



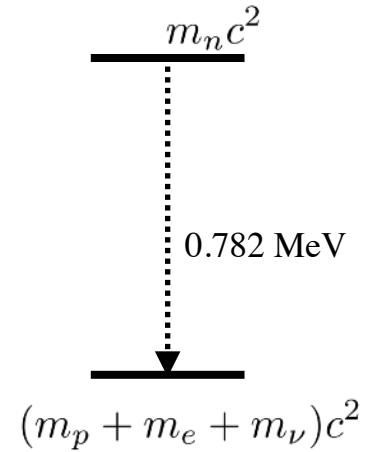
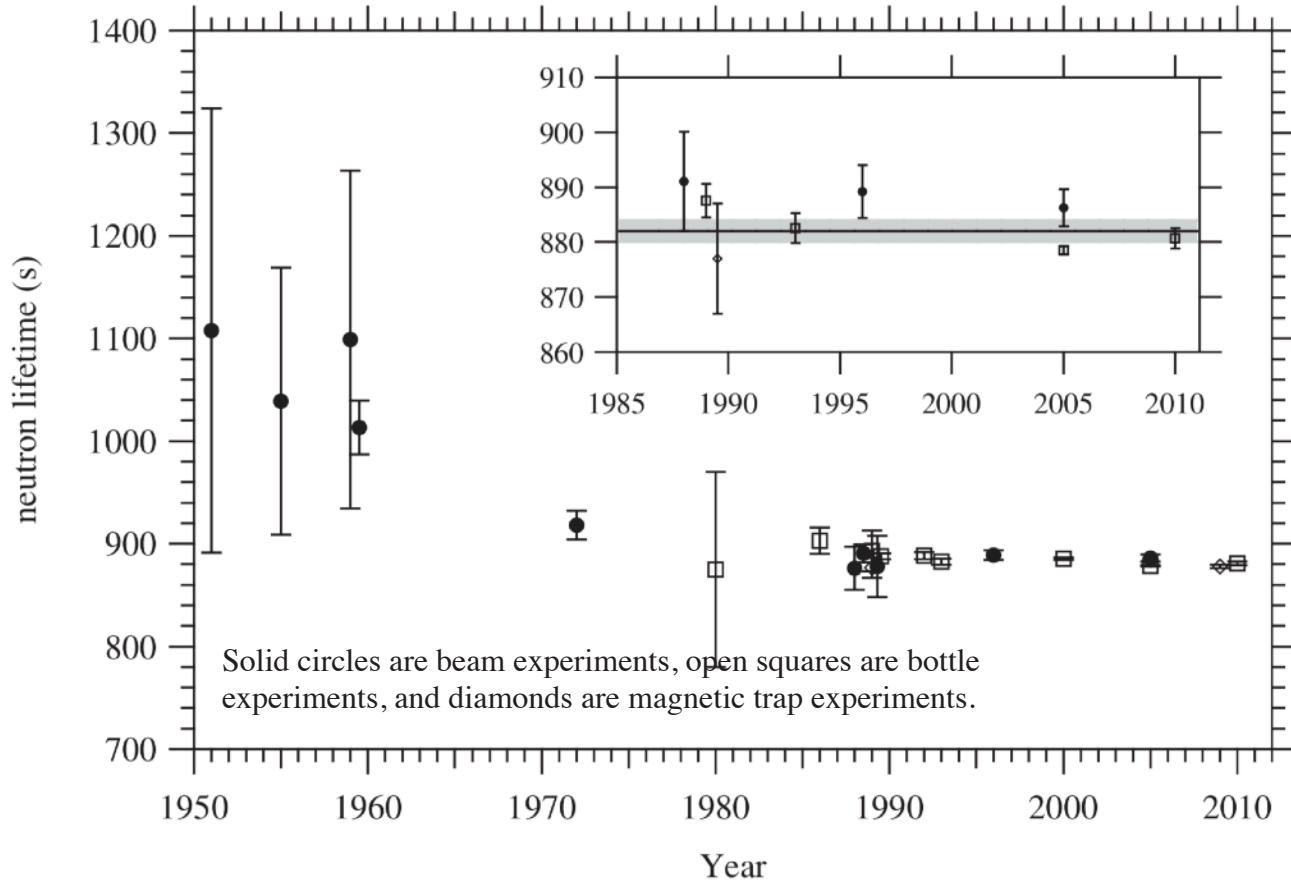
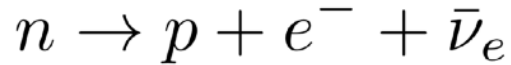
***Near threshold resonances and exotic
decay of ^{11}Be***

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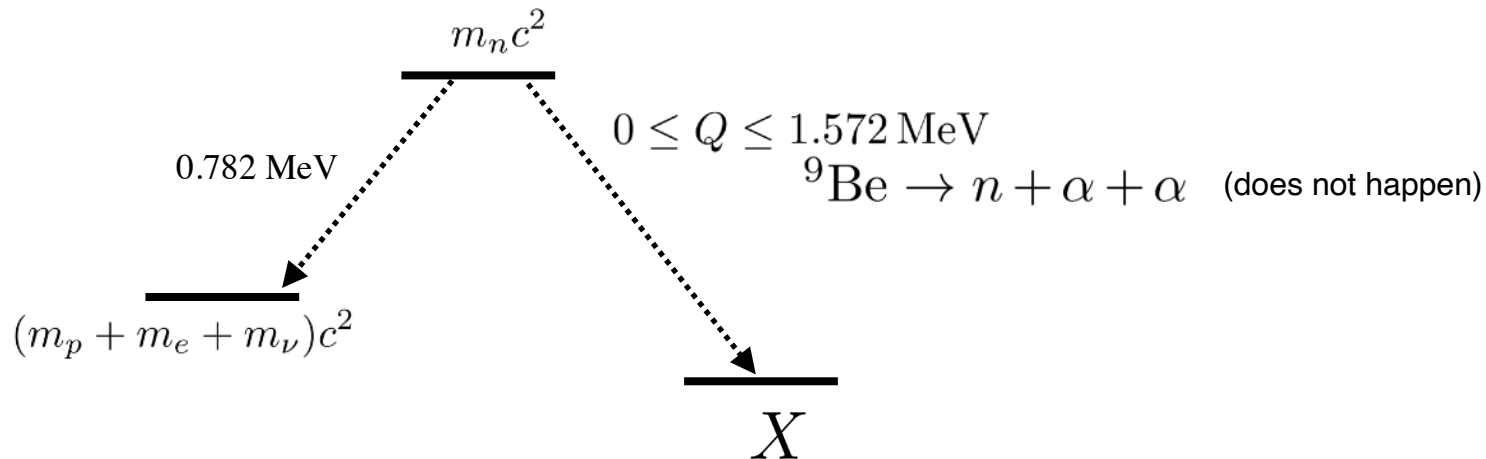
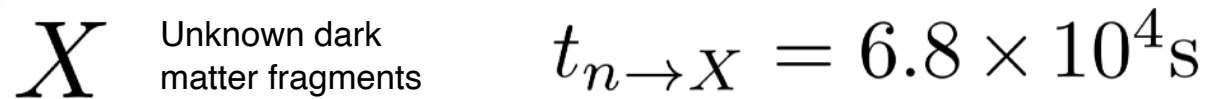
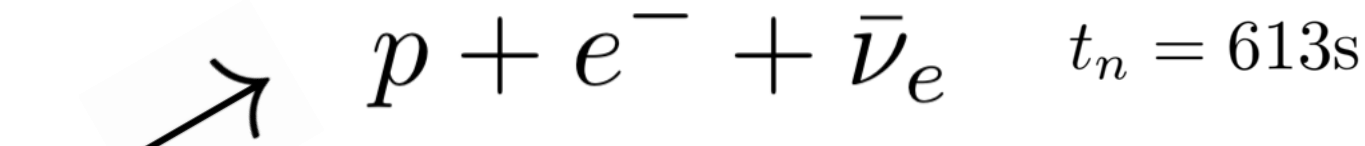
Four seconds of uncertainty



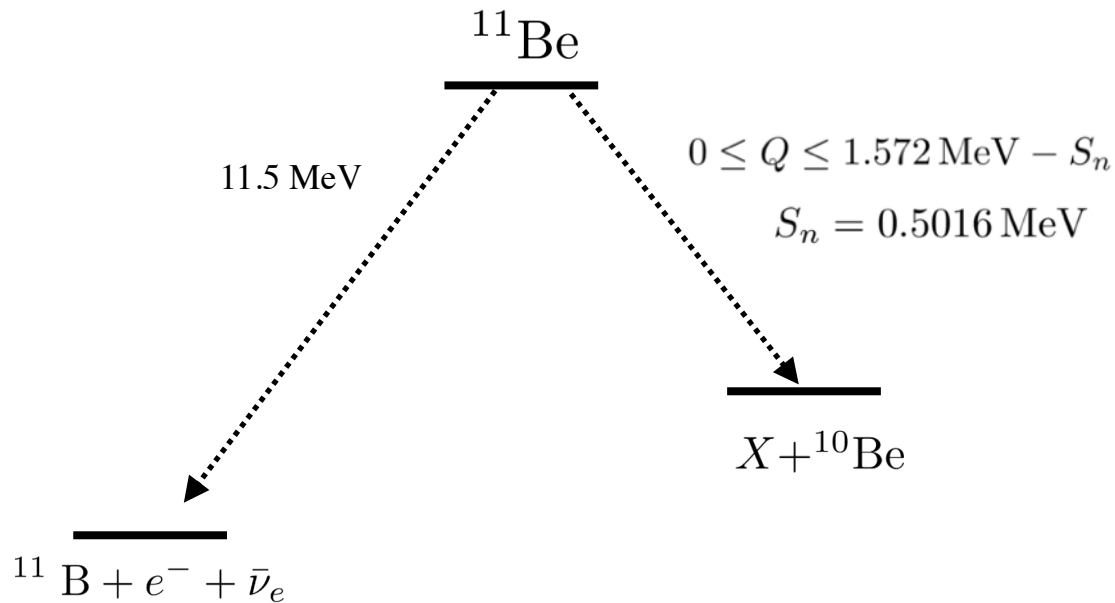
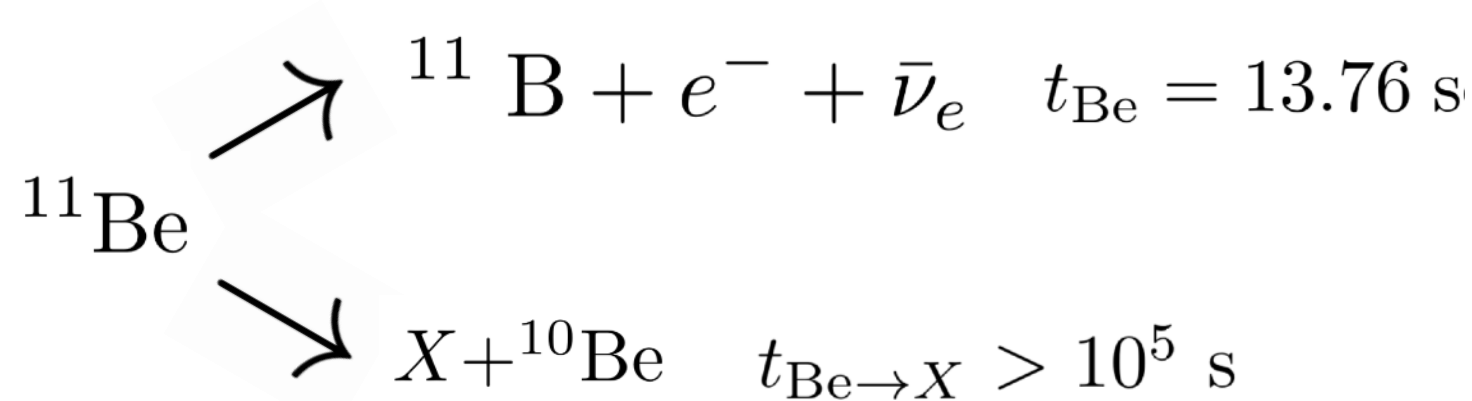
$$880\text{s} \leq \tau_n \leq 884\text{s}$$

$$\text{Half-life } 610\text{s} \leq t_n \leq 613\text{s}$$

What if?



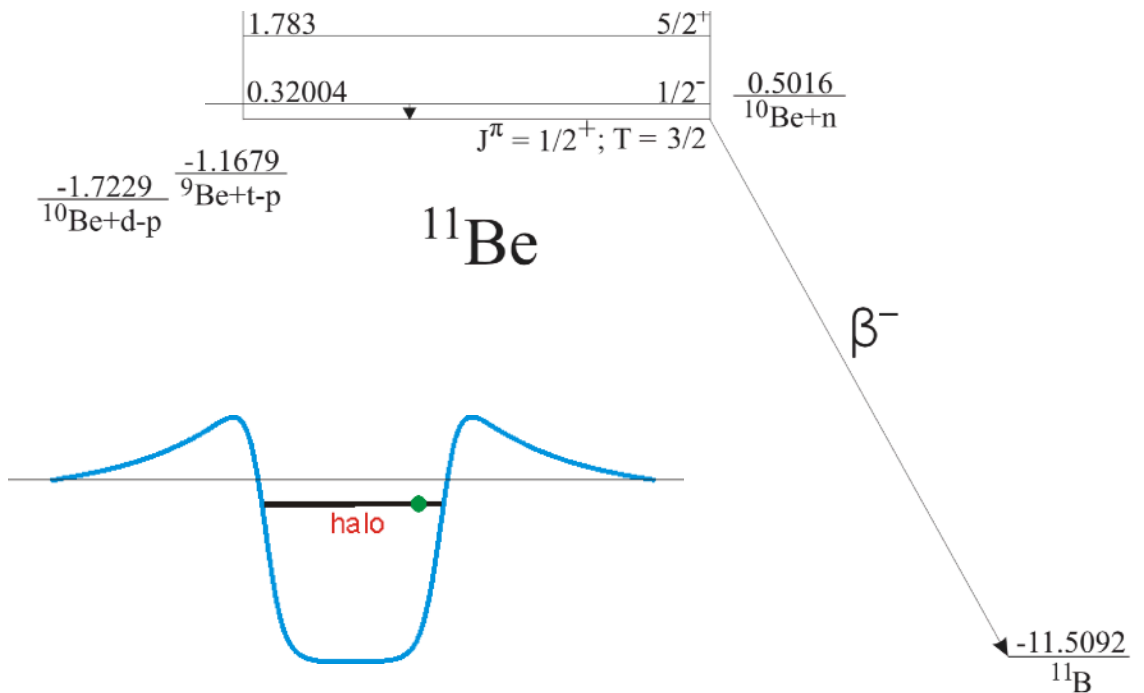
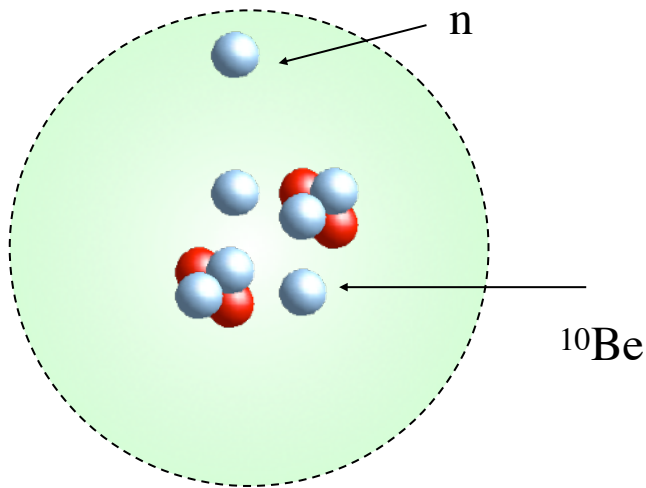
^{11}Be best candidate



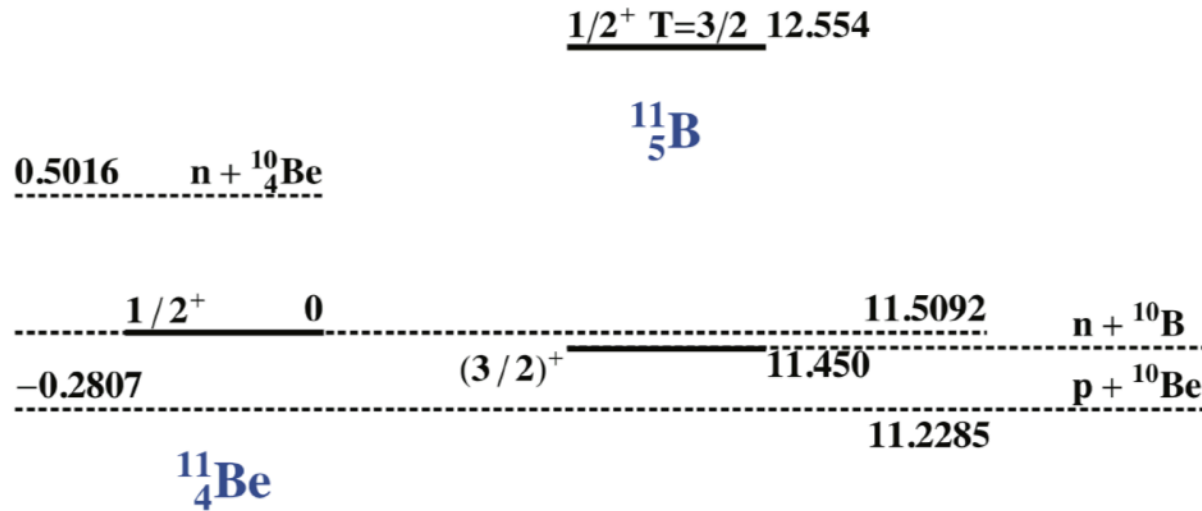
^{11}Be , an interesting nucleus

Halo phenomenon, weakly bound neutron
 Clustering+molecular structure
 Rotations

$$S_n = 0.5016 \text{ MeV}$$



^{11}Be beta-delayed proton decay



Ayyad Y, et al. Phys. Rev. Lett., 123 (2019) 082501.
 Riisager K, et al. Phys. Lett. B, 732 (2014) 305.
 Borge M, et al. J. Phys. G, 40 (2013) 035109.

$1/2^+$ 9.820

Observed half-life (???)

$$t_{\text{Be} \rightarrow \beta p} \approx 1 \times 10^6 \text{ s.}$$

$\alpha + ^7_3\text{Li}$

Notes on beta-decay rates

$$ft = \frac{\mathcal{T}}{B(F) + \lambda_A^2 B(GT)} \quad \mathcal{T} = 6145 \text{ s}$$

$$\lambda_A = 1.27$$

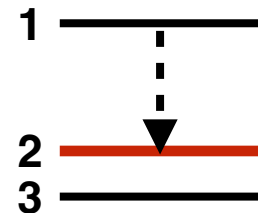
Neutron decay $n \rightarrow p + e^- + \bar{\nu}_e$ $B(F) = 1$ $B(GT) = 3$

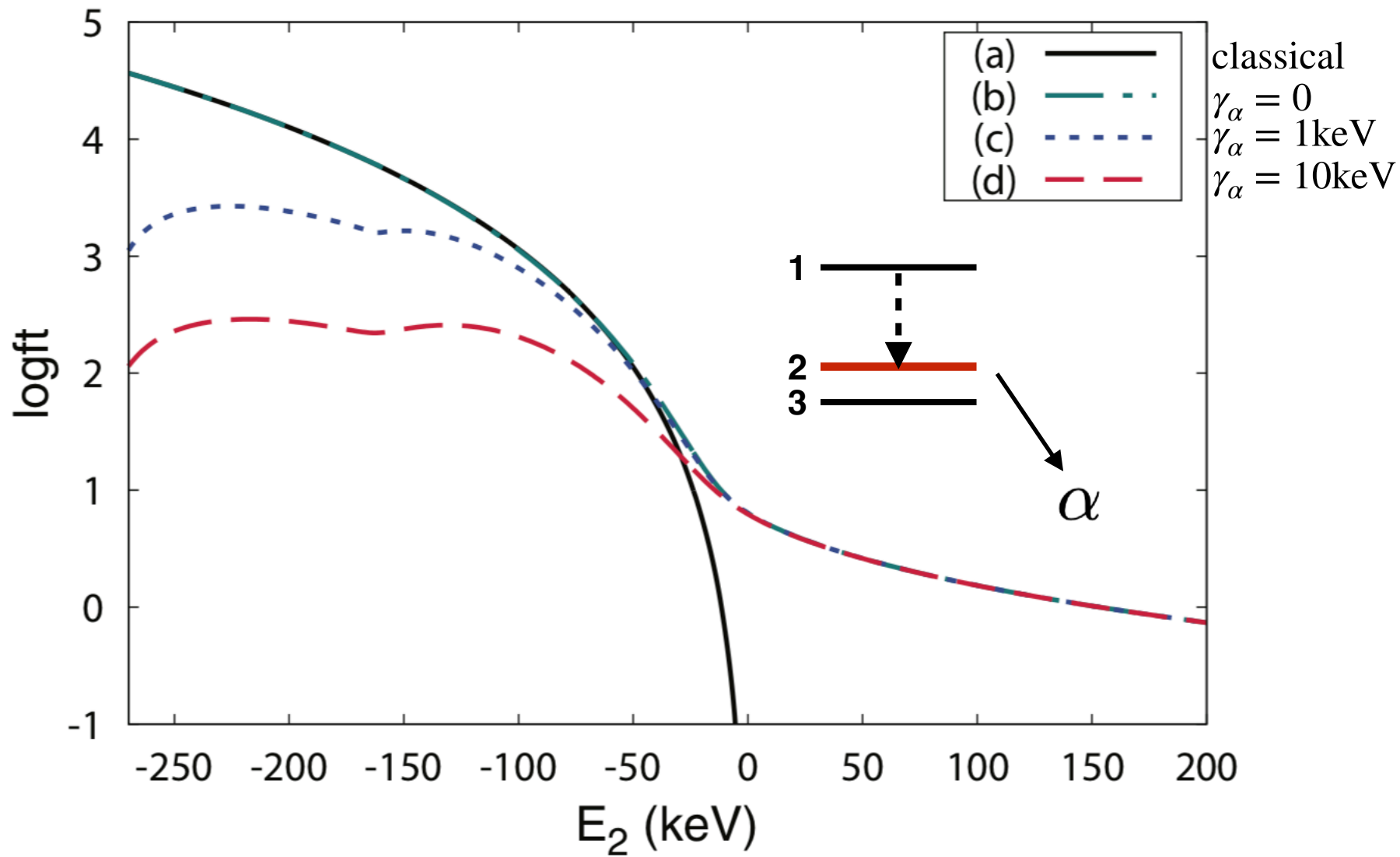
$$f(Q) = 1.715$$

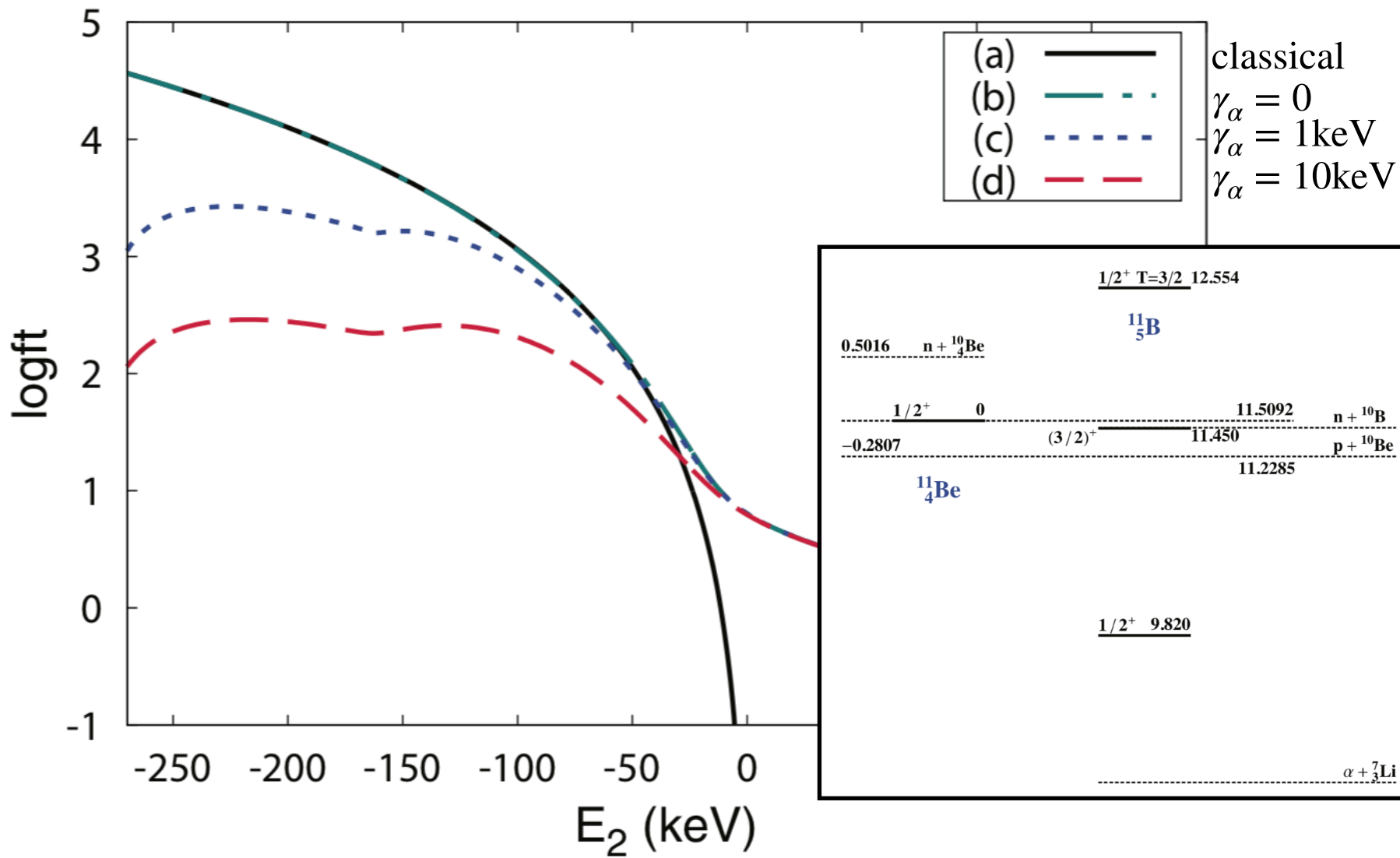
Sequential beta decay

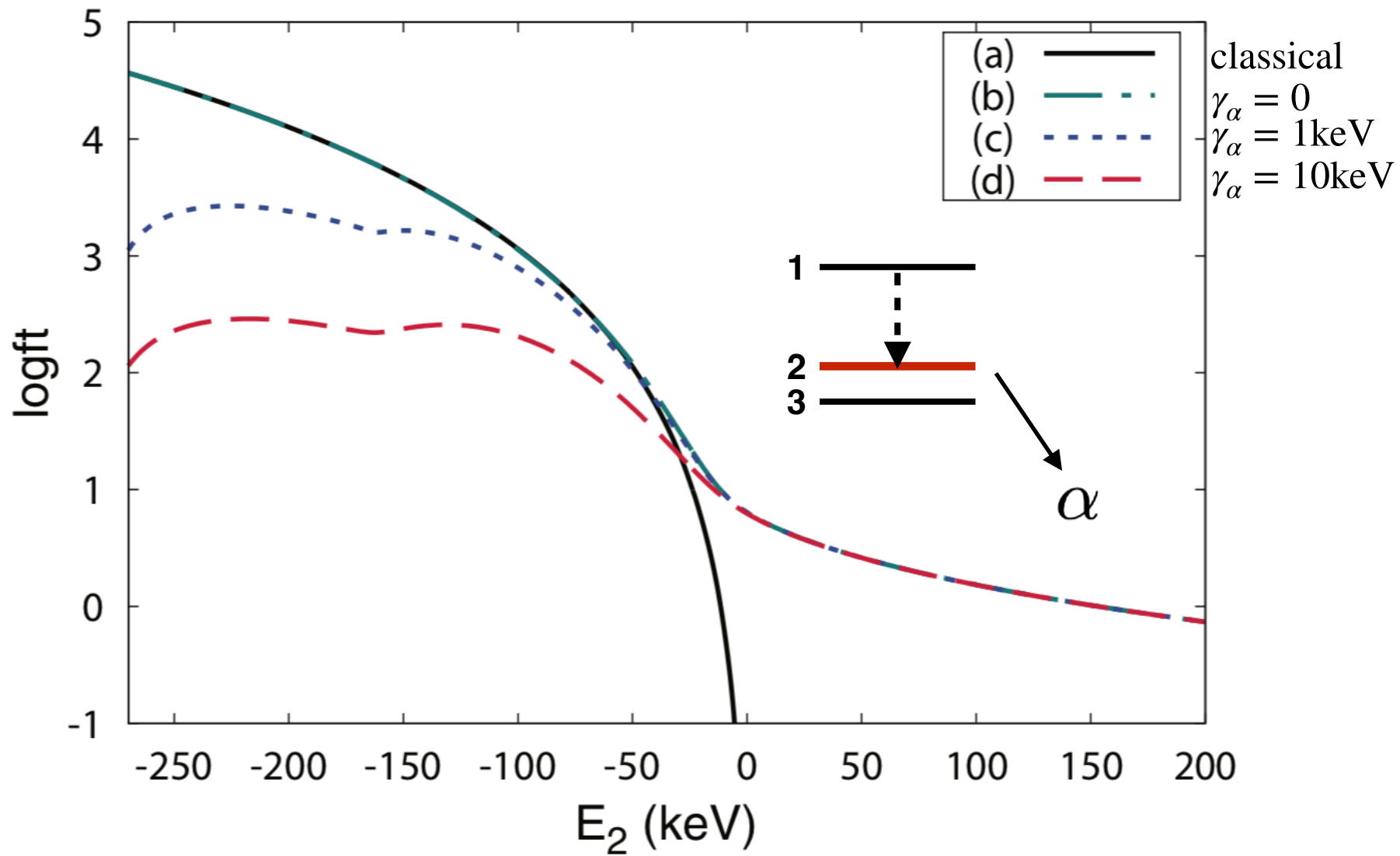
For sequential decay

$$\mathcal{F}(Q) = \int_0^Q \frac{d\epsilon}{2\pi} \frac{f(\epsilon)\gamma_2(Q - \epsilon)}{(\epsilon + E_2)^2 + \Gamma_2^2(Q - \epsilon)/2}$$

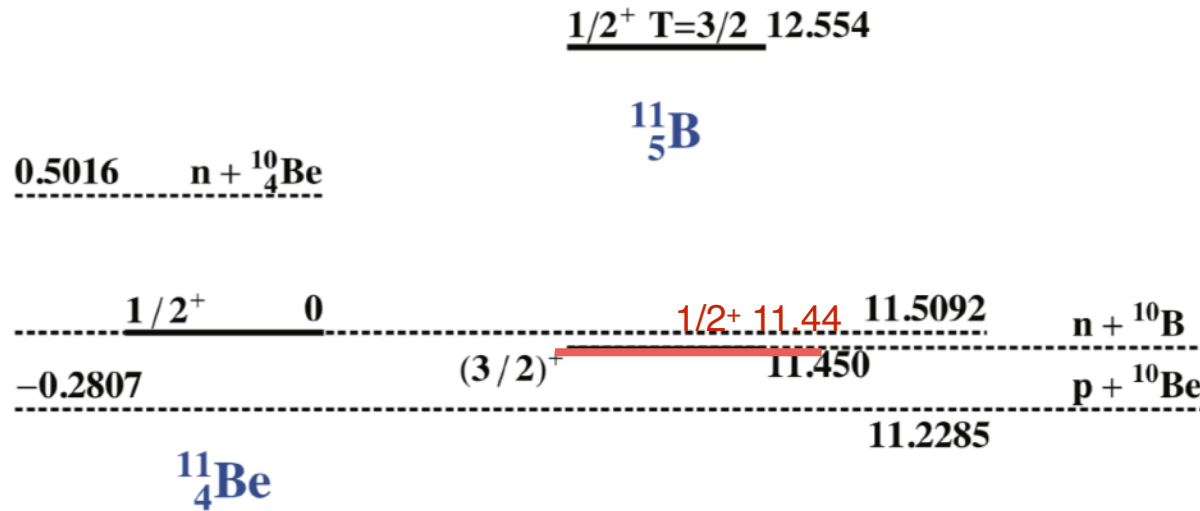








^{11}Be beta-delayed proton decay



E. Lopez-Saavedra *et al.*, *Phys. Rev. Lett.*, vol. 129, no. 1, p. 012502, Jun. 2022, doi: [10.1103/PhysRevLett.129.012502](https://doi.org/10.1103/PhysRevLett.129.012502).

Y. Ayyad *et al.* *Phys. Rev. Lett.*, vol. 129, no. 1, p. 012501, Jun. 2022, doi: [10.1103/PhysRevLett.129.012501](https://doi.org/10.1103/PhysRevLett.129.012501).

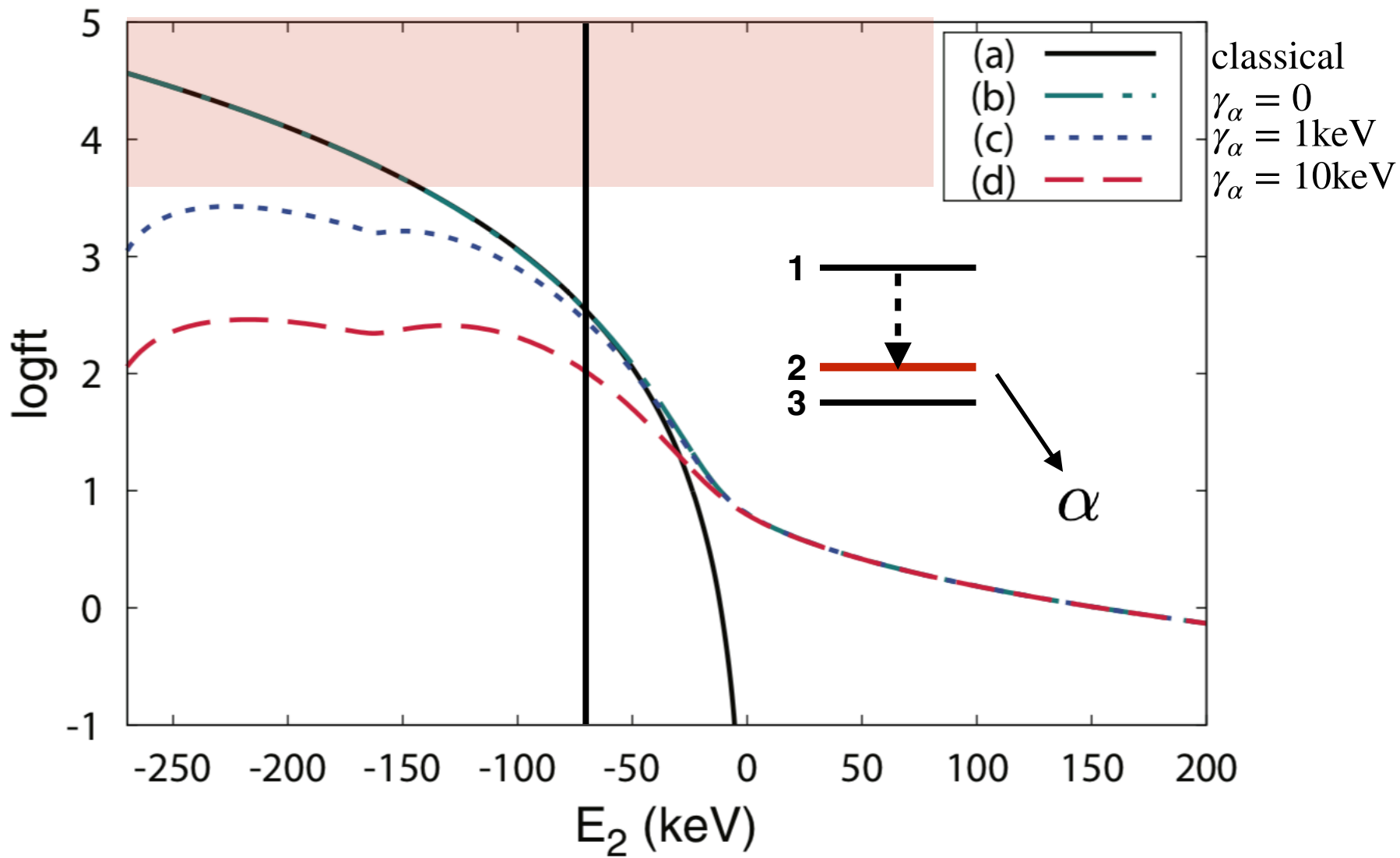
Observed half-life (???)

$$t_{\text{Be} \rightarrow \beta p} \approx 1 \times 10^6 \text{ s.}$$

$\alpha + ^7_3\text{Li}$

1/2+ states in 11B

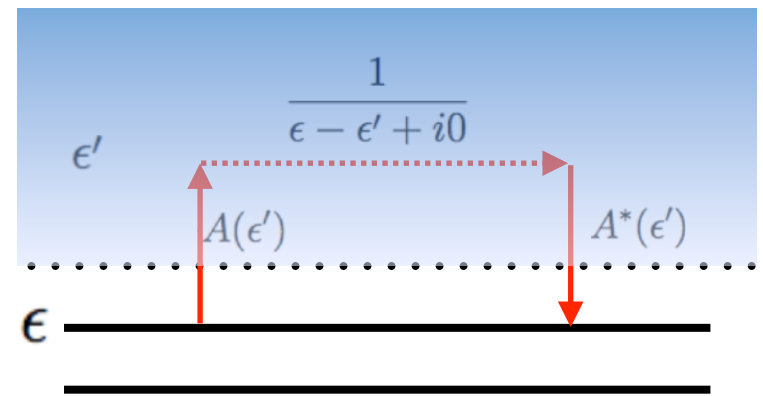
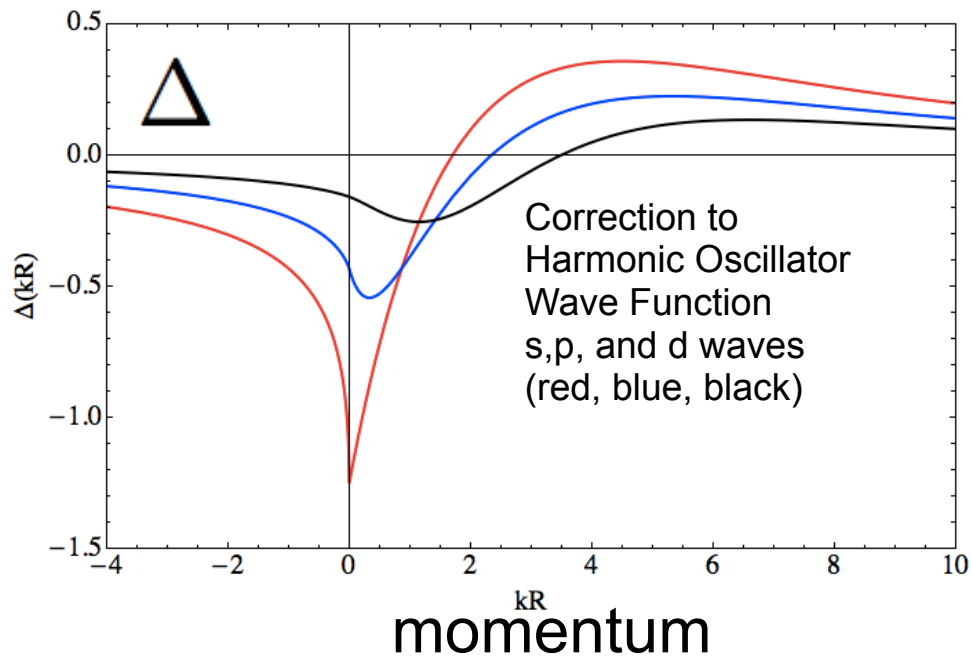
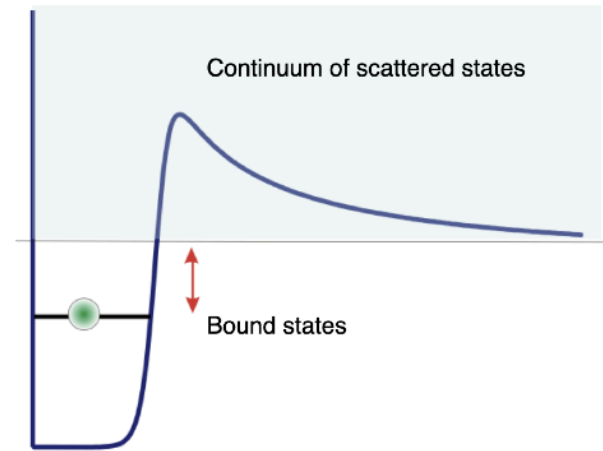
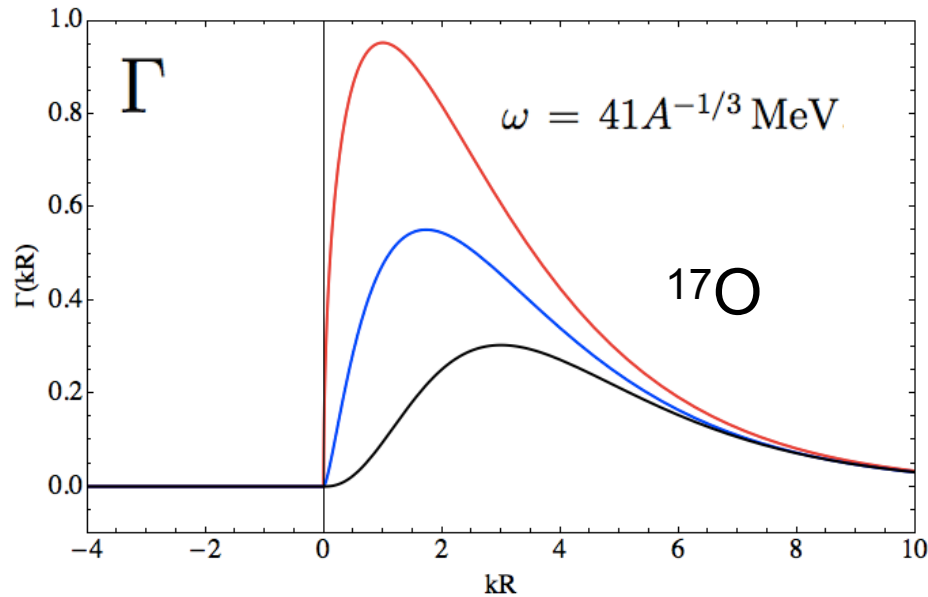
J	Theory (FSU)			Experiment	
	E(MeV)	log(ft)	SF(p)	E(MeV)	SF(p)
1/2+(1)	5.709	5.5	0.262	6.792	
1/2+(2)	10.545	3.4	0.117	9.820	
1/2+(3)	11.952	3.5	0.134	11.44	0.27(6)
1/2+(4) T=3/2	12.181		0.274	12.554	
1/2+(5)	12.827	4.0	0.028		
1/2+(6)	14.105	5.4	0.001		



Questions

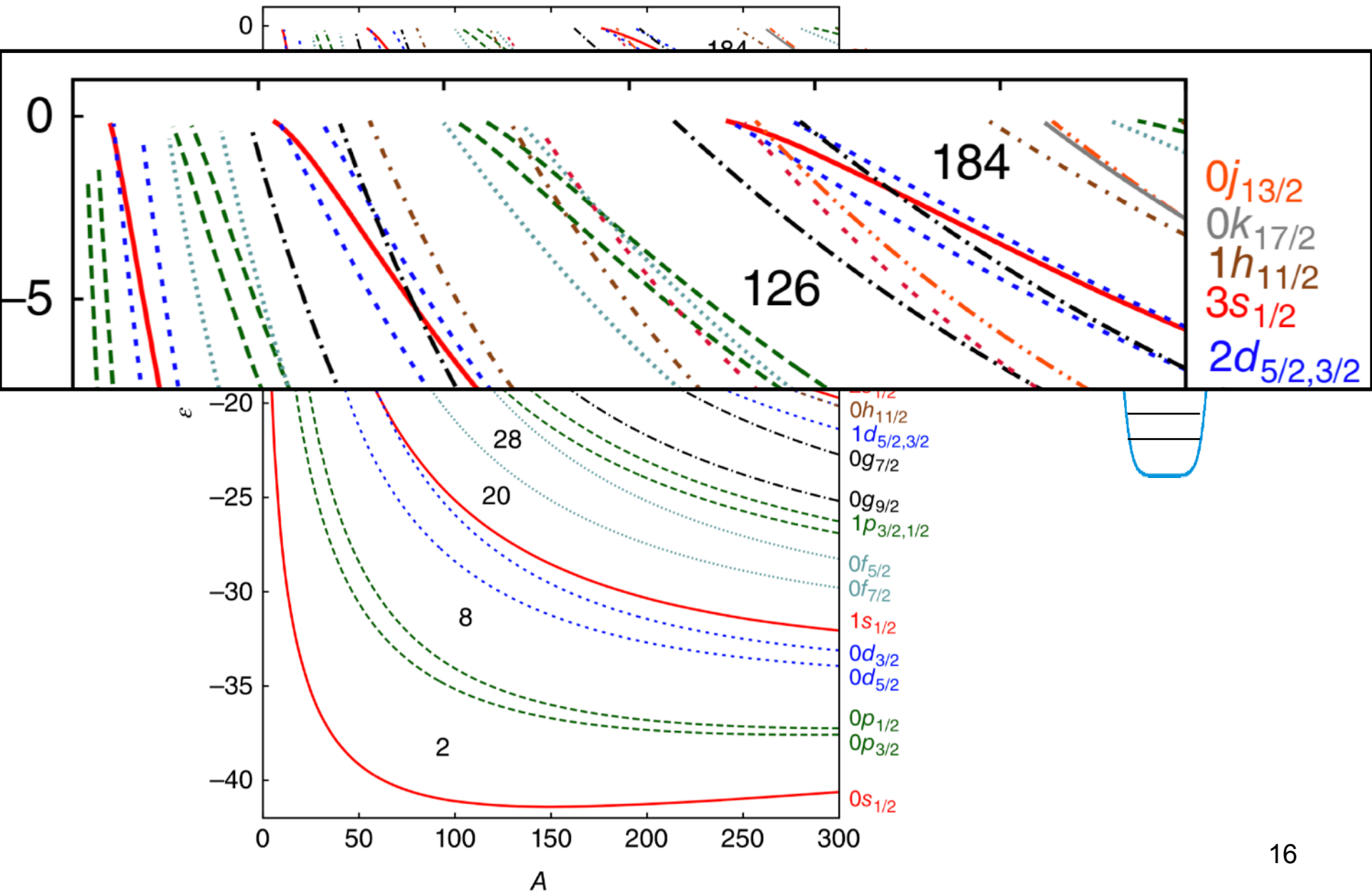
- Even with proton resonance, beta-delayed rate is impossible to explain
- The proton resonance is likely $1/2^+(3)$, why it is lowered (predicted 12.2 MeV, observed at 11.44 MeV)
- Why proton SF is so large, while there is no alpha decay?

Threshold discontinuity

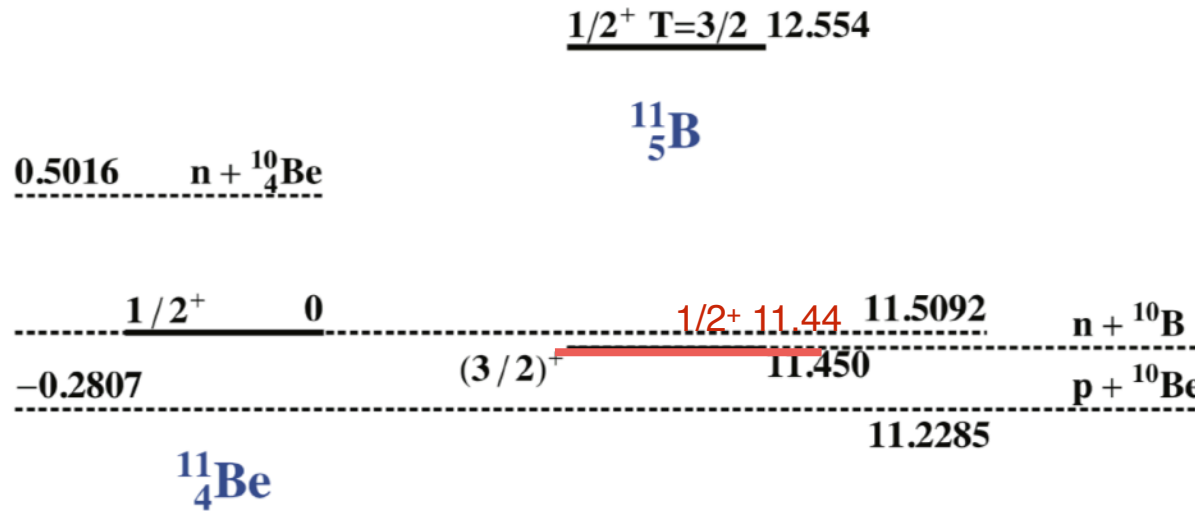


$$H'(\epsilon) = \int_0^{\infty} d\epsilon' A^*(\epsilon') \frac{1}{\epsilon - \epsilon' + i0} A(\epsilon')$$

Evolution of single particle energies



11Be beta-delayed proton decay



E. Lopez-Saavedra *et al.*, *Phys. Rev. Lett.*, vol. 129, no. 1, p. 012502, Jun. 2022, doi: [10.1103/PhysRevLett.129.012502](https://doi.org/10.1103/PhysRevLett.129.012502).

Y. Ayyad *et al.* *Phys. Rev. Lett.*, vol. 129, no. 1, p. 012501, Jun. 2022, doi: [10.1103/PhysRevLett.129.012501](https://doi.org/10.1103/PhysRevLett.129.012501).

Observed half-life (???)

$$t_{\text{Be} \rightarrow \beta p} \approx 1 \times 10^6 \text{ s.}$$

$\alpha + ^7_3\text{Li}$

Wave function realignment

Superradiance

$$H = \begin{pmatrix} \epsilon - \frac{i}{2}\Gamma & v \\ v & 0 \end{pmatrix} = H_0 - \frac{i\Gamma}{2} A^\dagger A \quad A = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

Stationary system $\Gamma = 0$

Energies $E_{1,2} = \frac{1}{2} \left(\epsilon \pm \sqrt{\epsilon^2 + 4v^2} \right)$

Spectroscopic Factors $SF_{1,2} = \frac{1}{2} \left(1 \pm \frac{\epsilon}{\sqrt{\epsilon^2 + 4v^2}} \right)$

Observing superradiance

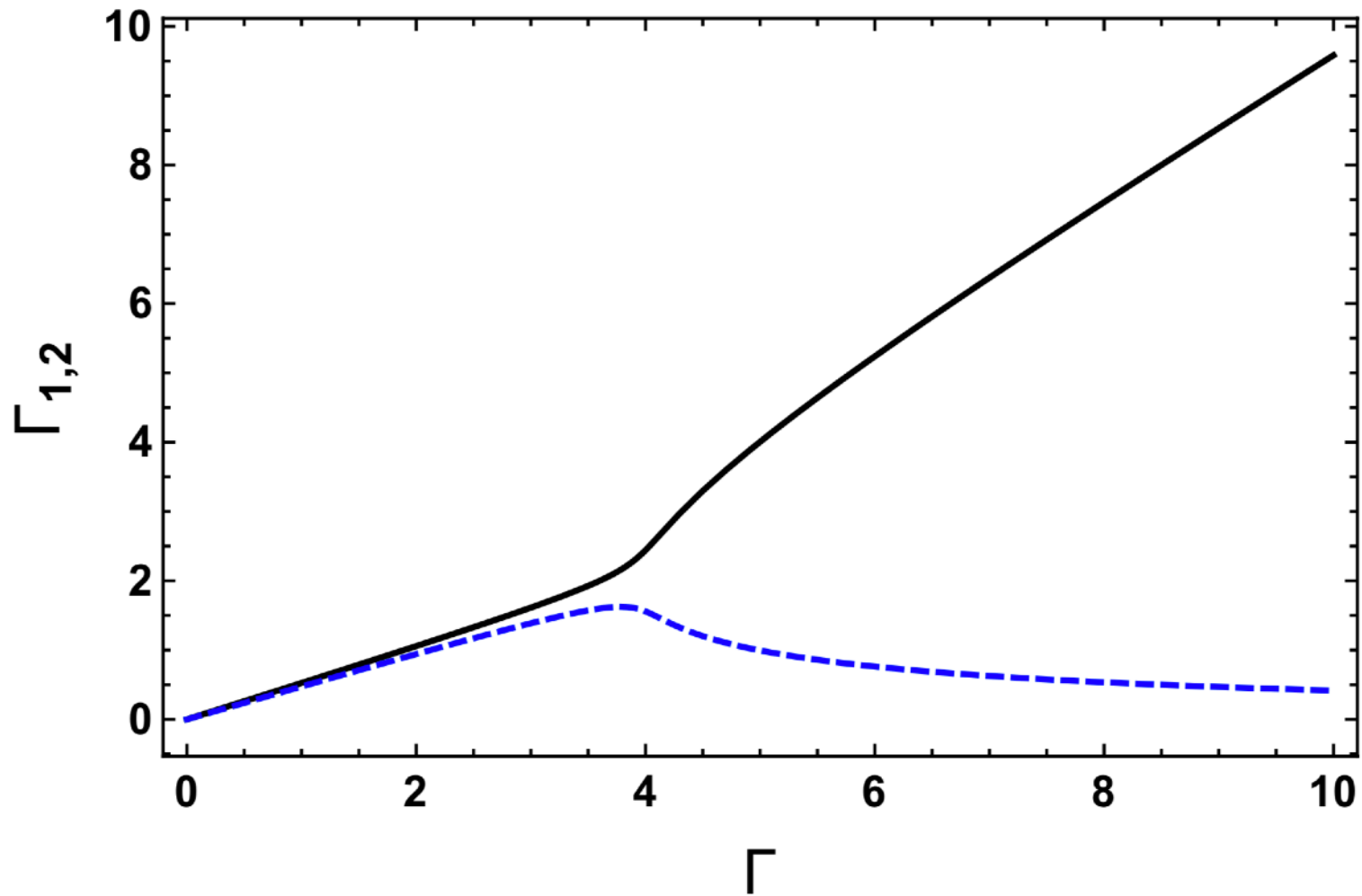
$$H = \begin{pmatrix} \epsilon - \frac{i}{2}\Gamma & v \\ v & 0 \end{pmatrix} = H_0 - \frac{i\Gamma}{2} A^\dagger A \quad A = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

Energies $\mathcal{E}_{1,2} = \frac{1}{2} \left(\epsilon - \frac{i}{2}\Gamma \pm \sqrt{\left(\epsilon - \frac{i}{2}\Gamma \right)^2 + 4v^2} \right)$

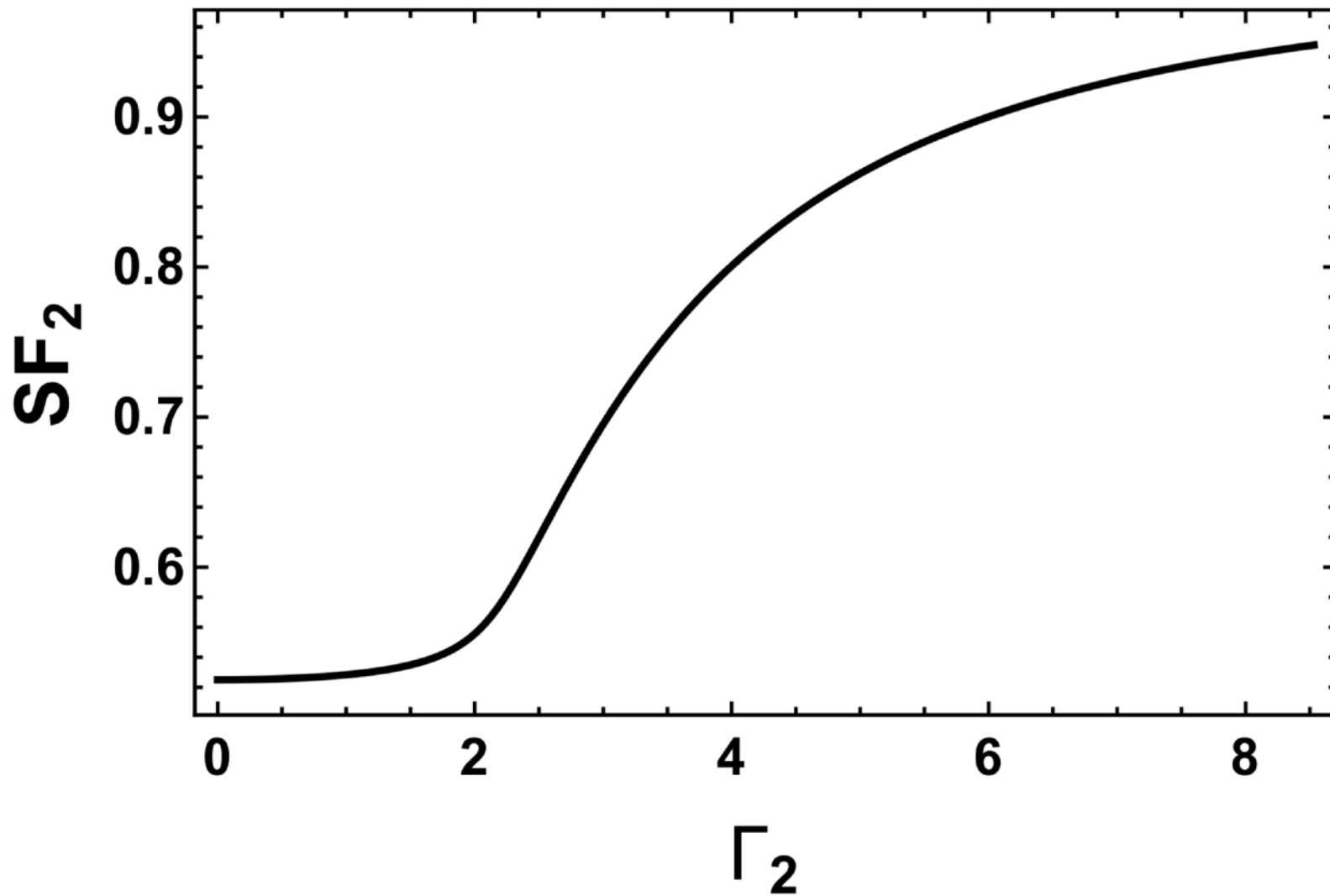
Width $\Gamma_{1,2} = -2 \operatorname{Im}(\mathcal{E}_{1,2})$

Spectroscopic Factors $\text{SF}_{1,2} = \Gamma_{1,2}/\Gamma$

Observing superradiance



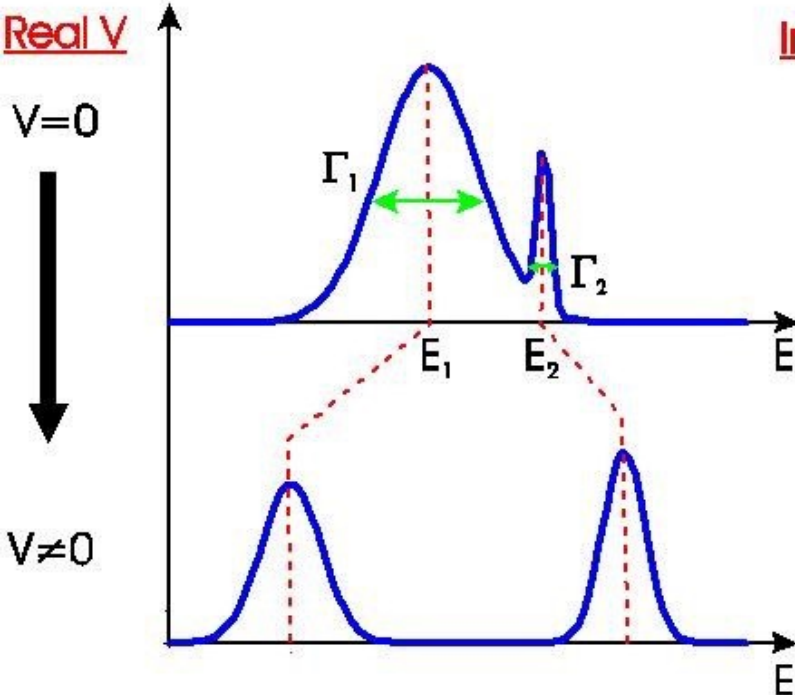
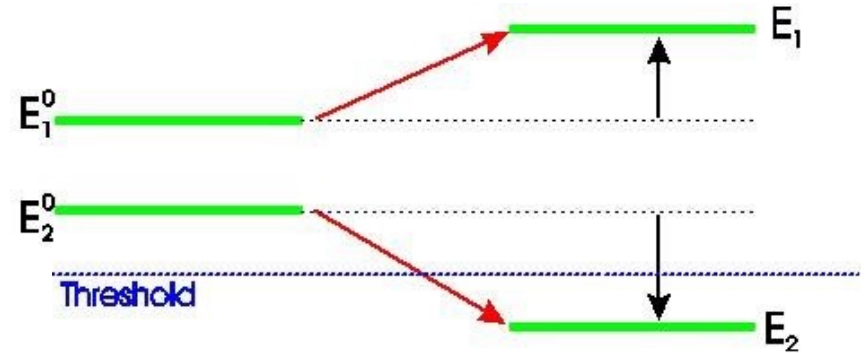
Spectroscopic factor for superradiant state



Example of interacting resonances

^{13}C , ^{13}N , ^{11}Li

$$\mathcal{H} = H^0 + V - iW/2$$



Imaginary W

$W \neq 0$

$W = 0$



Summary:

^{11}B resonant state may represent a remarkable near-threshold effect

Position of the state

Strong orientation towards proton decay channel

Weak alpha channel

^{11}Be decay and resonance in ^{11}B is not a fully resolved story.

Acknowledgements:

Funding: U.S. DOE contract DE-SC0009883.

Publications:

A. Volya, *EPL* 130 (2020) 12001.

E. Lopez-Saavedra et al., *Phys. Rev. Lett.*, 129, (2022) 012502.

A. Volya, M. Barbui, V. Z. Goldberg, and G. V. Rogachev, *Commun Phys* 5 (2022), 1