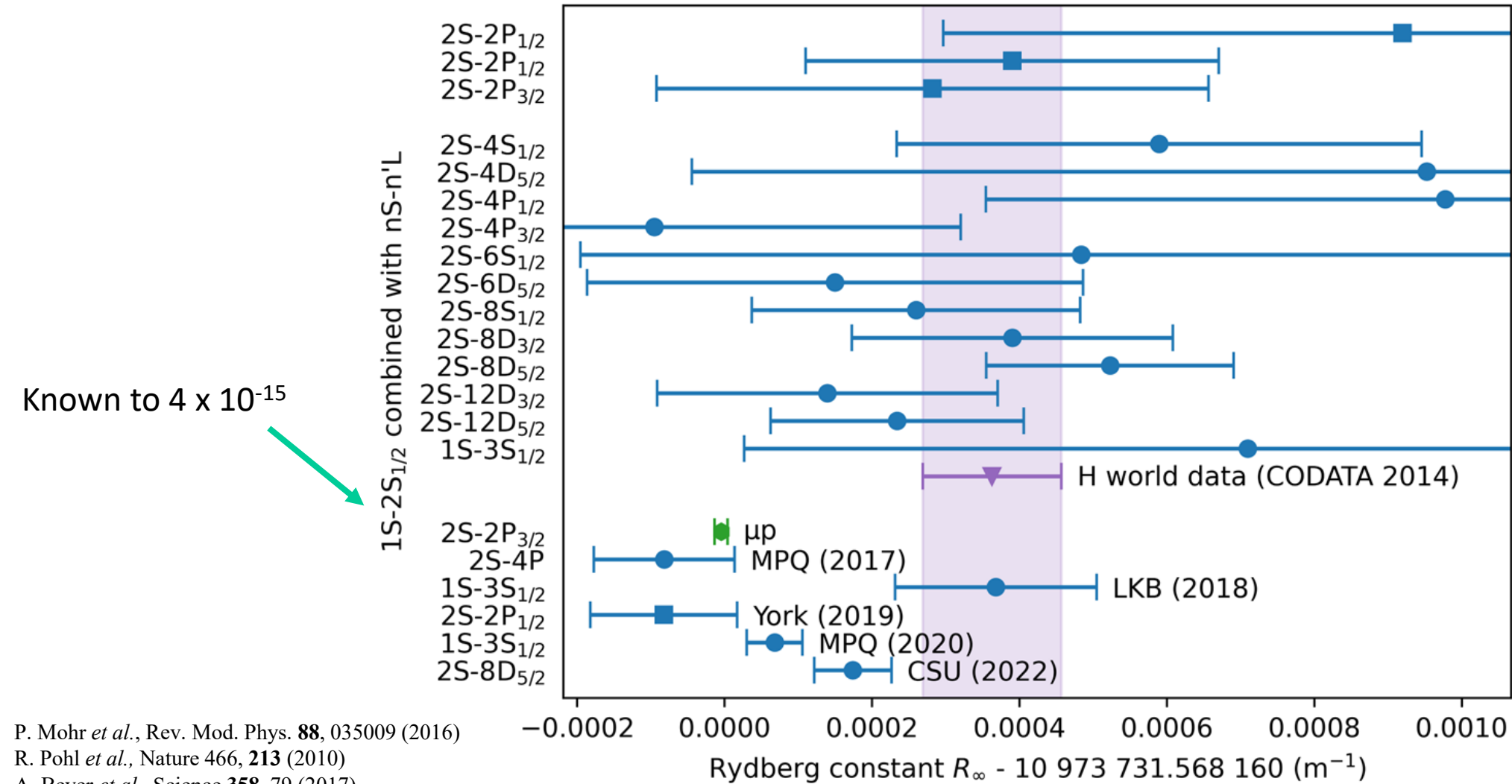
Total QED uncertainty : **36 kHz** ( $4 \times 10^{-12}$ ) (preliminary)

# Proton radius puzzle



P. Mohr *et al.*, Rev. Mod. Phys. **88**, 035009 (2016)  
 R. Pohl *et al.*, Nature **466**, **213** (2010)  
 A. Beyer *et al.*, Science **358**, 79 (2017)  
 H. Fleurbaey *et al.*, Phys. Rev. Lett. **120**, 183001 (2018)  
 N. Bezginov *et al.*, Science **365**, 1007 (2019)  
 A. Grinin *et al.*, Science **370**, 1061 (2020)  
 A. D. Brandt *et al.*, Phys. Rev. Lett. **128**, 023001 (2022)

# Rydberg constant puzzle



P. Mohr *et al.*, Rev. Mod. Phys. **88**, 035009 (2016)  
 R. Pohl *et al.*, Nature **466**, **213** (2010)  
 A. Beyer *et al.*, Science **358**, 79 (2017)  
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# He<sup>+</sup> spectroscopy for testing QED

- Measuring the 1S-2S transition

better than 400kHz ( $4 \times 10^{-11}$ )

—————> Determine  $R_\infty$  and contribute to the proton charge radius puzzle

better than 60 kHz ( $6 \times 10^{-12}$ ) [90 kHz from Pachucki et al. arXiv (2023)]

—————> Determine charge radius, which can be compared with  $\mu$ -He measurement

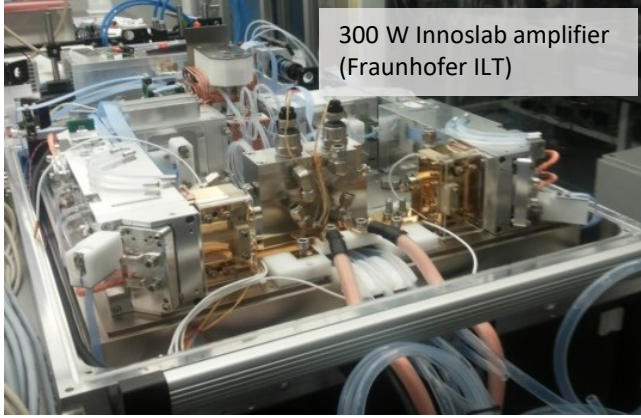
better than 36 kHz ( $4 \times 10^{-12}$ )

—————> QED theory uncertainty will be a limitation

- Measuring other transitions in  $^4\text{He}^+$  —————> QED test more independent from  $\mu$ -He and Hydrogen
- Measuring  $^3\text{He}^+$  —————> Charge radii difference, which can be compared with neutral He spectroscopy

# He<sup>+</sup> spectroscopy setup: overview

High-power IR frequency comb  
Yb:KYW laser + amplifiers  
@1030 nm

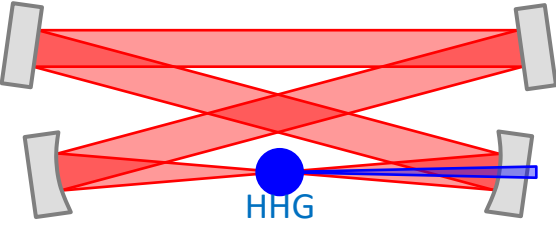


300 W Innoslab amplifier  
(Fraunhofer ILT)



Frequency comb at 60.8 nm

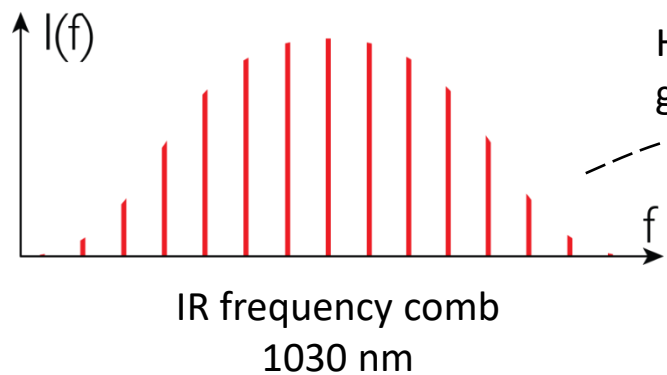
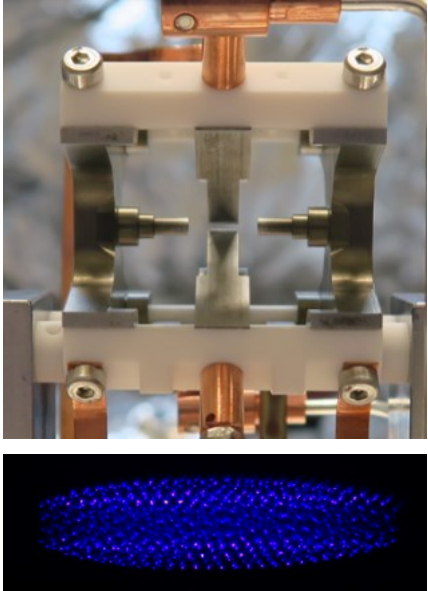
Intracavity high-harmonic generation  
17<sup>th</sup> harmonic



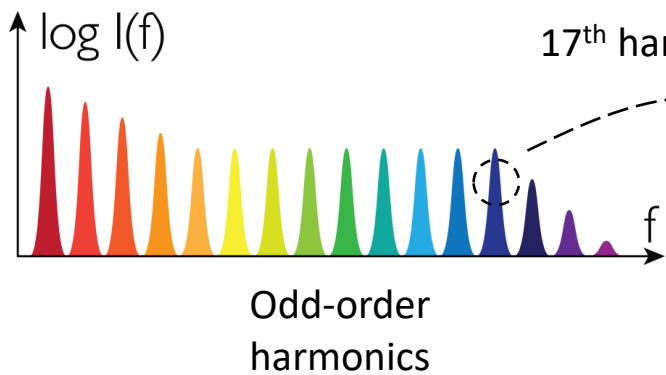
HHG



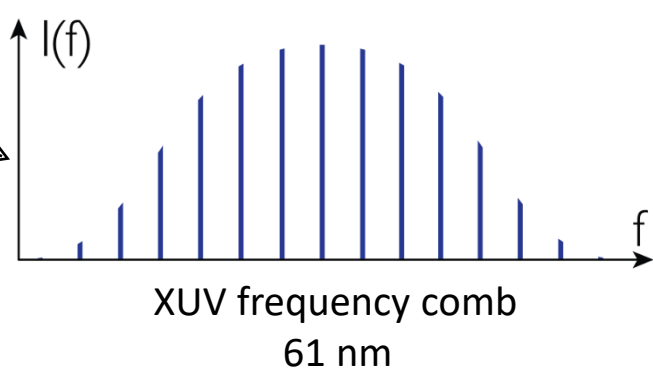
Trapped He<sup>+</sup> ions



High-harmonic generation



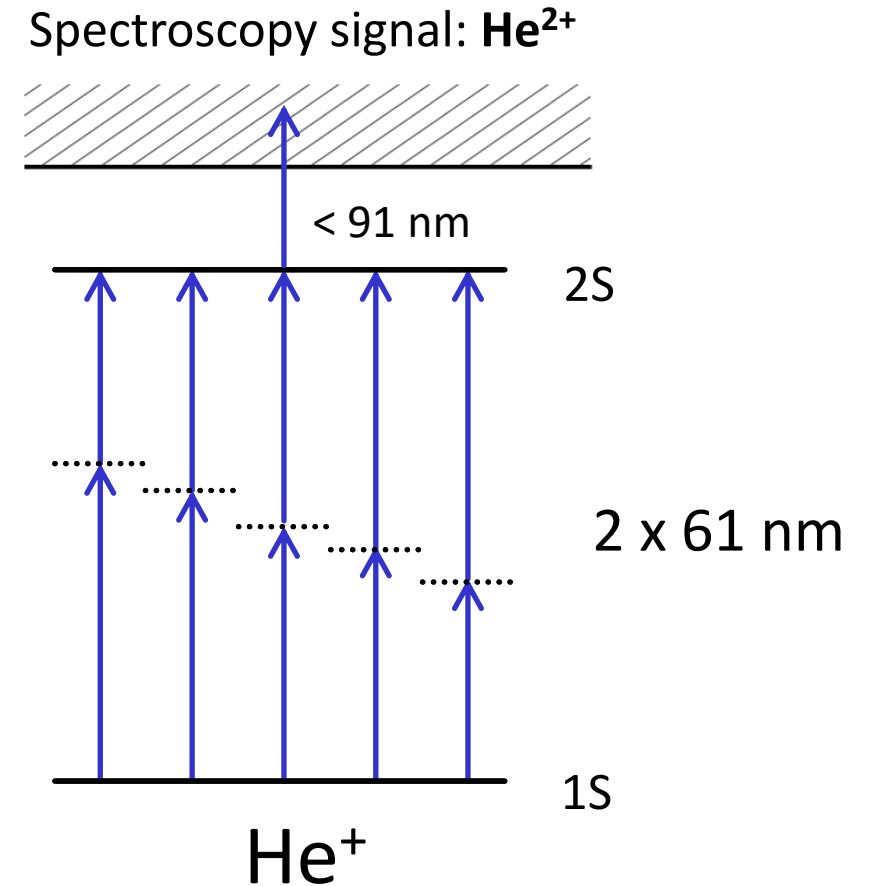
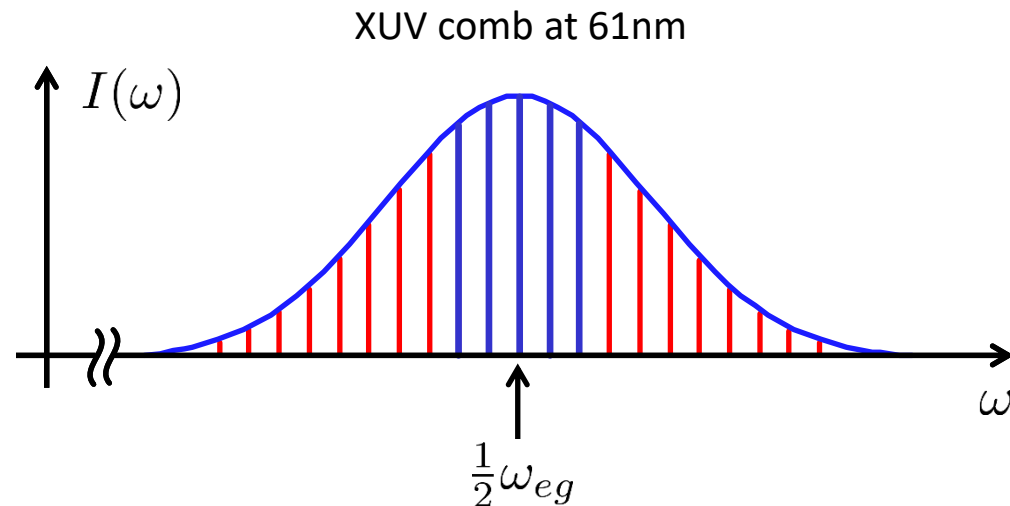
17<sup>th</sup> harmonic





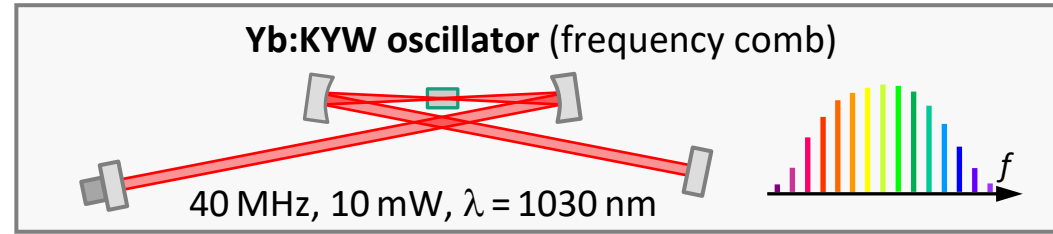
# Direct frequency comb spectroscopy

- Line width of a single laser mode
- Efficient nonlinear frequency conversion due to high peak power of pulsed laser
- As efficient as CW laser of same average power

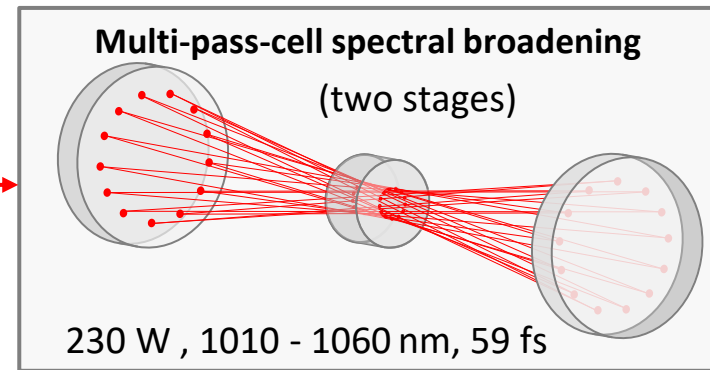
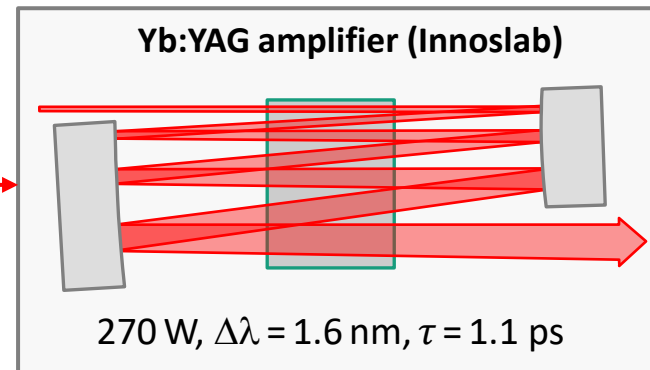
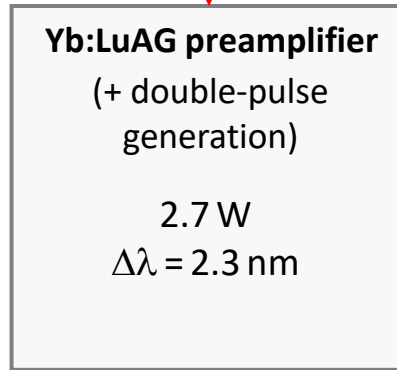


# 61 nm laser system

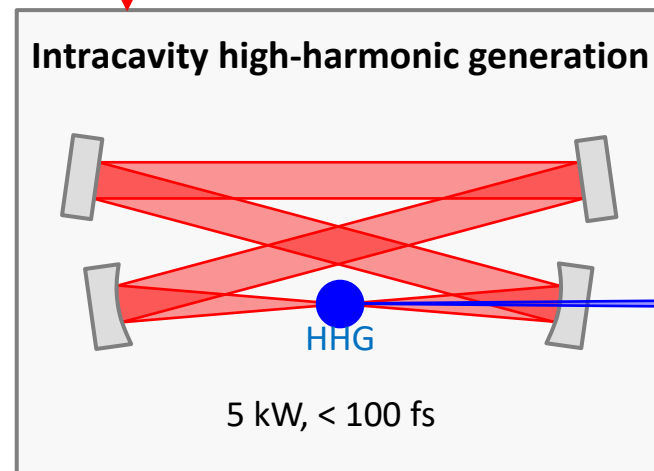
Seed laser



Amplification  
&  
compression



XUV comb  
generation



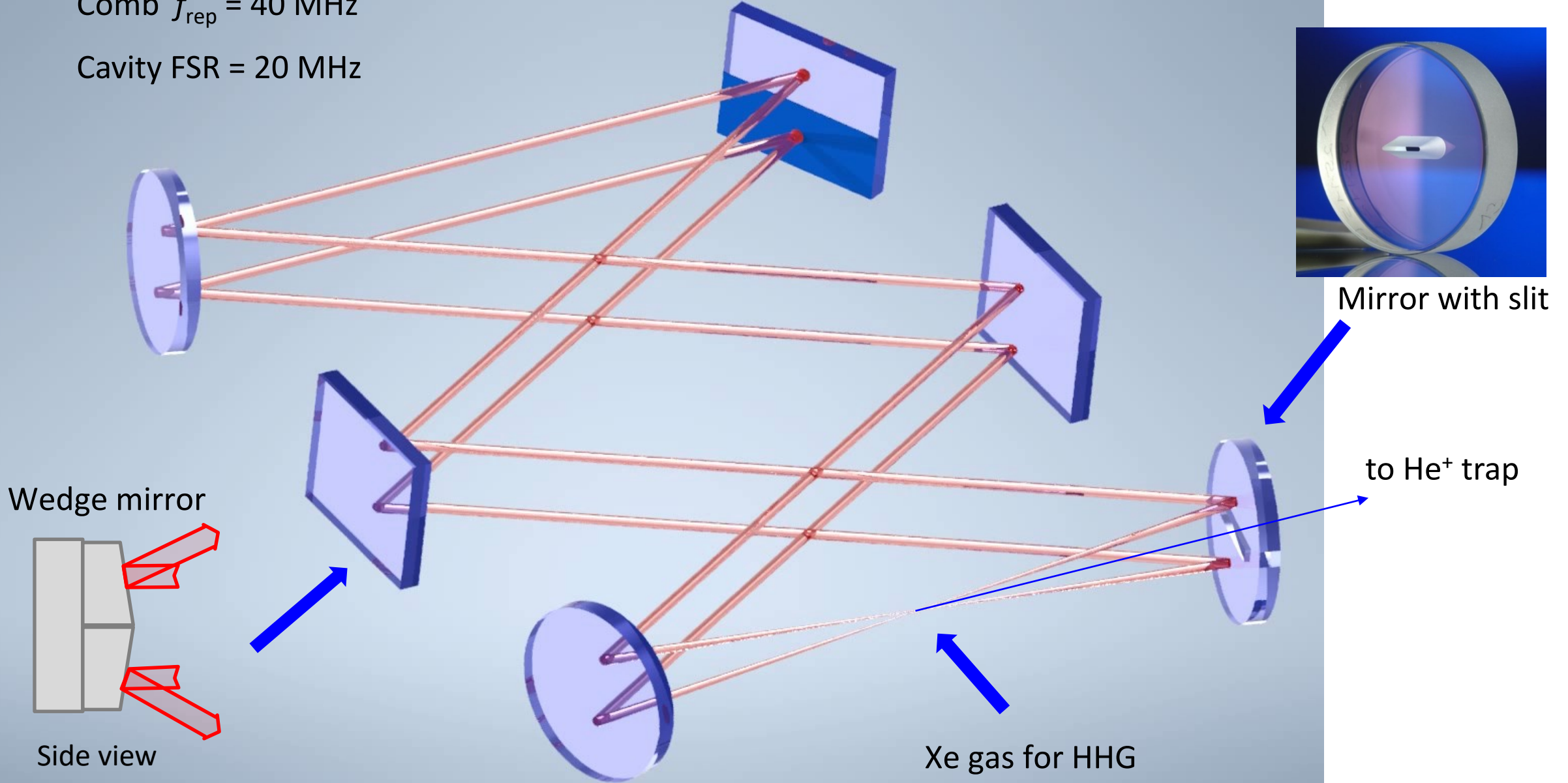
XUV comb

to He<sup>+</sup> trap

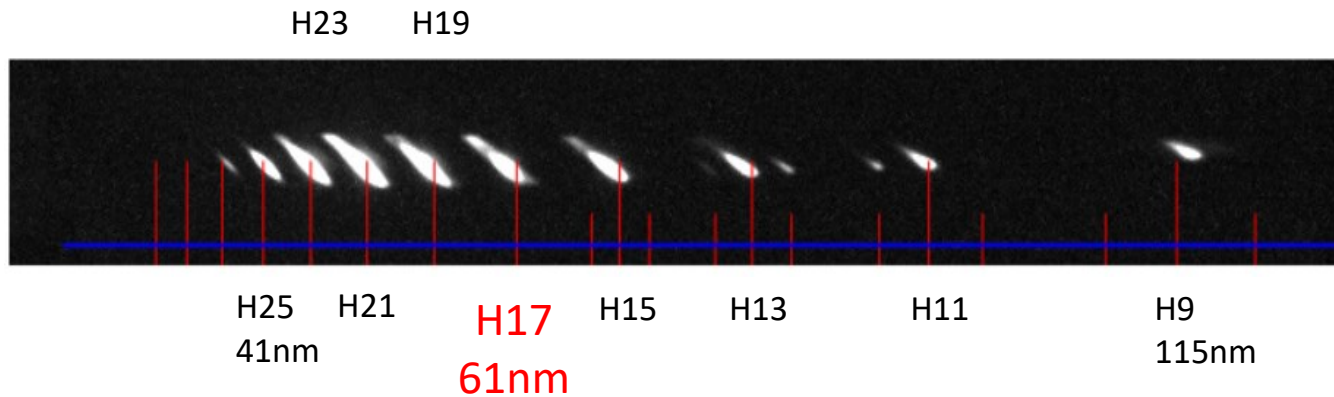
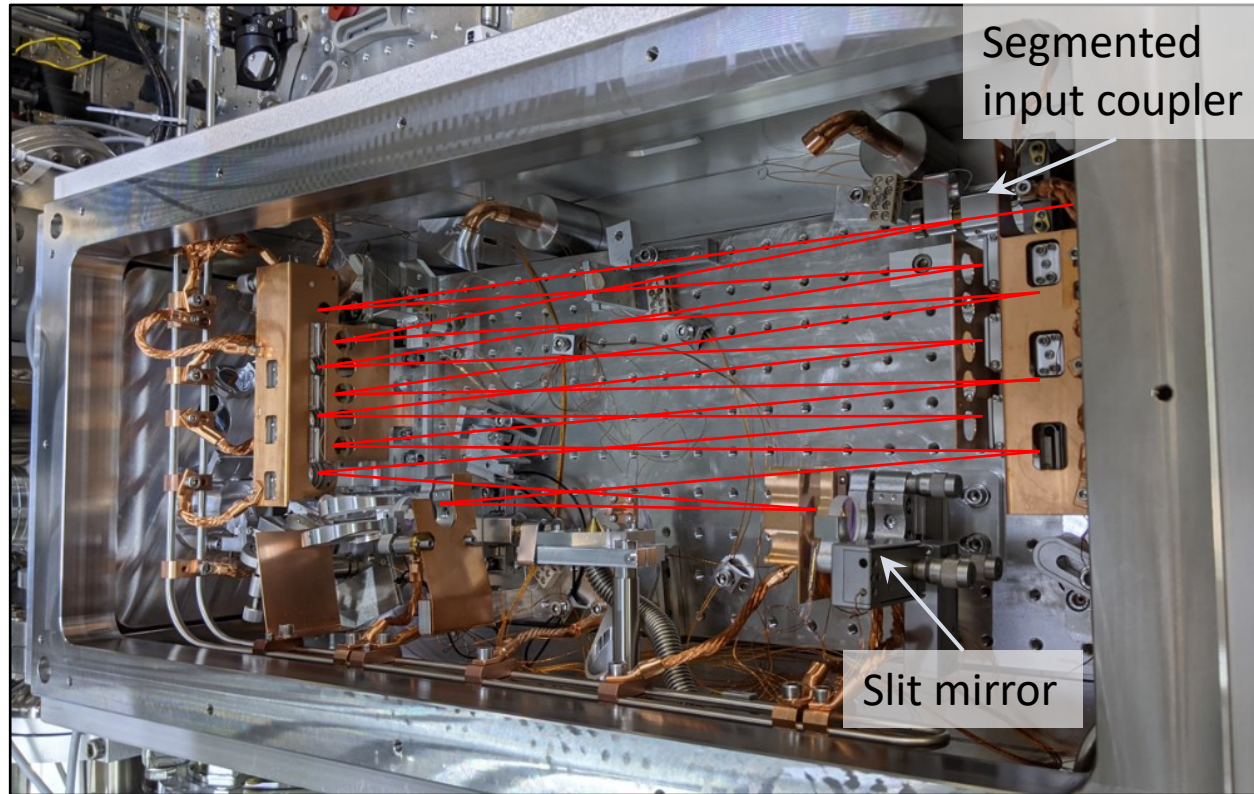
# Enhancement Resonator for HHG

Comb  $f_{\text{rep}} = 40 \text{ MHz}$

Cavity FSR = 20 MHz



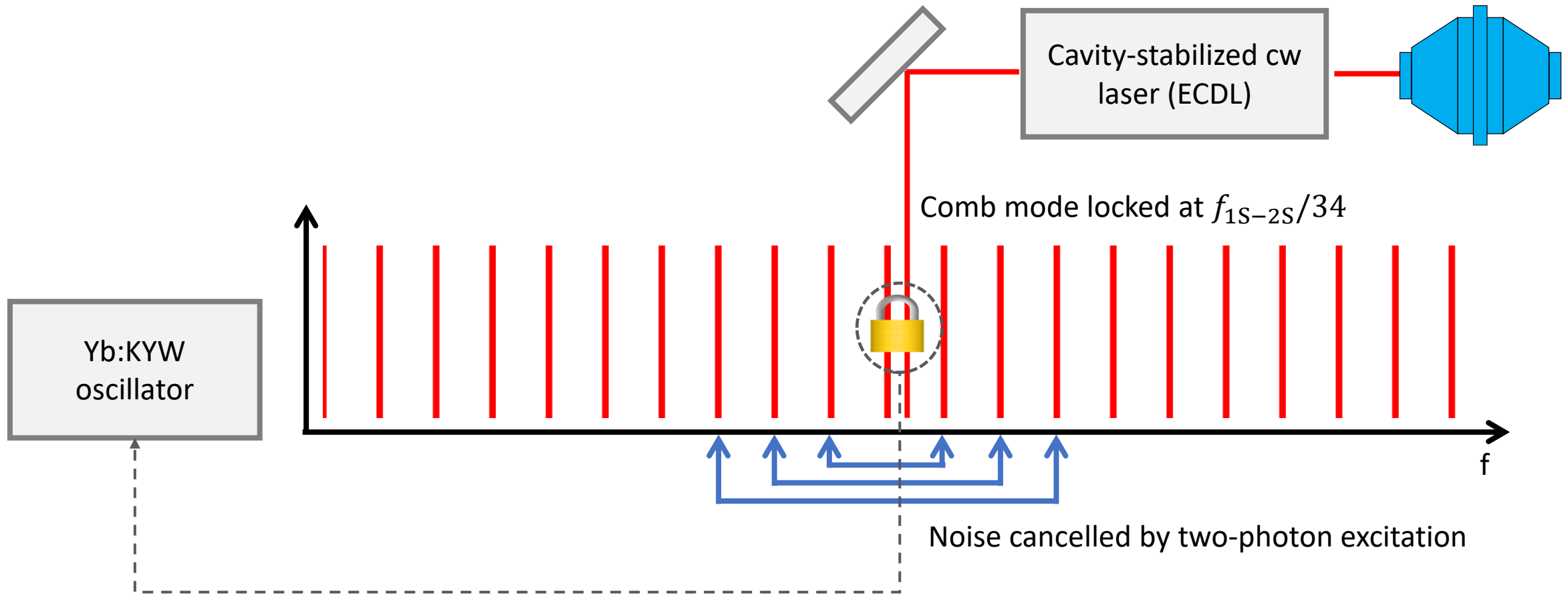
# Enhancement Resonator for HHG



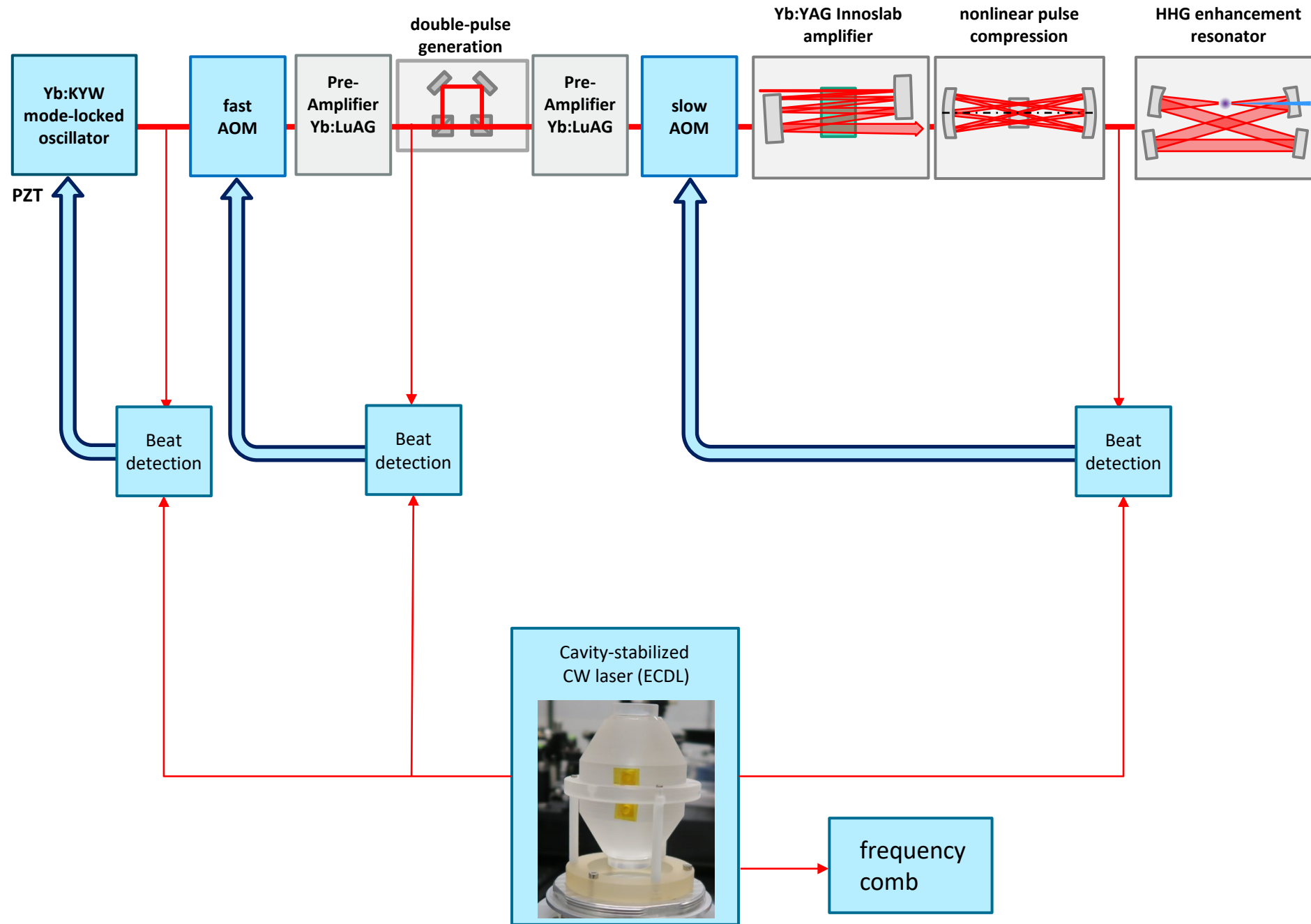
$\sim 30 \mu\text{W}$  at 60.8 nm (preliminary)

$\longrightarrow \sim 0.1 \text{ Hz}$  signal rate (ionization)

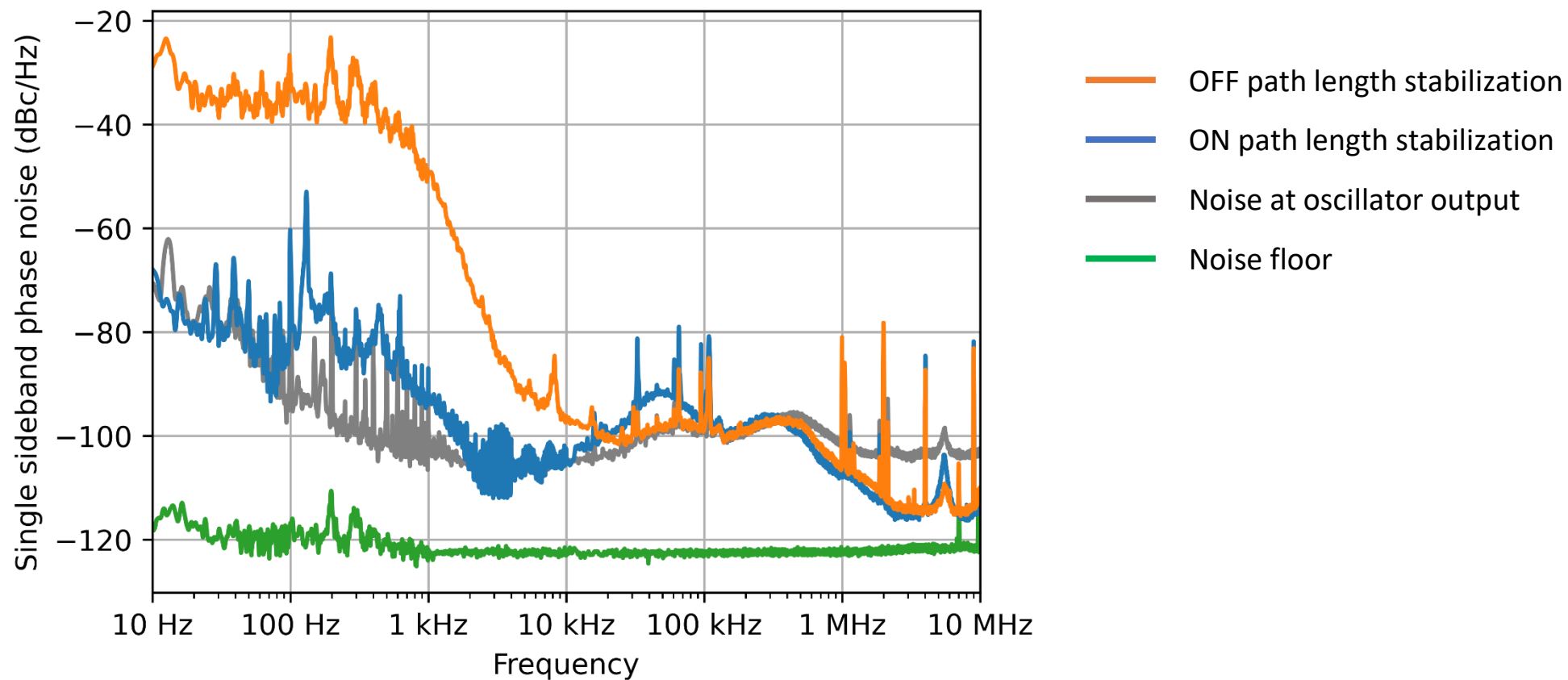
# Comb stabilization



# Stabilization of frequency comb



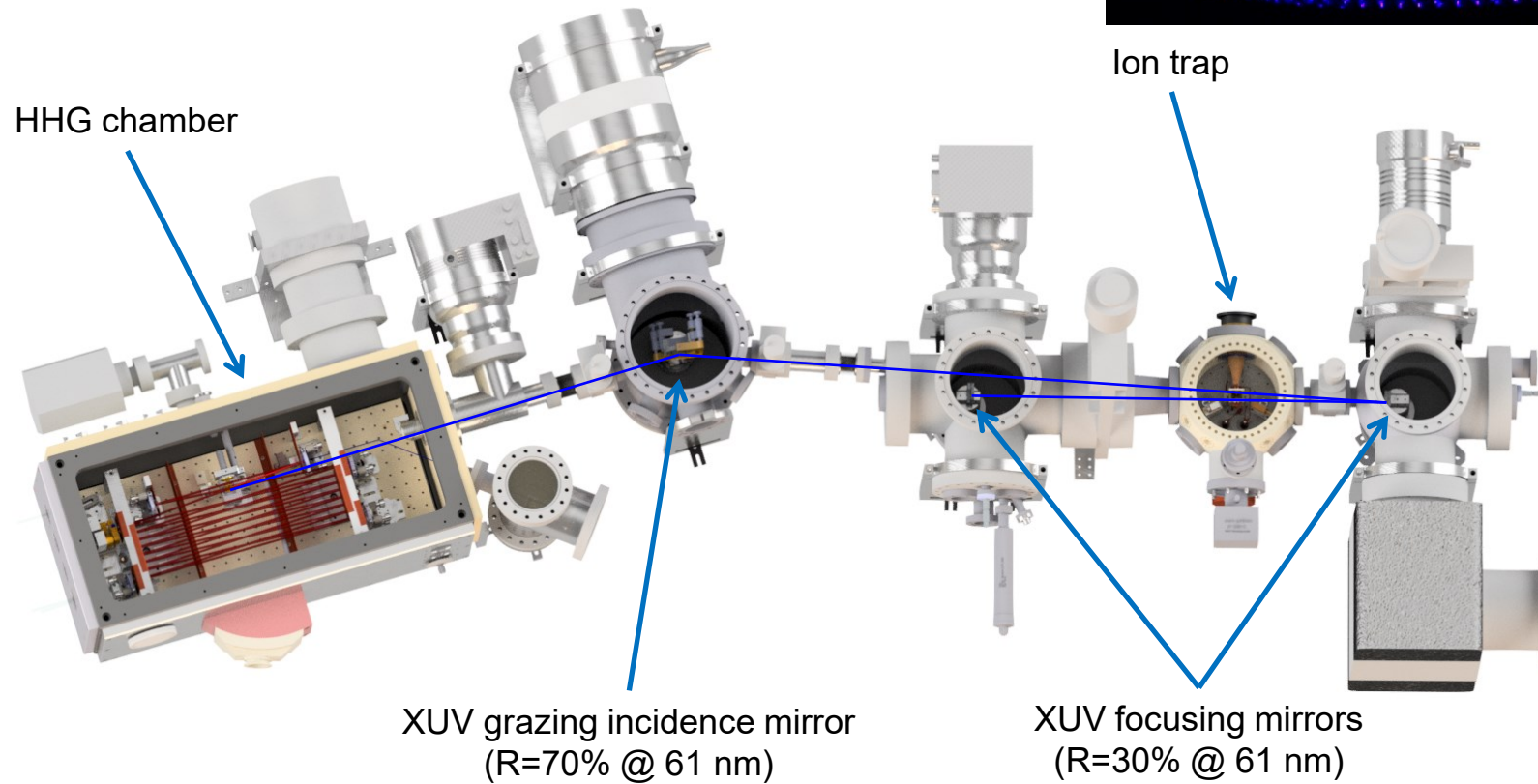
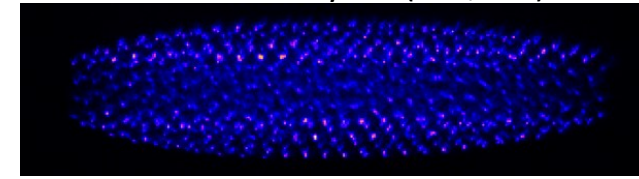
# Stabilization of frequency comb



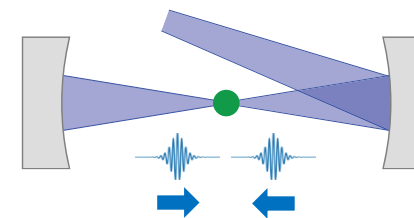
- 80% of power in carrier at XUV
- Less than 20% of signal loss due to phase noise

# XUV beam delivery to trapped He<sup>+</sup>

Sympathetically cooled He<sup>+</sup>  
in mixed ion crystal (He<sup>+</sup>/Be<sup>+</sup>)

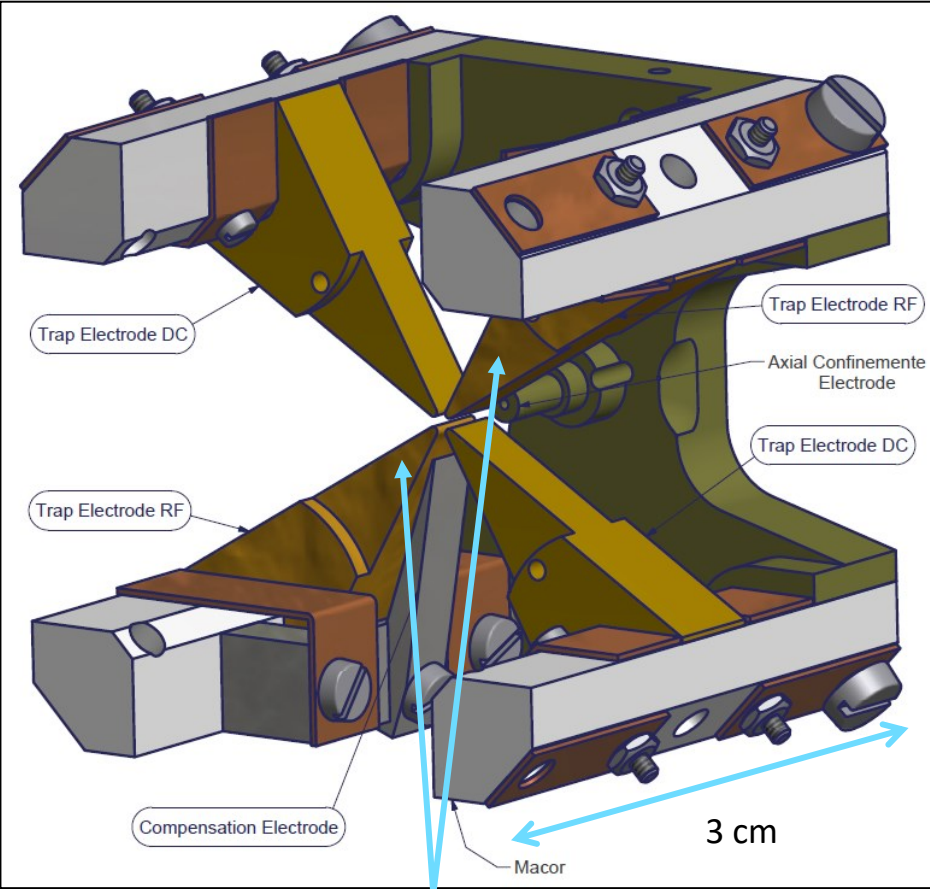


Doppler-free  
Anti-collinear excitation

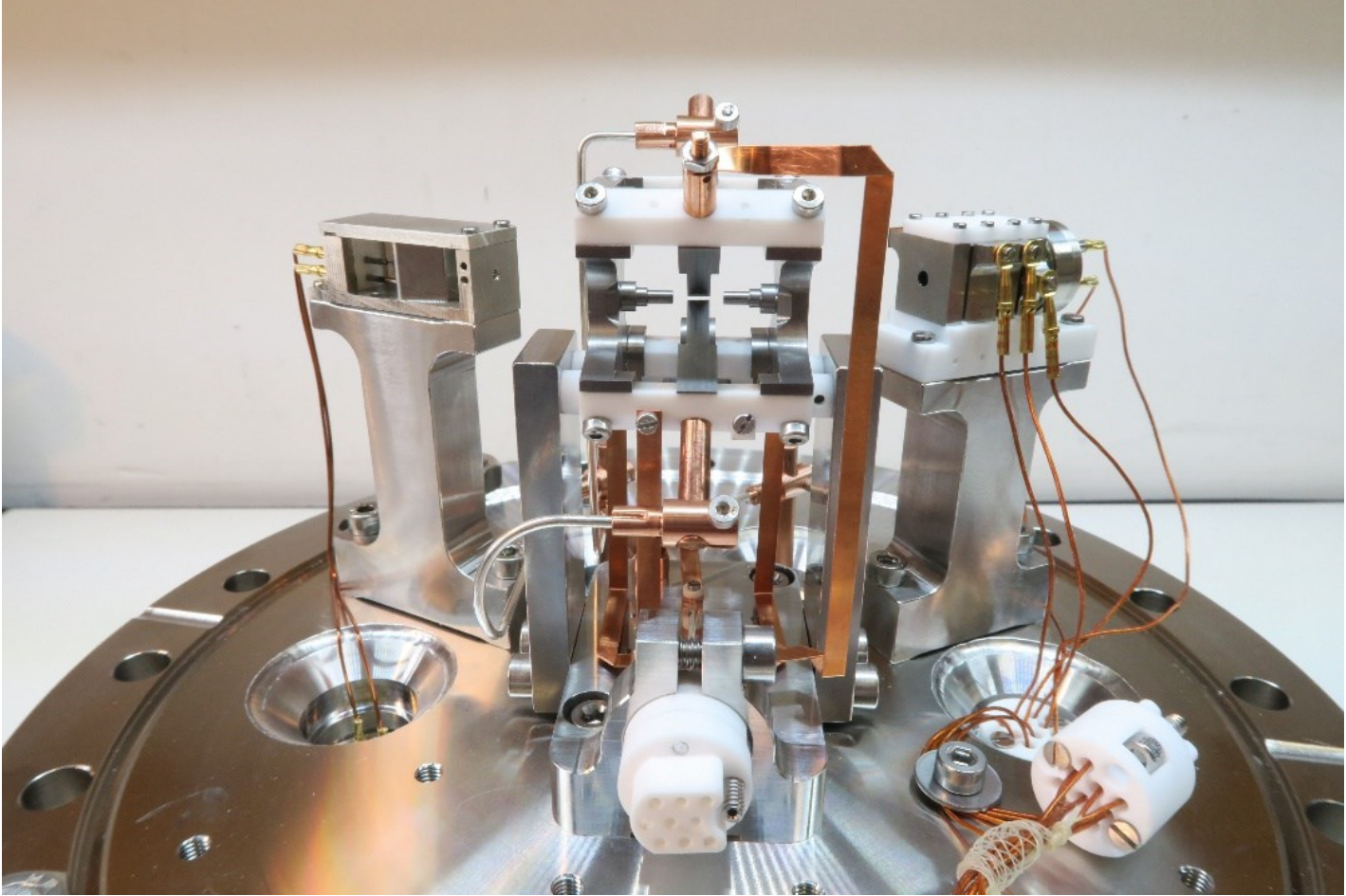




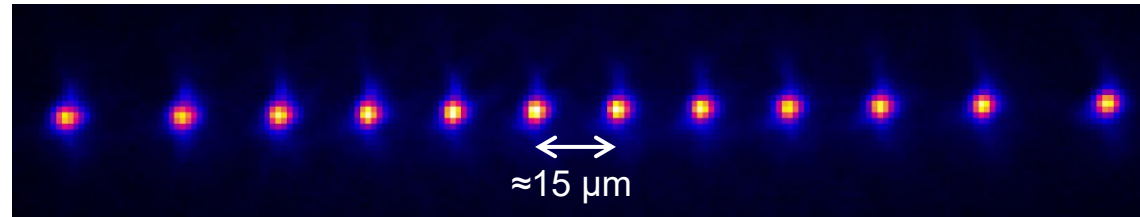
# Be<sup>+</sup>/He<sup>+</sup> ion trap



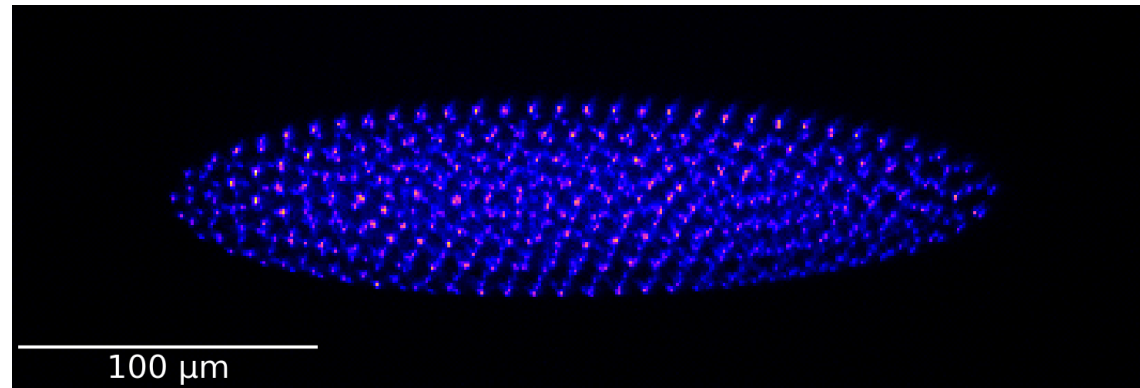
RF electrodes



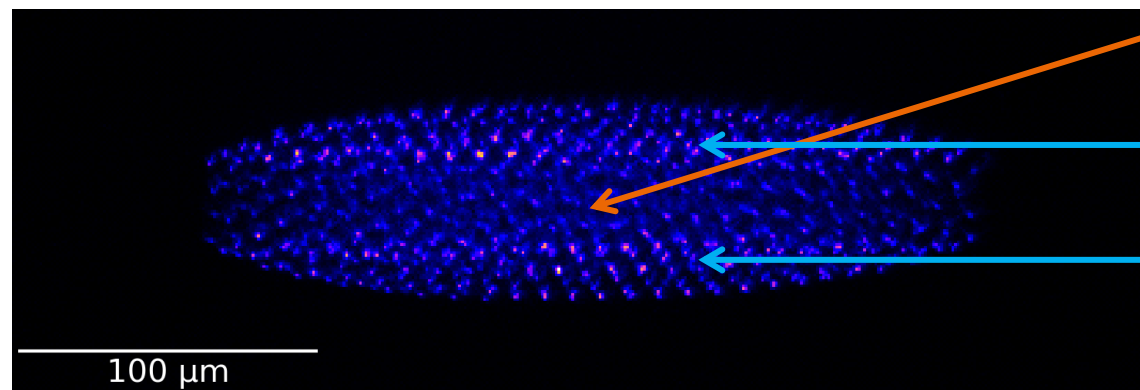
# Ion crystals and sympathetic cooling



Be<sup>+</sup> laser cooled to a few mK



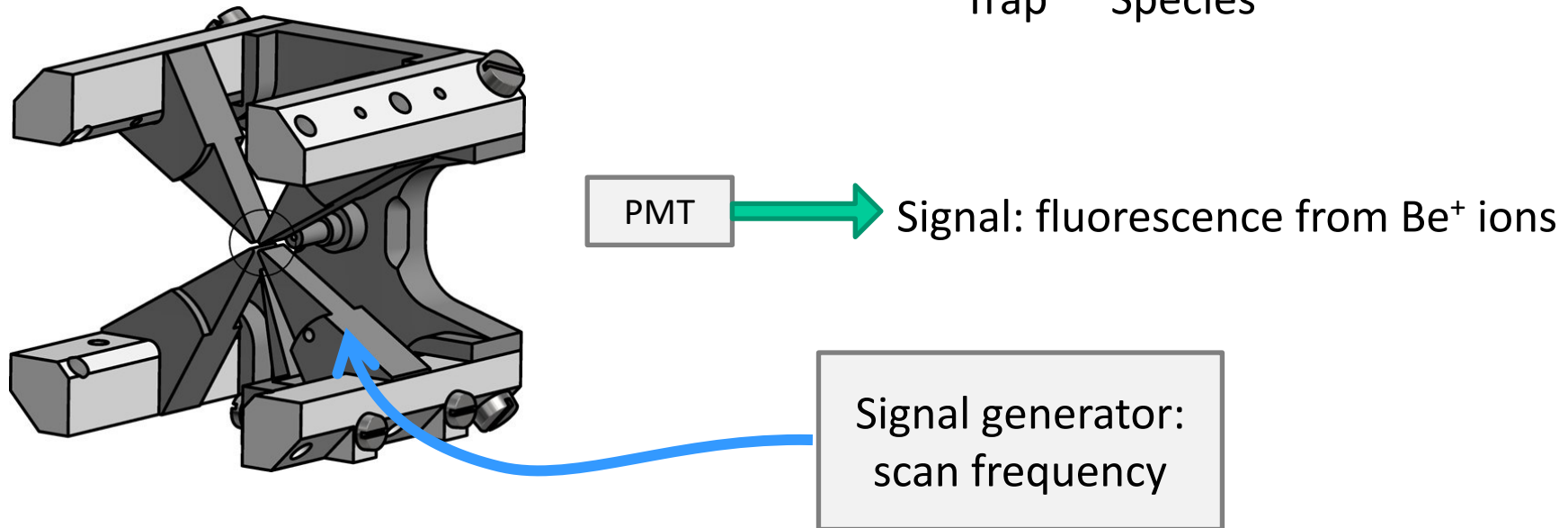
He<sup>+</sup> sympathetically cooled



# Spectroscopy signal: Secular excitation detection

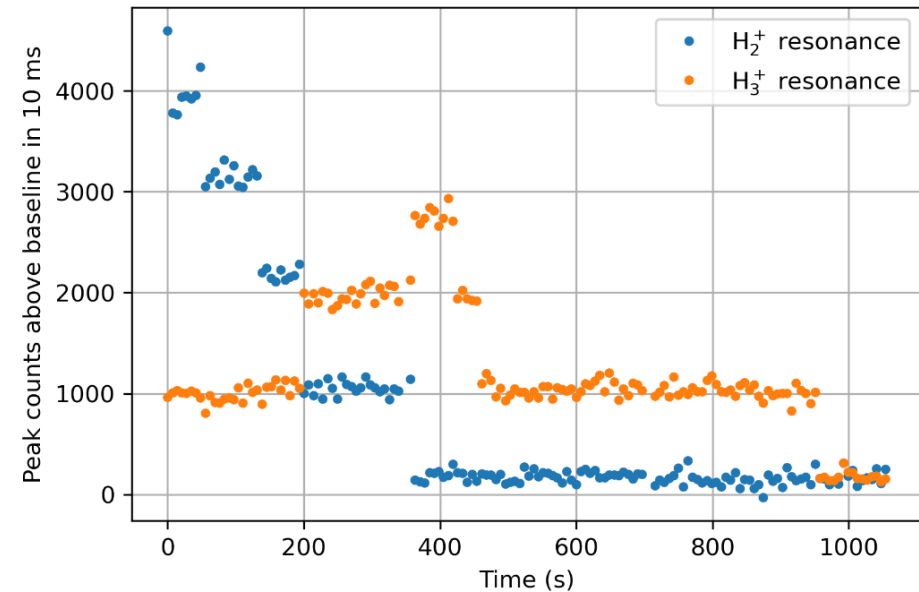
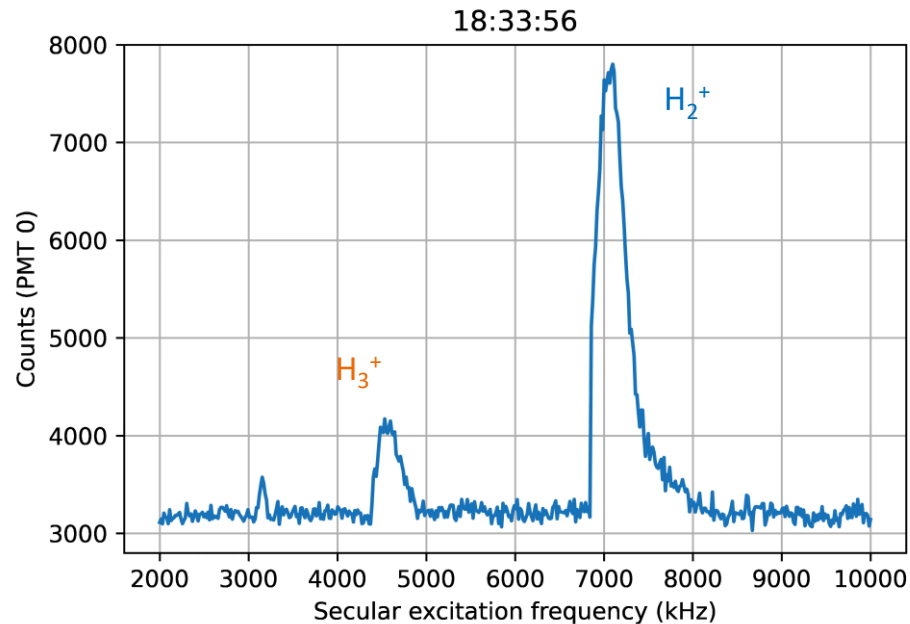
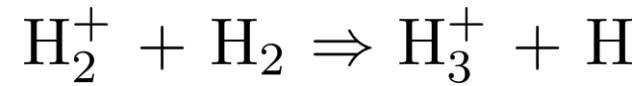
Motional resonance:  $\omega_{\text{sec}} \approx \frac{U_0}{\sqrt{2}\Omega r_0^2} \frac{Q}{m}$

↑                      ↑  
Trap                      Species



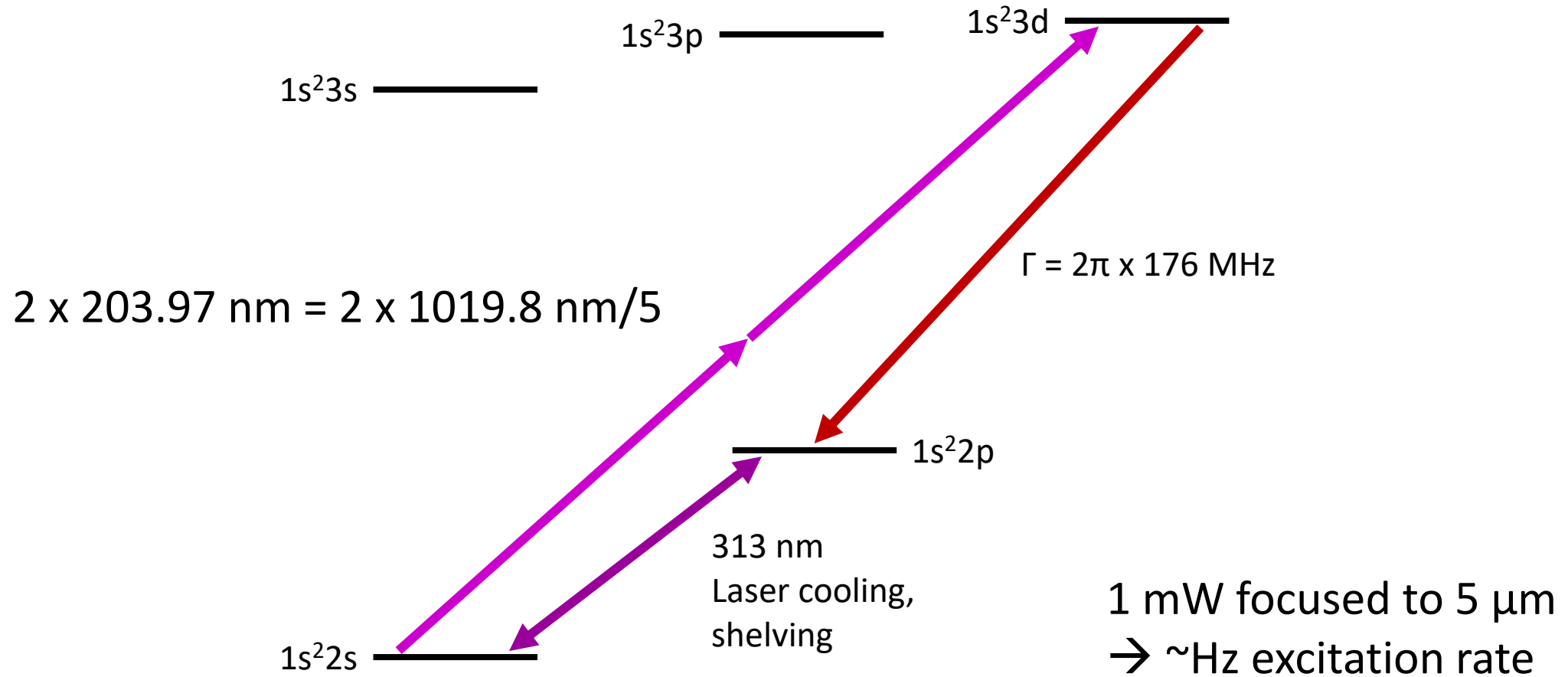
# Testing secular excitation detection

$\text{H}_2^+$ : Same charge-to-mass ratio as  $\text{He}^{2+}$

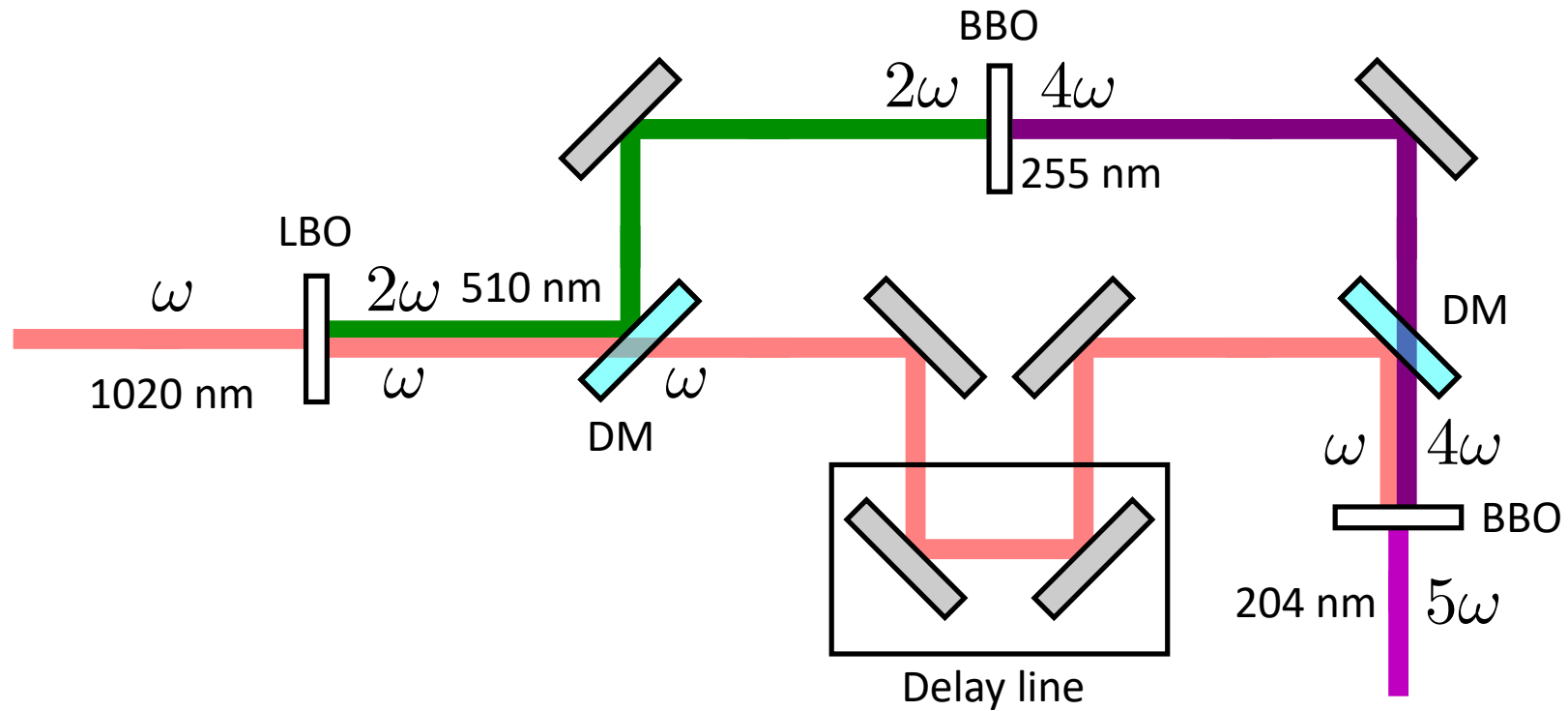


➡ Single event sensitive detection

# Driving two-photon transition in $\text{Be}^+$



# 5<sup>th</sup> harmonic generation in crystals



## Achieved:

- Generation of 61nm comb
- Trapped and cooled He<sup>+</sup>
- Demonstrated sensitive He<sup>2+</sup> detection

## Plans :

- Optimization of 61nm comb  
(power, spectrum)
- Testing spectroscopy setup with easier transition  
(Two-photon transition at 204 nm with Be<sup>+</sup>)
- Finding He<sup>+</sup> 1S-2S signal:  
QED prediction: ~ 70 kHz  
Expected linewidth of signal: ~ 1 kHz

# The He<sup>+</sup> team



Jorge  
Moreno



Fabian  
Schmid



Akira  
Ozawa



Johannes  
Weitenberg



Theodor  
W. Hänsch



Thomas  
Udem

Thank you for your attention!



