MENU 2023, October 16-20, 2023, Johannes Gutenberg University of Mainz





Two-pole structures as a universal phenomenon dictated by coupled-channel chiral dynamics

Li-Sheng Geng (耿立升) @ Beihang U.



2307.11631, Jia-Ming Xie, Jun-Xu Lu, **LSG***, Bing-Song Zou



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Λ(1405): **first exotic hadron and two-pole structure**

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Summary and outlook

$\Lambda(1405)$: why is it special



$\Lambda(1405)$: predicted before discovery as $\overline{K}N$ b state



$\Lambda(1405)$ as a dynamically generated state

 $\Box \overline{K}N$ bound state dynamically generated in chiral unitary approaches, which

combine chiral dynamics and coupled channel unitarity.

$$T = V + V + G + V + G + G + G + H + \cdots$$

Bethe-Salpeter Equation





Weinberg-Tomozawa potential

$$V_{ij}=-rac{C_{ij}}{4f^2}(E_i+E_j)$$

LO&NLO, Kaiser, Siegel, Weise, NPA594, 325(1995), 720 citations
 LO, Oset and Ramos, NPA635, 99(1998), 839 citations
 NLO, Oller and Meissner, PLB500, 263(2001), 883 citations

Λ(1405)-dynamical generated two-pole structure!

□Isopin 0, four coupled channels: $\pi \Sigma(1330)$, $\overline{KN}(1433)$, $\eta \Lambda(1662)$, $K\Xi(1813)$

□Renormalization scale $\mu = 630$ MeV, with four different $a_i(\mu)$

Two poles: $W_H = 1424.3 - 17.1i$, $W_L = 1389.1 - 64.1i$



Oller and Meissner, PLB500, 263(2001) Jido, Oller, Oset, Ramos, and Meissner, NPA725, 181 (2003) Hyodo and Jido, PPNP67, 55 (2012)

Λ(1405)-dynamical generated two-pole structure!



Oller and Meissner, PLB500(2001)263 Jido, Oller, Oset, Ramos, and Meissner, NPA725, 181 (2003) Hyodo and Jido, PPNP67, 55 (2012)

Evidence for the two-pole structure of the *A*(1405) **state**

PRL 95, 052301 (2005)

PHYSICAL REVIEW LETTERS

week ending 29 JULY 2005

Evidence for the Two-Pole Structure of the $\Lambda(1405)$ Resonance

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The $K^- p \rightarrow \pi^0 \pi^0 \Sigma^0$ reaction is studied within a chiral unitary model. The distribution of $\pi^0 \Sigma^0$ states forming the $\Lambda(1405)$ shows, in agreement with a recent experiment, a peak at 1420 MeV and a relatively narrow width of $\Gamma = 38$ MeV. The mechanism for the reaction is largely dominated by the emission of a π^0 prior to the $K^- p$ interaction leading to the $\Lambda(1405)$. This ensures the coupling of the $\Lambda(1405)$ to the $K^- p$ channel, thus maximizing the contribution of the second state found in chiral unitary theories, which is narrow and of higher energy than the nominal $\Lambda(1405)$. This is unlike the $\pi^- p \rightarrow K^0 \pi \Sigma$ reaction, which gives more weight to the pole at lower energy and with a larger width. The data of these two experiments, together with the present theoretical analysis, provide firm evidence of the two-pole structure of the $\Lambda(1405)$.







The two-pole structure persists at N2LO

Meson-baryon scattering up to N2LO, Jun-Xu Lu, LSG*, M. Doering and M. Mai, PRL130, 071902(2023)



		Pole positions [MeV]	$ g_{\pi\Sigma} $ [GeV]	$ g_{\eta\Lambda} $ [GeV]	$ g_{\bar{K}N} $ [GeV]	$ g_{K\Xi} $ [GeV]
NNLO	$\Lambda(1380)$	$1392 \pm 8 - i(102 \pm 15)$	6.40 ± 0.10	3.01 ± 0.15	2.31 ± 0.10	0.45 ± 0.01
	$\Lambda(1405)$	$1425 \pm 1 - i(13 \pm 4)$	2.15 ± 0.07	5.45 ± 0.24	4.99 ± 0.08	0.58 ± 0.02
NNLO*	$\Lambda(1380)$	$1384 \pm 7 - i(85 \pm 11)$	3.26 ± 0.11	0.87 ± 0.02	2.04 ± 0.11	0.61 ± 0.02
	$\Lambda(1405)$	$1419 \pm 2 - i(14 \pm 4)$	3.24 ± 0.17	0.42 ± 0.02	6.01 ± 0.12	0.81 ± 0.03

Proper definition of two-pole structures!

Two-pole structures refer to the fact that two dynamically generated states, one resonant and one bound, are located close to each other between two coupled channels and with a mass difference smaller than the sum of their widths.

Two poles overlap, which can create the impression that there is only one state in the invariant mass distribution of their decay products.



Hyodo and Jido, PPNP67, 55 (2012)

LSG, Oset, Roca, and Oller, PRD75, 014017 (2007)

Two prominent examples: $\Lambda(1405)$ and $K_1(1270)$



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Summary and outlook

SU(3) group-theoretical explanation



Jido, Oller, Oset, Ramos, and Meissner, NPA725, 181(2003)

Feng-Kun Guo et al., 2308.07658

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Three questions to ask/answer (not by flavor sym.)



Weinberg-Tomozawa Interaction (leading order)

DLeading order interaction between a NGB and a ground-state baryon

$$\mathcal{L}_{PB}^{WT} = \frac{1}{4f^2} \operatorname{Tr} \left(\bar{\mathcal{B}} i \gamma^{\mu} \left[\Phi \partial_{\mu} \Phi - \partial_{\mu} \Phi \Phi, \mathcal{B} \right] \right)$$

$$\Phi = \begin{bmatrix} \frac{1}{\sqrt{2}} \pi^0 + \frac{1}{\sqrt{6}} \eta_8 & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}} \pi^0 + \frac{1}{\sqrt{6}} \eta_8 & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}} \eta_8 \end{bmatrix} \qquad \mathcal{B} = \begin{bmatrix} \frac{1}{\sqrt{2}} \Sigma^0 + \frac{1}{\sqrt{6}} \Lambda & \Sigma^+ & p \\ \Sigma^- & -\frac{1}{\sqrt{2}} \Sigma^0 + \frac{1}{\sqrt{6}} \Lambda & n \\ \Xi^- & \Xi^0 & -\frac{2}{\sqrt{6}} \Lambda \end{bmatrix}$$

□The Weinberg-Tomozawa (WT) potential--parameter free

$$V_{ij} = -\frac{C_{ij}}{4f^2} \left(2\sqrt{s} - M_i - M_j \right) = -\frac{C_{ij}}{4f^2} \left(E_i + E_j \right)$$

Xiu-Lei Ren, Mon.17:10 (spectroscopy)

Λ(1405)--dynamically generated in Chiral Unitary Approaches



Dynamically generated state — singularities of unitarized amplitude T

See, e.g., Oller, Oset, and Ramos, PPNP45, 157 (2000)

DTo simplify the discussion, consider only the **two most relevant channels** around 1400 MeV: $\overline{K}N(1433)$, $\pi\Sigma(1330)$ --equivalent to the full four-body analysis

> With the subtraction constants: $a_{\overline{K}N} = -1.95$, $a_{\pi\Sigma} = -1.92$, we obtain two poles: $W_H = 1426.0 - 20.1i$, $W_L = 1393.1 - 68.7i$ (to be compared with the four-channel results) $W_H = 1424.3 - 17.1i$, $W_L = 1389.1 - 64.1i$)

UWe gradually turn off the intra-channel coupling to see what happens

Zero coupling limit, see, e.g., Hyodo et al, Phys.Rev.C 77 (2008) 035204 A. Cieplý et al, Nucl. Phys. A, 954:17-40, 2016.

Q1: Is the coupling important?

DMultiply a factor $0 \le x \le 1$, to the off-diagonal matrix elements of the WT potential

$$C_{ij} = \begin{bmatrix} 3 & -\sqrt{\frac{3}{2}}x \\ & 4 \end{bmatrix}$$

□ Even in the limit of complete decoupling (x = 0), there are still two poles:

> $W_H = 1421.8 - 0i,$ $W_L = 1382.2 - 93.6i$



Coupling is relevant for the decay into the lower channel

Q2: How does the nature of NG bosons play a role?

DThe diagonal chiral WT potential

$$V_{\bar{K}N-\bar{K}N}(\sqrt{s}) = -\frac{6}{4f^2}E_{\bar{K}} = -\frac{6}{4f^2}\sqrt{m_{\bar{K}}^2 + q^2}, \qquad m_{K} = 496 \text{ MeV}$$
$$V_{\pi\Sigma-\pi\Sigma}(\sqrt{s}) = -\frac{8}{4f^2}E_{\pi} = -\frac{8}{4f^2}\sqrt{m_{\pi}^2 + q^2}. \qquad m_{\pi} = 138 \text{ MeV}$$

> Explicit chiral symmetry breaking leads to $m_{\pi} \ll m_{K}$. As a result, close to the thresholds, the $\overline{K}N(1433)$ interaction is stronger than the $\pi\Sigma(1330)$ one, which leads to a $\overline{K}N(1433)$ bound state

> The small pion mass combined with the q^2 (energy)-dependence of the interaction is responsible for the dynamical generation of a $\pi\Sigma(1330)$ resonance

Role of explicit chiral symmetry breaking

To study pole trajectories as a function of the light-quark (pion) mass dependence, we need the pion mass dependence of the mesons and baryons

 $m_K^2 = 0.291751 + 0.670652m_\pi^2.$

$$M_B(m_{\pi}) = M_0 + M_B^{(2)} = M_0 + \sum_{\phi=\pi,K} \xi_{B,\phi} m_{\phi}^2$$

Ren, LSG*, Camalich, Meng, and Toki, JHEP12, 073 (2012)

 $> M_0$ is the chiral limit of the baryon mass.

 $\geq \xi_{B,\phi}$ are the relevant parameters containing three low-energy constants, fitted to the lattice QCD data of the **PACS-CS** Collaboration.

Variation of higher pole with m_{π} : simple

DAs m_{π} increases, both the real and the imaginary parts of the higher pole decrease, which indicates that the effective $\overline{K}N$ attraction becomes weaker and the coupling to $\pi\Sigma$ decreases as well.

DNote that the two thresholds increase as well as m_{π} increases.



Variation of lower pole with m_{π} : complicated

□For $m_{\pi} \approx 200$ MeV, , it becomes a virtual resonance from a resonant state.

For a pion mass about 300
 MeV, it becomes a bound state and remains so up to the pion mass of 500 MeV.



The evolution of the lower pole clearly demonstrates the chiral dynamics underlying the two-pole structure of $\Lambda(1405)$.

Lattice QCD study

2307.10413v1

The two-pole nature of the $\Lambda(1405)$ from lattice QCD

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⁶Department of Physics, Carnegie Mellon University, Pittsburgh, Pennsylvania 15213, USA
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This letter presents the first lattice QCD computation of the coupled channel $\pi\Sigma-\bar{K}N$ scattering amplitudes at energies near 1405 MeV. These amplitudes contain the resonance $\Lambda(1405)$ with strangeness S = -1 and isospin, spin, and parity quantum numbers $I(J^P) = 0(1/2^-)$. However, whether there is a single resonance or two nearby resonance poles in this region is controversial theoretically and experimentally. Using single-baryon and meson-baryon operators to extract the finite-volume stationary-state energies to obtain the scattering amplitudes at slightly unphysical quark masses corresponding to $m_{\pi} \approx 200$ MeV and $m_K \approx 487$ MeV, this study finds the amplitudes exhibit a virtual bound state below the $\pi\Sigma$ threshold in addition to the established resonance pole just below the $\bar{K}N$ threshold. Several parametrizations of the two-channel K-matrix are employed to fit the lattice QCD results, all of which support the two-pole picture suggested by SU(3) chiral symmetry and unitarity.

> $m_{\pi} \approx 200$ MeV, a virtual bound state below $\pi\Sigma$ and a resonant (bound) state just below $\overline{K}N$

$$\det[\widetilde{K}^{-1}(E_{\rm cm}) - B^{\boldsymbol{P}}(E_{\rm cm})] = 0 \qquad \frac{E_{\rm cm}}{m_{\pi}}\widetilde{K}_{ij} = A_{ij} + B_{ij}\Delta_{\pi\Sigma},$$



Two poles are found on the (-, +) sheet, which is the one closest to physical scattering in the region between the two thresholds. Their locations are

$$E_1 = 1392(9)(2)(16) \text{ MeV},$$

$$E_2 = [1455(13)(2)(17) - i11.5(4.4)(4)(0.1)] \text{ MeV},$$
(6)

and their couplings

$$\left|\frac{c_{\pi\Sigma}^{(1)}}{c_{\bar{K}N}^{(1)}}\right| = 1.9(4)(6), \qquad \left|\frac{c_{\pi\Sigma}^{(2)}}{c_{\bar{K}N}^{(2)}}\right| = 0.53(9)(10). \tag{7}$$

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Bulava, Mon.10:00 (plenary) Cid-Mora, Mon.16:50 (spectroscopy)

Quark mass evolution—QCDSF-UKQCD



Trajectories following the QCDSF setup



• For $m_{\pi} \approx 200$ MeV, a virtual bound state coupling more to the $\pi\Sigma$ channel and a higher pole coupling more to the $\overline{K}N$ channel were identified.

Q3: Is energy dependence of WT potential relevant?

 $V_{ij} = -\frac{C_{ij}}{4f^2} \left(2\sqrt{s} - M_i - M_j \right) = -\frac{C_{ij}}{4f^2} \left(E_i + E_j \right)$

DReplace the $E_i + E_j$ with $m_i + m_j$, i.e. eliminate the energy dependence.

- **D**With the original subtraction constants, we obtain only **one pole** at 1413.3 13.2i, corresponding to a \overline{KN} bound state.
- **D**S The energy dependence is responsible for the emergence of two-pole structures as we defined here. **D**As the pion mass is much smaller than the kaon mass, the attraction of the $\pi\Sigma$ channel is much weaker than that of the $\overline{K}N$ channel, thus cannot support a bound state.
- □If we increase the attractive potential, we can obtain two bound states, but not a bound state and a resonant state.

 $K_1(1270)$ $I(J^P) = 1/2(1^+), S = 1; M = 1253 \pm 7$ MeV, Γ = 90 ± 20 MeV

DNGB scattering off (instead of a **baryon**) a vector meson

$$\mathcal{L}_{PV}^{WT} = -\frac{1}{4f^2} \operatorname{Tr} \left(\left[\mathcal{V}^{\mu}, \partial^{\nu} \mathcal{V}_{\mu} \right] \left[\Phi, \partial_{\nu} \Phi \right] \right) \qquad \qquad V_{ij} \left(s \right) = -\epsilon^{i} \cdot \epsilon^{j} \frac{C_{ij}}{8f^2} \left[3s - \left(M_{i}^{2} + m_{i}^{2} + M_{j}^{2} + m_{j}^{2} \right) - \frac{1}{s} \left(M_{i}^{2} - m_{i}^{2} \right) \left(M_{j}^{2} - m_{j}^{2} \right) \right].$$

Simplified as the light mass of NGB and in the chiral limit of $M_i = M_j \equiv M$ $V_{ij}(s) = -\epsilon^i \cdot \epsilon^j \frac{C_{ij}}{8f^2} 4M (E_i + E_j)$

Coupled channels: $K^*\pi(1030)$, $\rho K(1271)$, $\omega K(1278)$, $K^*\eta(1440)$, $\phi K(1515)$



Further two-pole structures: singly charmed baryon



 $\Box \overline{K} \Sigma_{c}(2949), \pi \Xi_{c}'(2714);$ ηΞ_{c}'(3125), KΩ_{c}(3191); isospin ½, strangness -1 Λ = 800 MeV



 $W_H = 2882.7 - 21.0i$ $W_L = 2842.6 - 127.9i$

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- Chiral symmetry strongly constrains the interactions of a heavy matter particle with a NG boson--the Weinberg-Tomozawa potentials.
- **2.** The NG boson nature of π , K, (and η) are responsible for the generation of two nearby poles: one bound and one resonant.
- 3. The explicit chiral and SU(3) flavor symmetry breaking dictates that the two relevant coupled channels are close to each other such that the lineshapes of the two states overlap and thus create the impression that there is only one state.

Summary and outlook

■We anticipate such two-pole structures in other systems governed by the same chiral dynamics and encourage dedicated experimental and lattice QCD studies to verify the chiral dynamics underlying such phenomena.

We stress that as noted already in the literature flavor symmetry also plays a relevant role here, as it dictates the relative coupling strengths between different channels.

Thanks a lot for your attention!