

# R-Value Measurement at BESIII

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and the Structure of the Nucleon

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# Definition of R-Value

Ratio of leading-order cross sections of hadron and muon pair production in  $e^+e^-$  annihilation

$$R \equiv \frac{\sigma^0(e^+e^- \rightarrow \text{hadrons})}{\sigma^0(e^+e^- \rightarrow \mu^+\mu^-)} \equiv \frac{\sigma_{\text{had}}^0}{\sigma_{\mu\mu}^0}$$

With  $\sigma_{\mu\mu}^0$  directly from QED:  $\sigma_{\mu\mu}^0 = \frac{4\pi\alpha}{3s} \frac{\beta_\mu(3 - \beta_\mu^2)}{2}$ , with  $\beta_\mu = \sqrt{1 - \frac{4m_\mu^2}{s}}$

**Important input to current tests of Standard Model**

# Running of the Fine Structure Constant $\Delta\alpha_{\text{em}}$

$\alpha(m_Z^2)$  one of three essential observables for electroweak precision physics

$$\Delta\alpha = 1 - \frac{\alpha(0)}{\alpha(s)} = \Delta\alpha_{\text{lepton}}(s) + \Delta\alpha_{\text{had}}^{(5)}(s) + \Delta\alpha_{\text{top}}(s)$$

From perturbation theory

top quark contribution

Hadronic Vacuum Polarization contribution

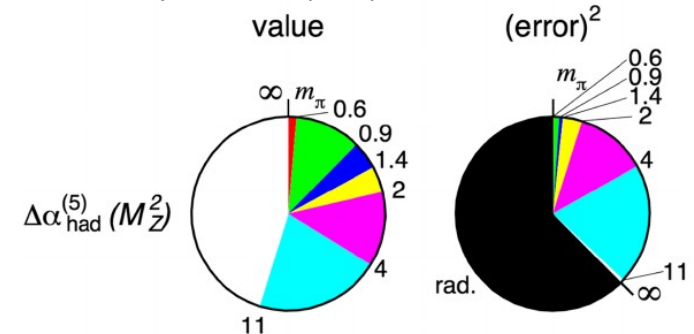
$$\Delta\alpha_{\text{had}}^{(5)}(s) = -\frac{\alpha s}{3\pi} P \int_{s_{th}}^{\infty} ds' \frac{R(s')}{s'(s' - s)}$$

R-Value over wide energy range important input:

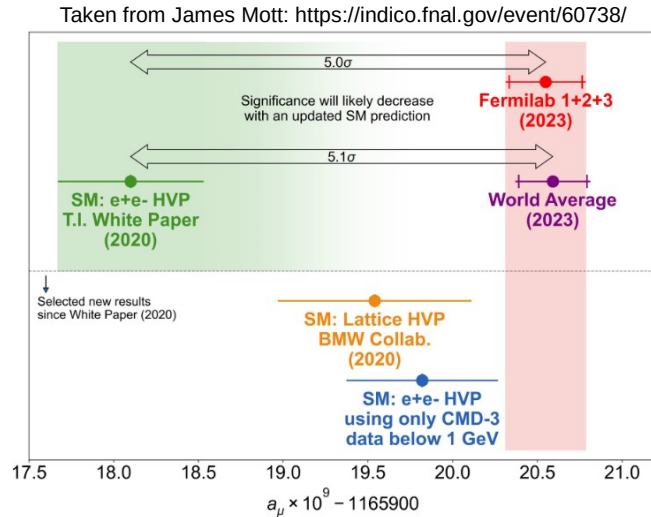
Source	Contribution( $\times 10^{-4}$ )
$\Delta\alpha_{\text{lepton}}(M_Z^2)$	$314.979 \pm 0.002$
$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$	$276.0 \pm 1.0$
$\Delta\alpha_{\text{top}}(M_Z^2)$	$-0.7180 \pm 0.0054$

Eur.Phys.J. 80 (2020) 241

Phys.Rev.D97 (2019) 114025

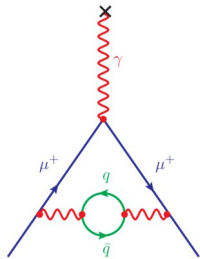


# Anomalous Magnetic Moment of the Muon



Muon anomaly  $a_\mu = \frac{g_\mu - 2}{2}$

- Accuracy better than 0.5 ppm in experiment and theory
  - Exp:  $116\,592\,059(22) \times 10^{-11}$  (arXiv:2308.06230)
  - SM:  $116\,591\,810(43) \times 10^{-11}$  (Physics Reports 887 (2020) 1–16)
- Discrepancy between SM prediction and experiment
- Hadronic contributions dominate uncertainty of  $a_\mu^{\text{SM}}$



Hadronic Vacuum Polarization contribution:

- Dispersion integral
- R-Value as experimental input

$$a_\mu^{\text{HVP}} = \left( \frac{\alpha m_\mu}{3\pi} \right)^2 \int_{2m_\pi}^{\infty} ds \frac{R(s)K(s)}{s^2}$$

- Tensions with latest Lattice QCD calculations and cross section measurements

# Beijing $e^+e^-$ Collider – BEPCII



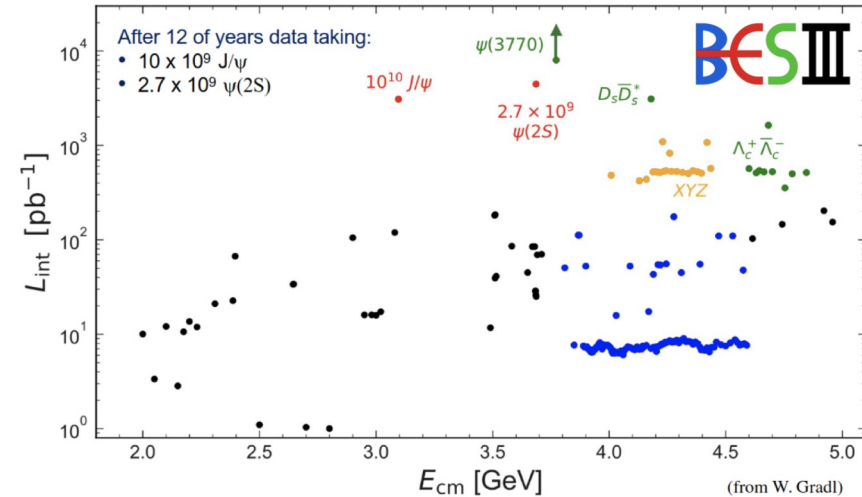
- Center-of-mass energies from 2 – 5 GeV
- Design luminosity exceeded:  $1.1 \times 10^{33} \text{cm}^{-2}\text{s}^{-1}$  at 3.77 GeV

World's largest  $e^+e^-$  data sets at  $\tau$ -charm energies

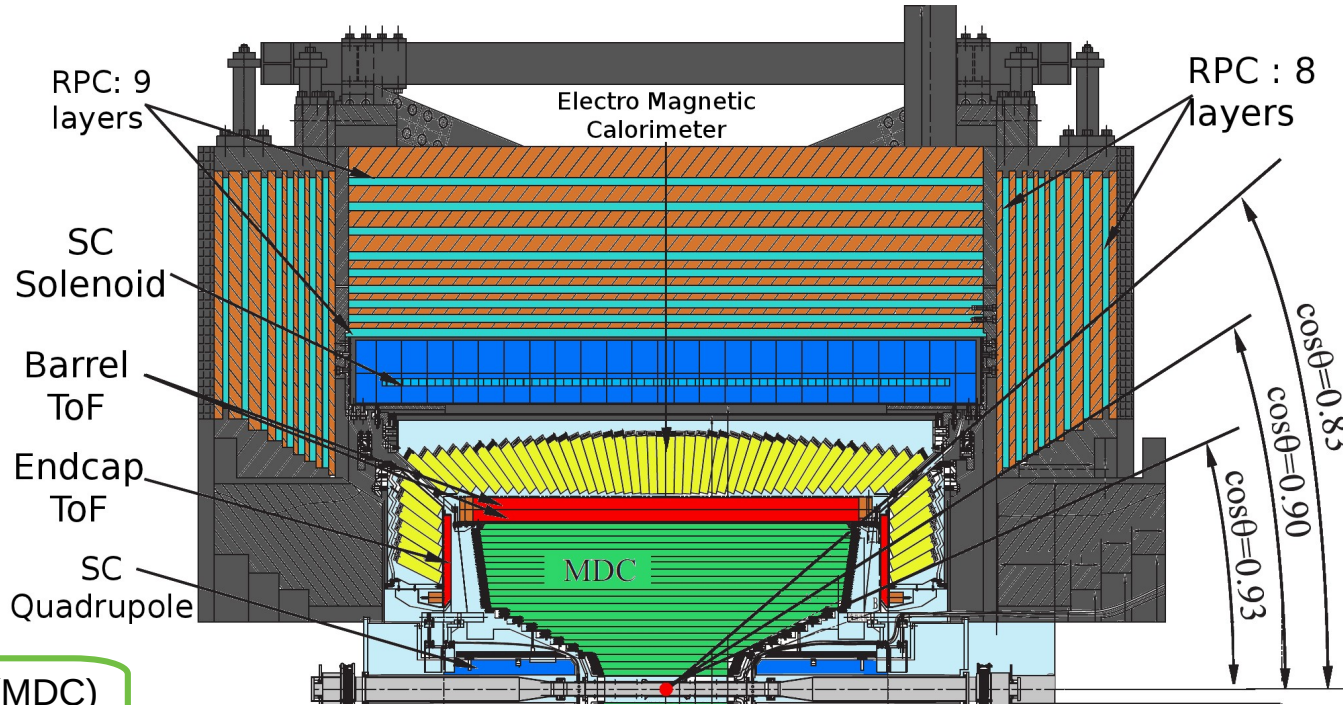
- $10^{10} J/\psi$  and  $2.7 \times 10^9 \psi(2S)$  directly produced
- More than  $40 \text{ fb}^{-1}$  collected between 3.773 and 5 GeV
- Currently collecting  $20 \text{ fb}^{-1}$  at 3.773 GeV

This work:

- 14 R scan data points ( $\sim 110 \text{ pb}^{-1}$ )
- 2.23 GeV – 3.67 GeV



# Beijing Spectrometer – BESIII



## Drift Chamber (MDC)

- $\sigma(p)/p = 0.5\%$
- $\sigma_{dE/dx} = 6.0\%$

## Time-of-flight system (TOF)

- $\sigma(t) = 60\text{ps}$

## Superconducting Magnet

- 1 T magnetic field

## EM Calorimeter (EMC)

- 6240 CsI(Tl) crystals
- $\sigma(E)/E = 2.5\%$
- $\sigma_{Z,\phi}(E) = 0.5 - 0.7 \text{ cm}$

## Muon Chambers

- 8 – 9 layers of RPC
- $p > 400 \text{ MeV}/c$
- $\delta R\Phi = 1.4 \sim 1.7 \text{ cm}$

# Determination of R-Value

Leading-order QED cross section

$$e^+e^- \rightarrow \mu^+\mu^-$$

Residual background contributions

- MC simulations
- Beam related contributions from data

$$R = \frac{1}{\sigma_{\mu\mu}^0} \cdot \frac{N_{\text{had}}^{\text{obs}} - N_{\text{bkg}}}{\mathcal{L} \cdot \epsilon_{\text{trig}} \cdot \epsilon_{\text{had}} \cdot (1 + \delta)}$$

Integrated luminosity

- Determined from LA-Bhabha scattering
- 0.8% uncertainty

Trigger efficiency  
for hadronic events ~100%

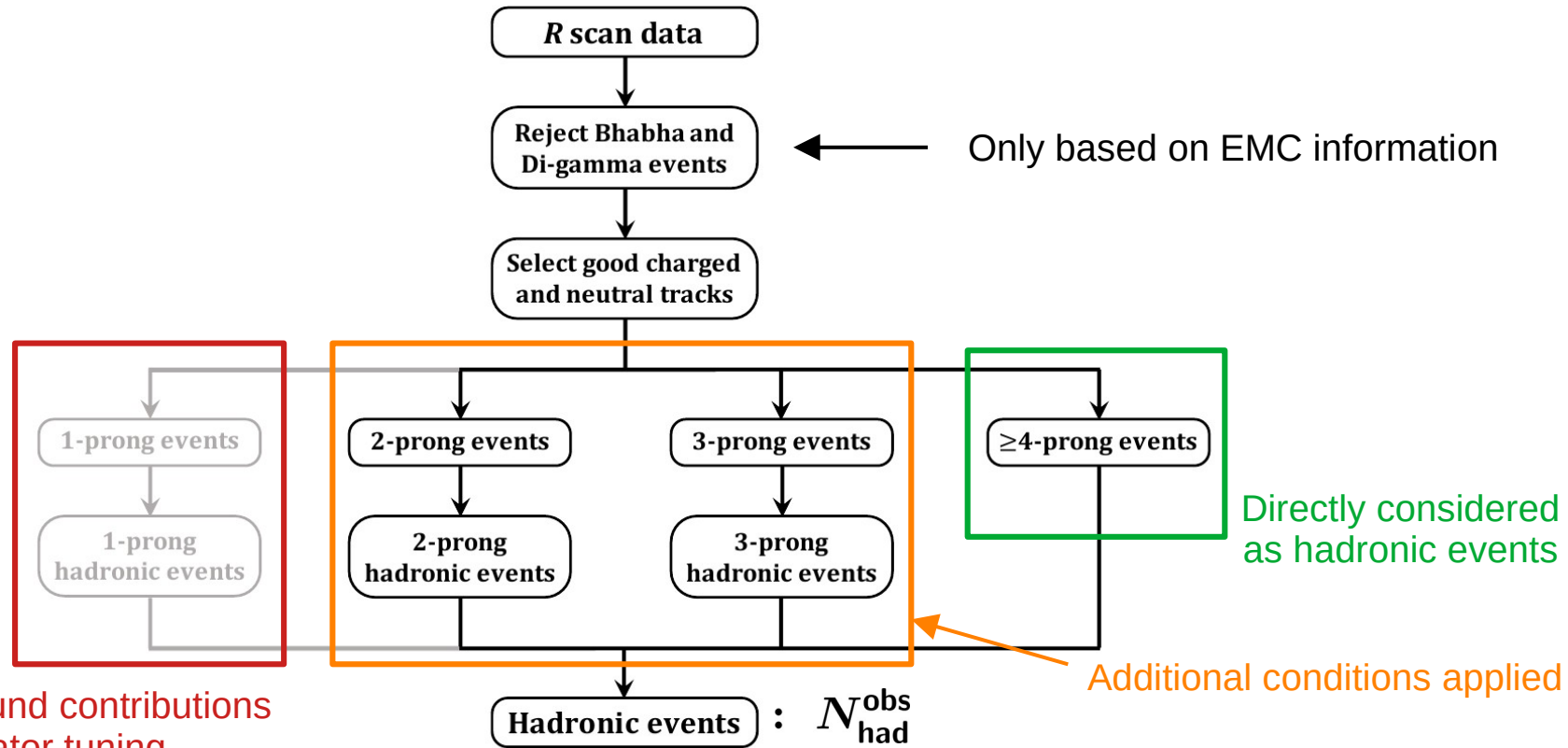
Radiative corrections

- Feynman diagrams
- Structure functions
- Agreement better than 1.4%

Detection efficiency for hadronic events

- Most crucial source of uncertainties
- Evaluated using two different generator models

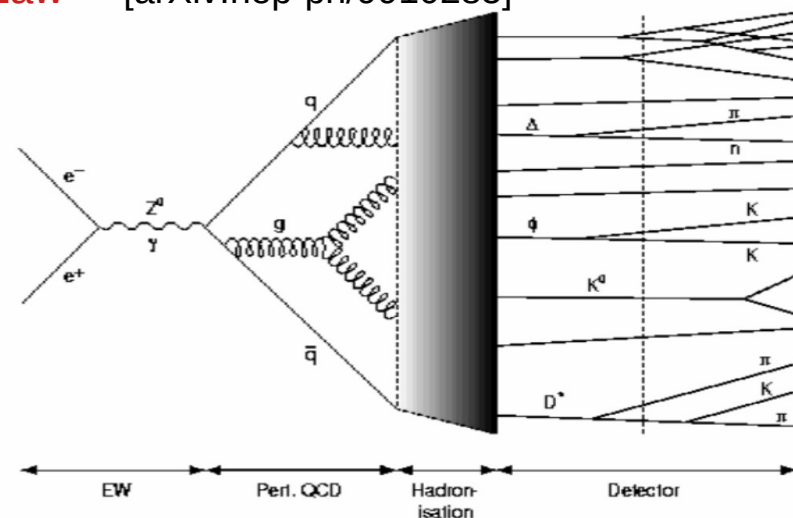
# Analysis Strategy



High QED background contributions  
Only used in generator tuning

# LUARLW: Nominal Model for Signal Simulation

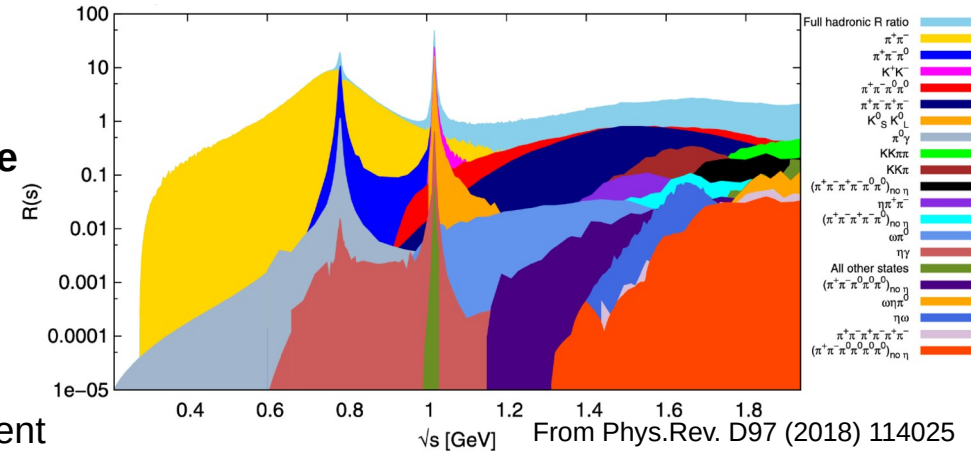
- **Inclusive** event generator
- Self-consistent model
- Developed from **JETSET** for low energies
- Kinematics of initial hadrons determined from **Lund Area Law** [arXiv:hep-ph/9910285]
- Generation of resonant and continuum states
- Initial state radiation implemented from  $m_{\pi\pi}$  to  $\sqrt{s}$
- Phenomenological Parameters tuned to data
- Used in most previous R-Value measurements



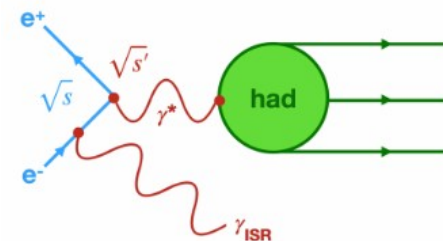
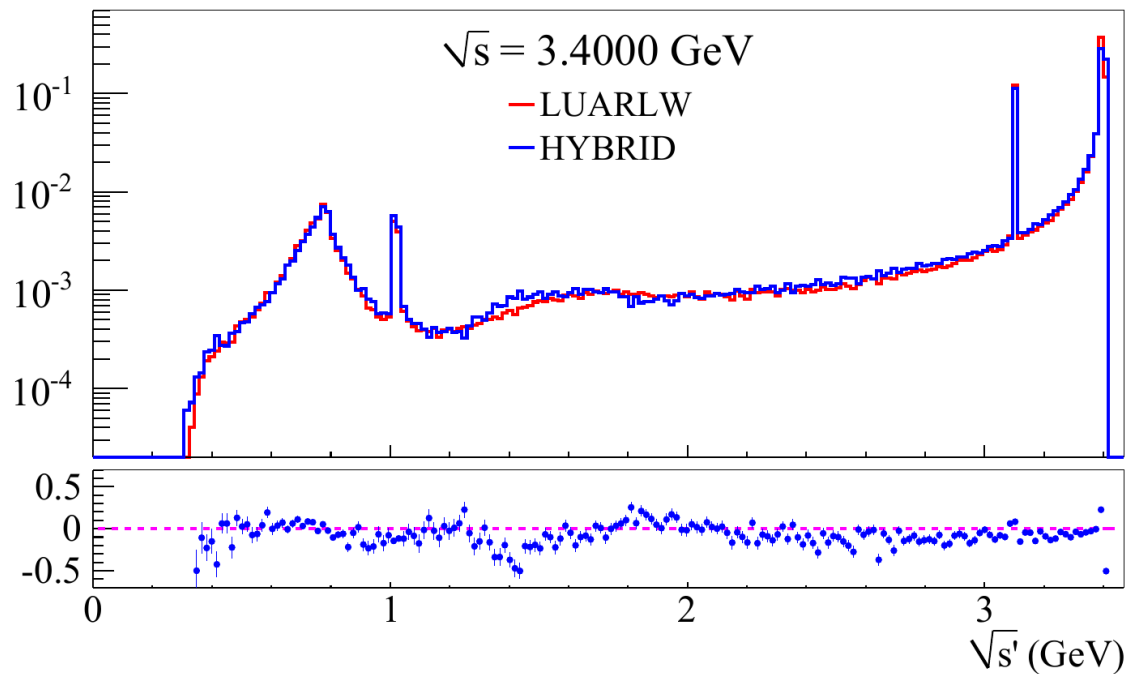
# Alternative Model: “Hybrid Generator”

New event generator developed:

- Idea: Use as much experimental information as possible
- Combination of three established event generators
  - Phokhara
  - 10 exclusive channels, hadronic models tuned to experiment
  - ConExc
  - More than 50 channels with cross sections from experiment
  - LUARLW
- Alternative ISR and VP correction schemes implemented



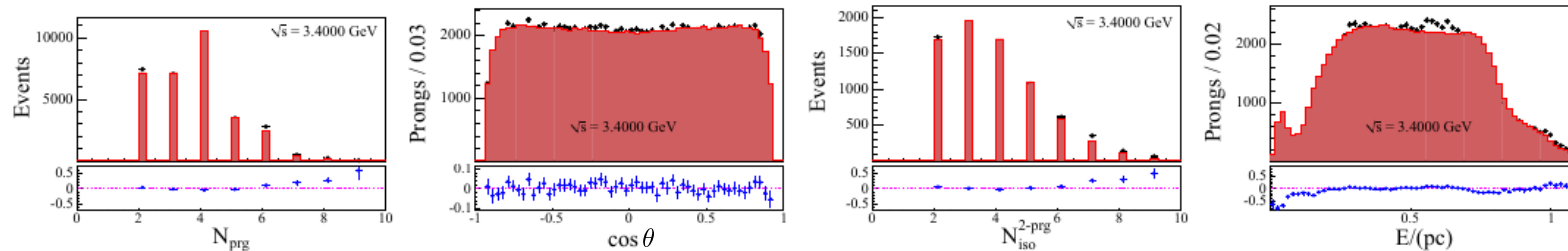
# Comparison of the two Generators



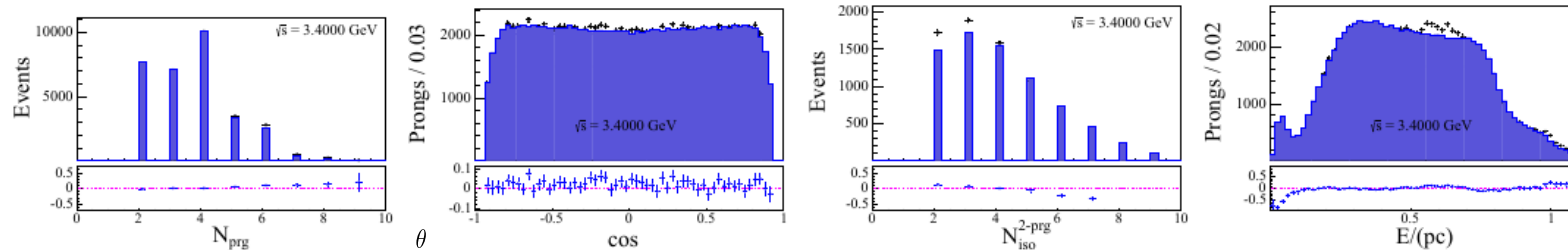
- Effective energy spectrum of simulated ISR processes
- Consistent spectra from two different generators (different ISR schemes)

# Comparison of the two Generators

LUARLW



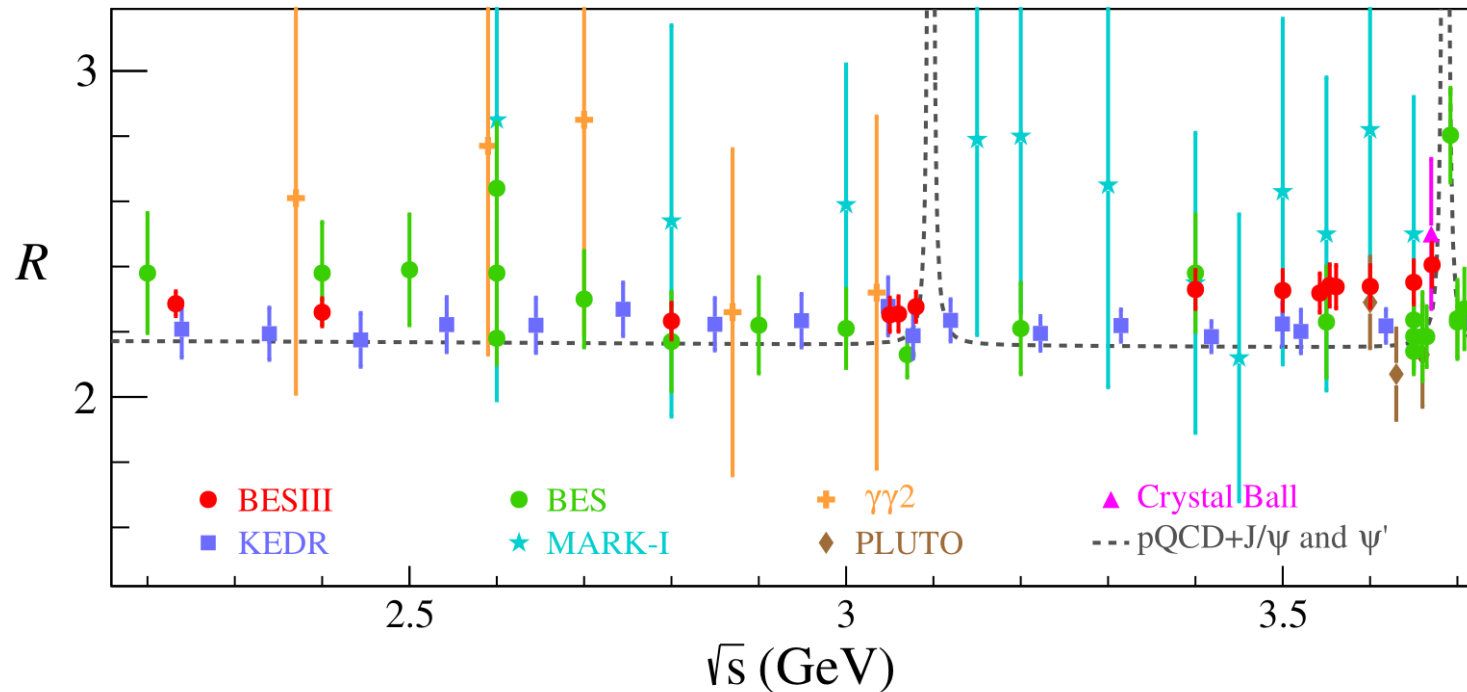
HYBRID



- $N_{\text{prg}}, \theta$  : Number and polar angle of selected charged tracks
- $E/(\text{pc})$  : Ratio of deposited energy and measured momentum per track
- $N_{\text{iso}}^{2\text{prg}}$  : Number of isolated clusters in 2-prong events

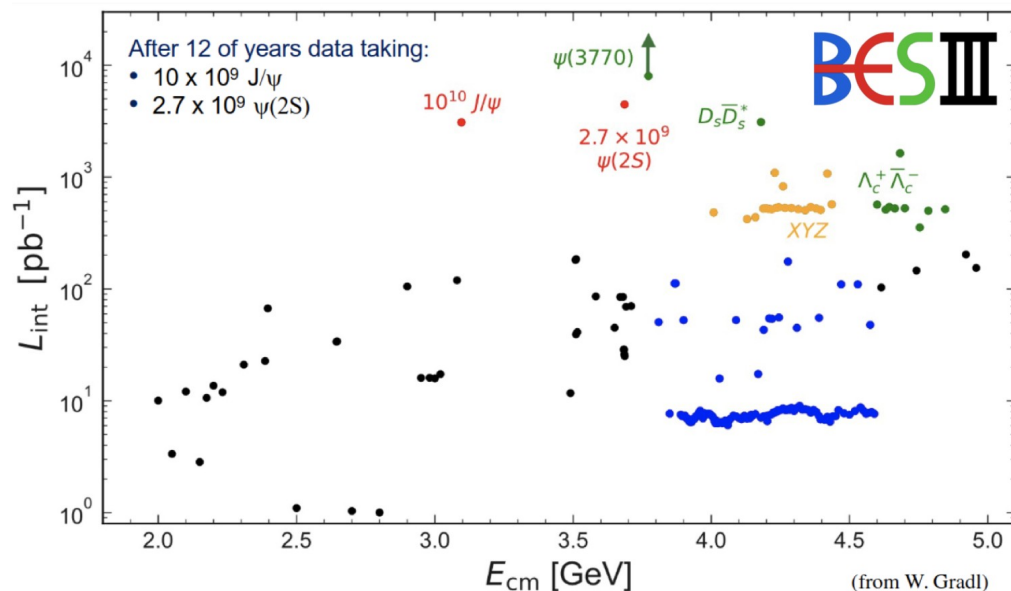
**Good agreement  
of both generator models  
and data !**

# Resulting R-Values



- Accuracy better than **2.6%** for  $\sqrt{s} < 3.1\text{GeV}$  and better than **3%** above
- Exceeding pQCD prediction by  $2.7\sigma$  between 3.4 and 3.6 GeV

# Further R-Value Measurements at BESIII



This work:

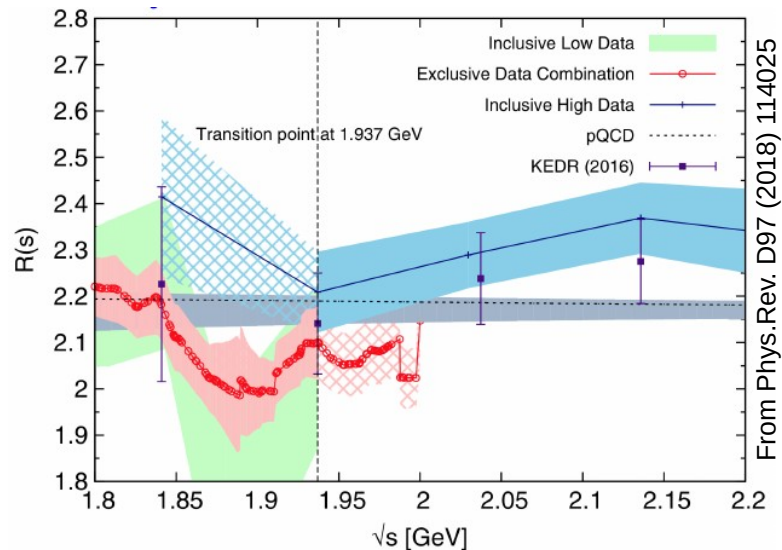
- 14 R scan data points ( $\sim 110 \text{ pb}^{-1}$ )
- 2.23 GeV – 3.67 GeV

For future analysis:

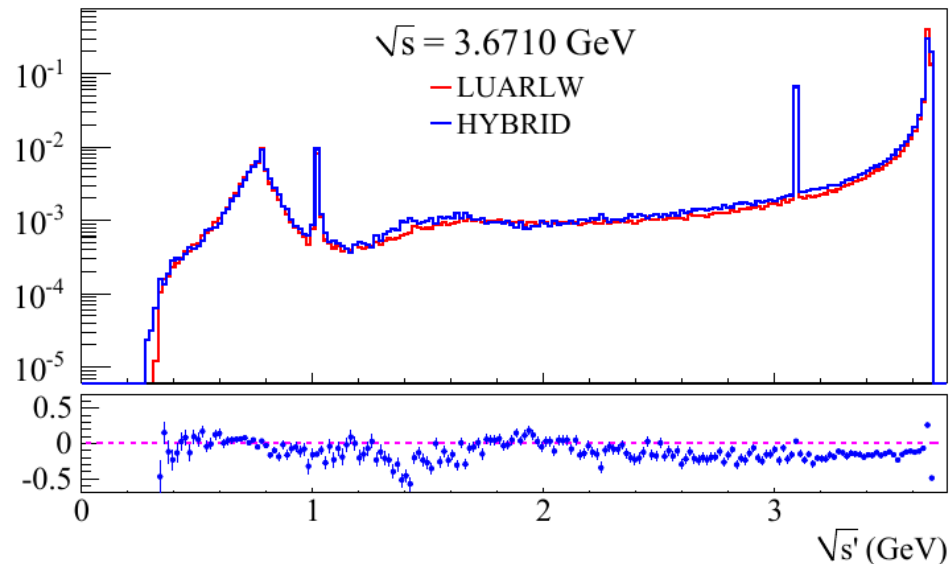
- 21 R scan data points
- 104 R scan data points
- 2.00 GeV – 3.08 GeV
- 3.85 GeV – 4.59 GeV
- $\sim 550 \text{ pb}^{-1}$
- $\sim 800 \text{ pb}^{-1}$

- Large amounts of additional data already collected
  - 139 energy scan points with  $>10^5$  hadrons
- High accuracy R-Value measurements in continuum and open-charm region

# Alternative Approach to R-Value Measurement



- **Exclusive** measurements for  $\sqrt{s} < 2$  GeV
- **Inclusive** measurements for  $\sqrt{s} > 2$  GeV
- Tensions in transition region



- Use **ISR technique**
- Exploit large charmonium data sets at BESIII
- **Better detection efficiency** due to ISR kinematics
- Comparison of inclusive and exclusive measurements

# Summary

High accuracy determination of R-Value important for Standard Model tests

- Running of  $\alpha_{\text{em}}(M_Z^2)$
- Muon anomaly  $a_\mu$

Pilot R-Value measurement at BESIII published in 2022

Phys. Rev. Lett. 128 (2022) 062004

- $2.2324 \leq \sqrt{s}[\text{GeV}] \leq 3.6710$
- Accuracy better than
  - 2.6% below 3.1 GeV
  - 3% in the region above
- Additional high statistics energy scan data samples available
- Alternative approach exploiting ISR being developed at BESIII

See poster by T. Lenz