

$0\nu\beta\beta$ in Effective Field Theory

Wouter Dekens

with

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J. Menéndez, P. Soriano, M. Hoferichter,
U. van Kolck, A. Walker-Loud



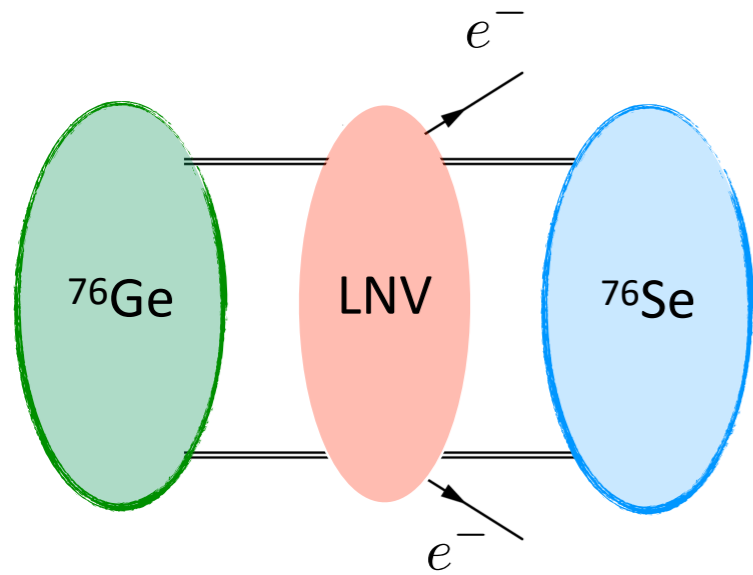
UNIVERSITY *of* WASHINGTON



INSTITUTE for
NUCLEAR THEORY

Introduction

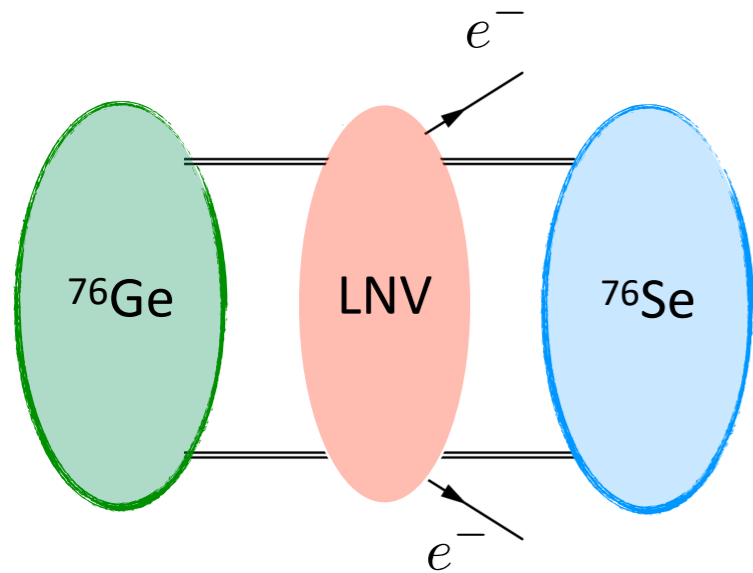
$0\nu\beta\beta$



- Violates lepton number, $\Delta L=2$

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- Stringently constrained experimentally
 - To be improved by 1-2 orders

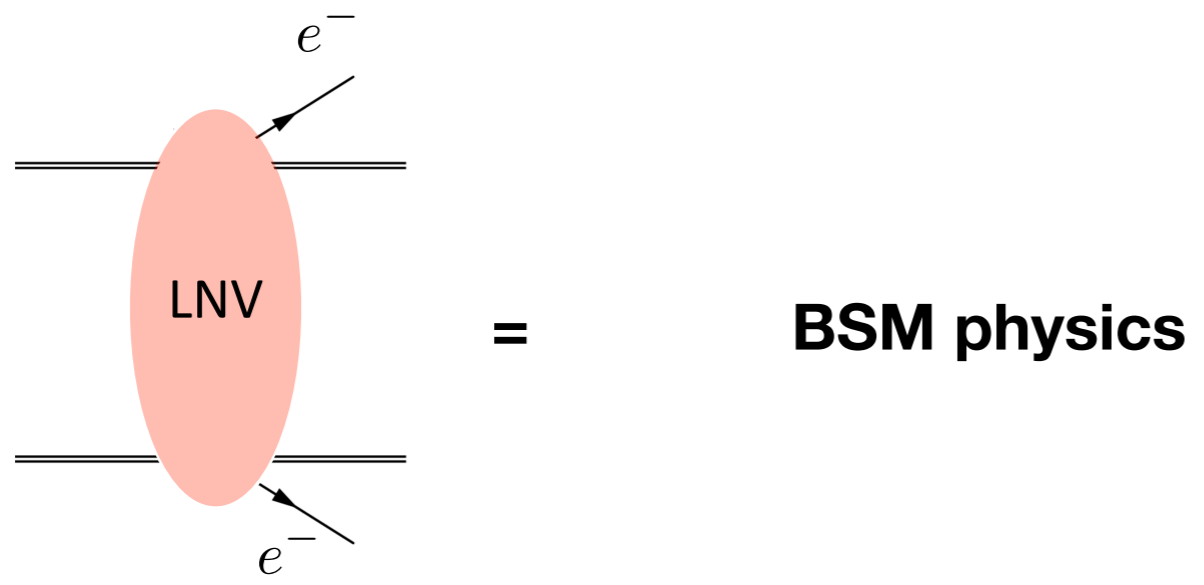
$T_{1/2}^{0\nu}({}^{76}\text{Ge})$	$T_{1/2}^{0\nu}({}^{130}\text{Te})$	$T_{1/2}^{0\nu}({}^{136}\text{Xe})$
Gerda	Cuore	KamLAND-zen
$> 9 \cdot 10^{25} \text{ yr}$	$> 3.2 \cdot 10^{25} \text{ yr}$	$> 2.3 \cdot 10^{26} \text{ yr}$

Future reach:
(LEGEND, nEXO,
CUPID)

$$T_{1/2}^{0\nu} > 10^{28} \text{ yr}$$

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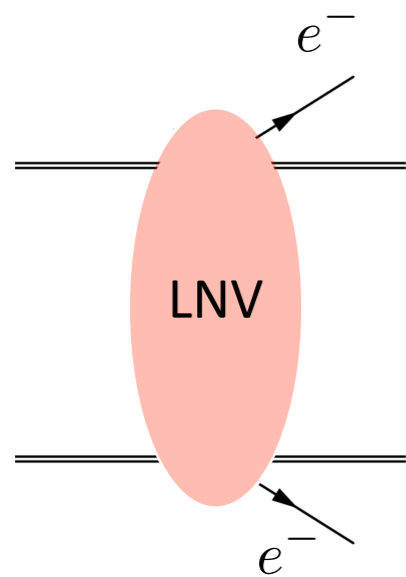
- Would imply
 - Neutrino's are Majorana particles
 - Physics beyond the SM
 - Connections to LHC, leptogenesis?

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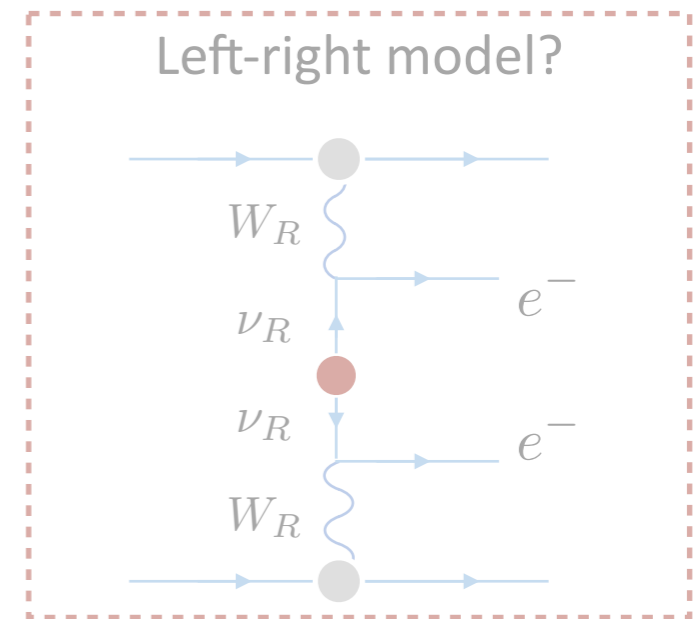
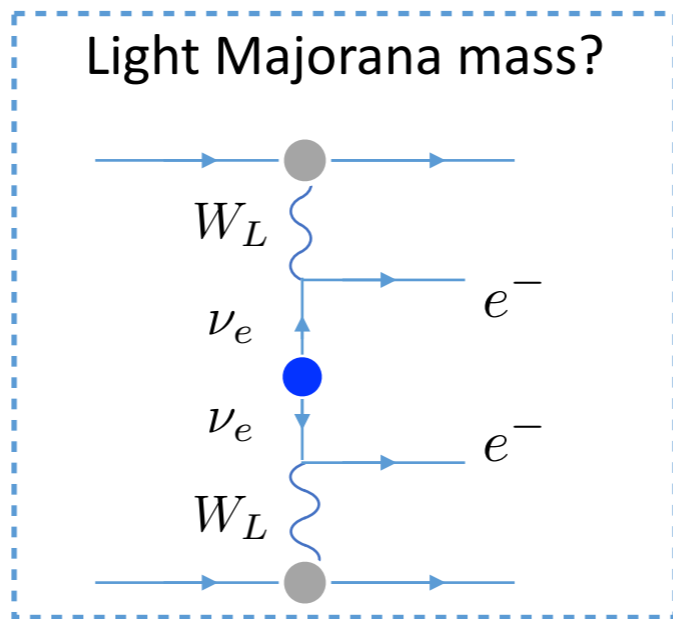
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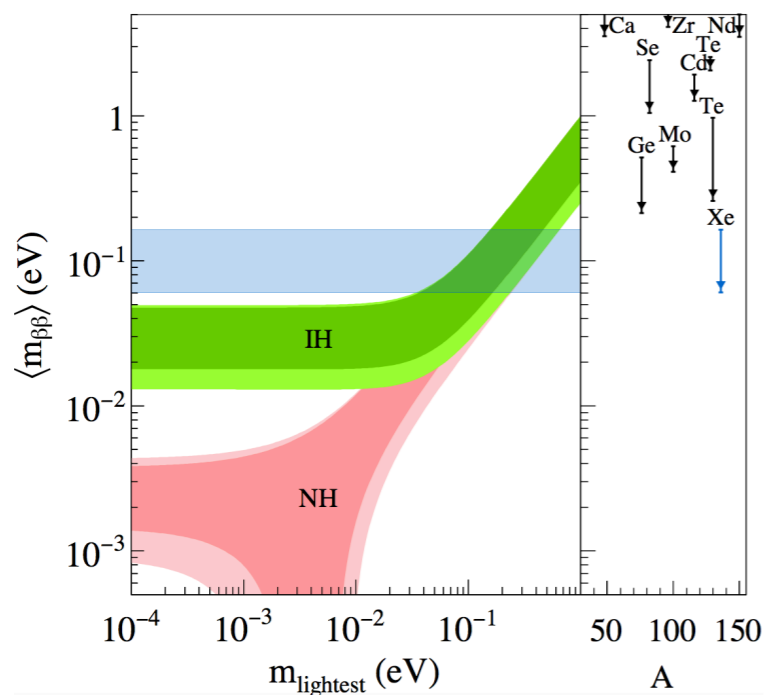


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+ ??

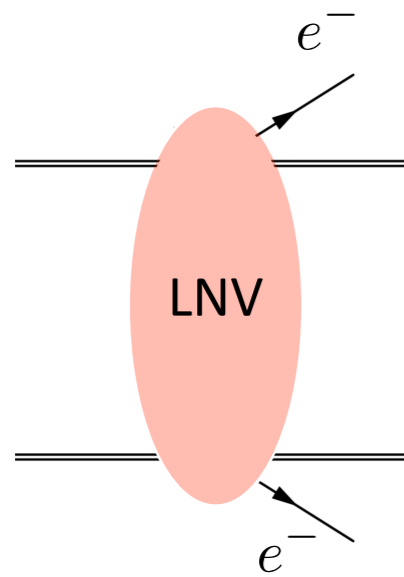
Well-known Majorana mass mechanism



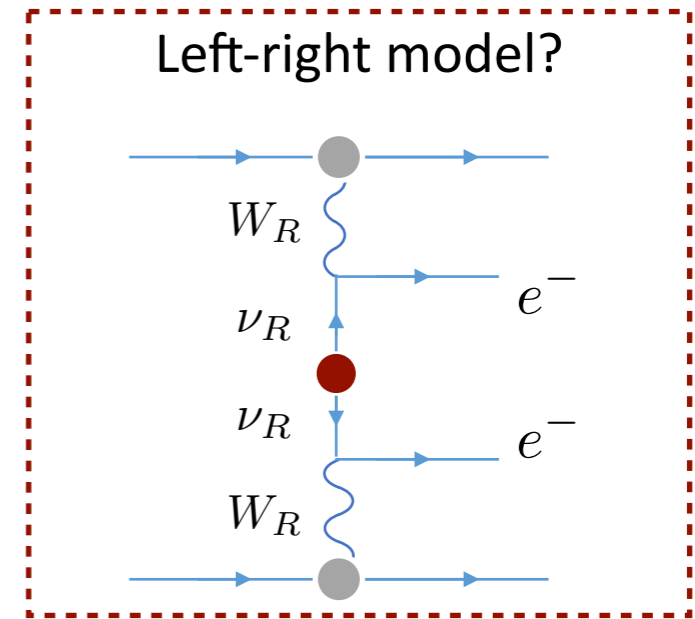
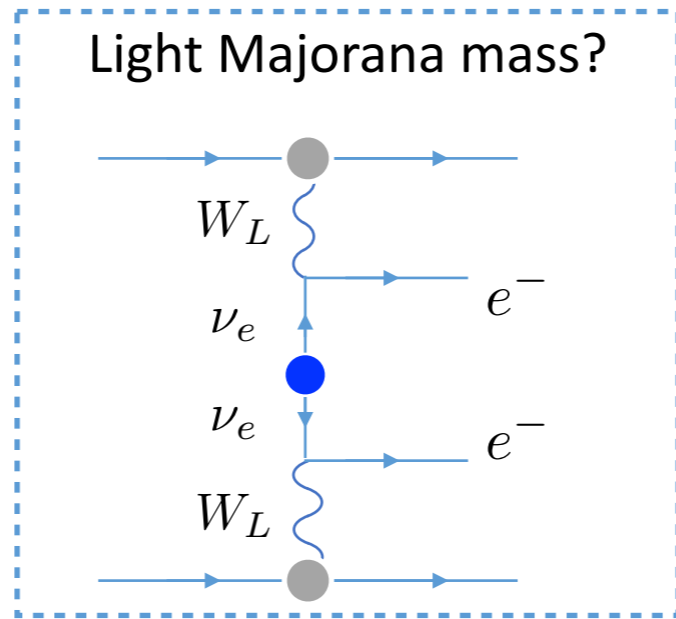
- Implications for the mass hierarchy

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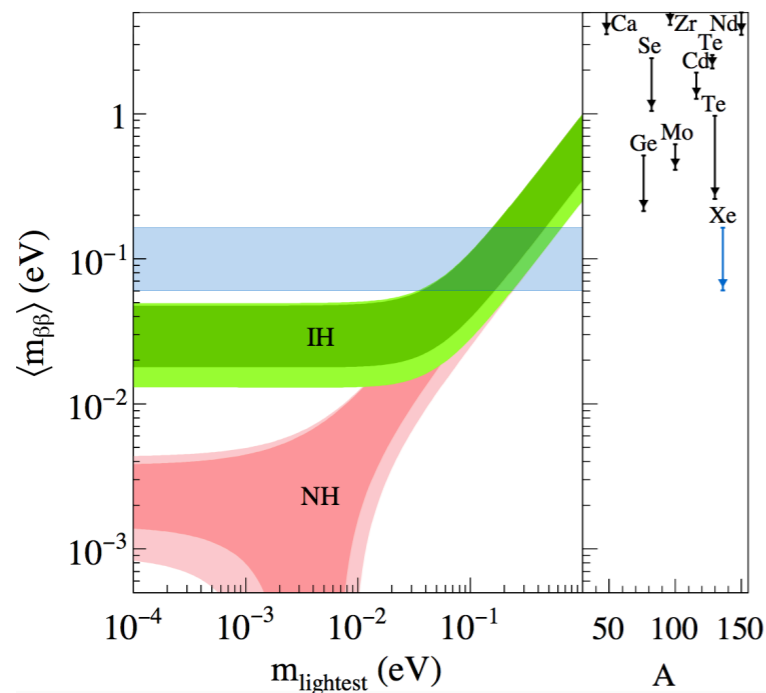
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Well-known Majorana mass mechanism

BSM mechanisms

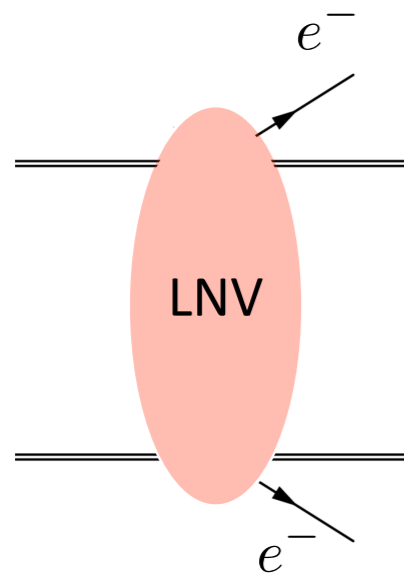


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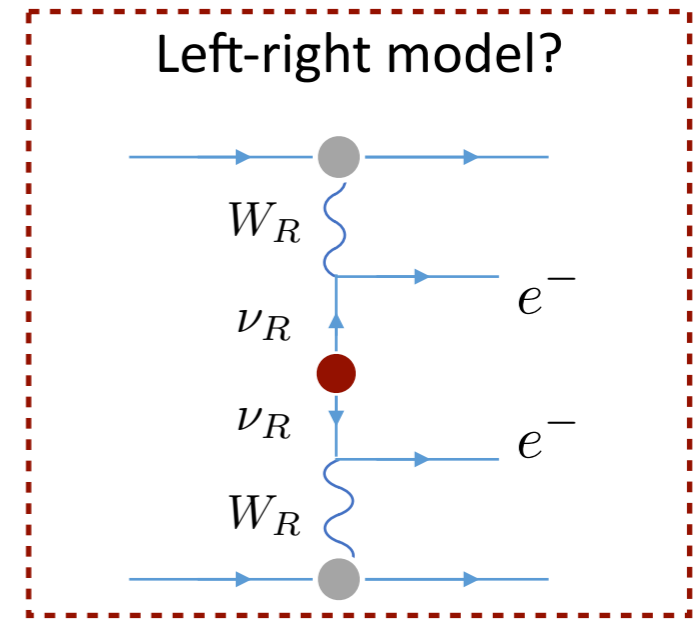
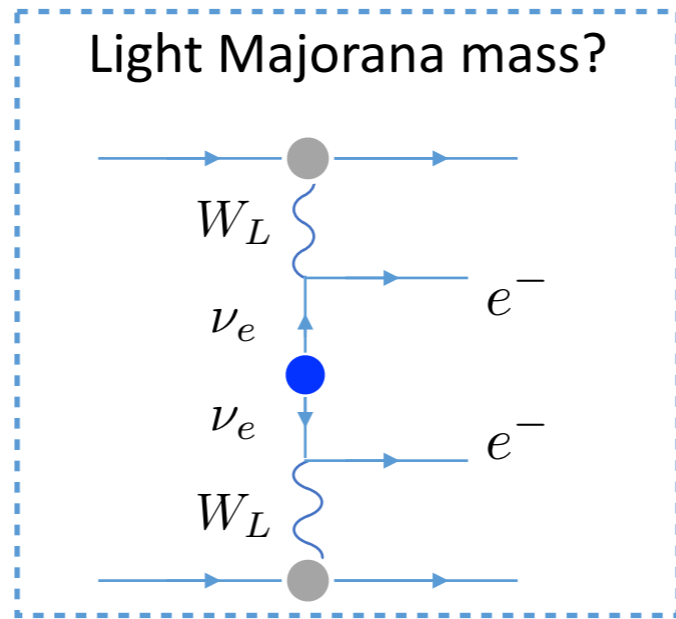
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 - Sterile neutrinos
 - Left-right model
 - Leptoquarks...

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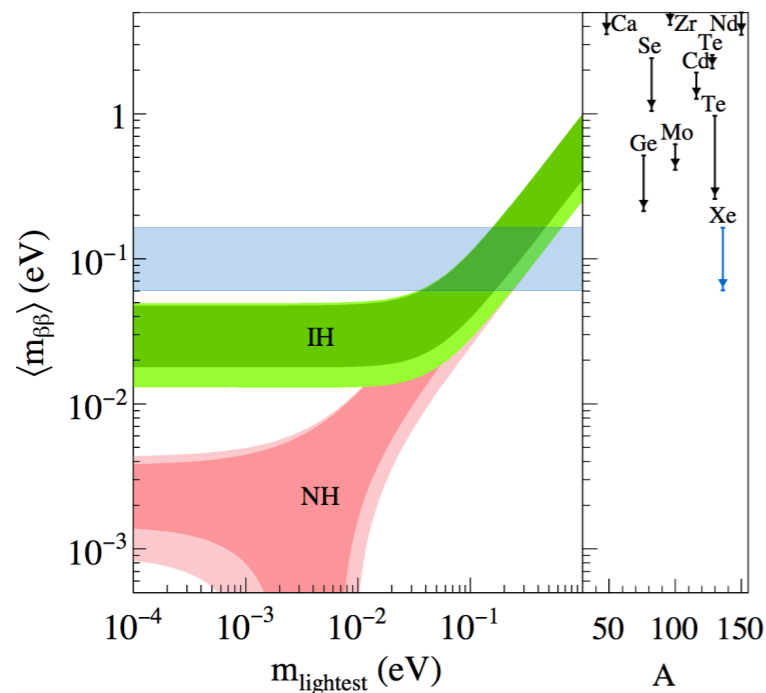
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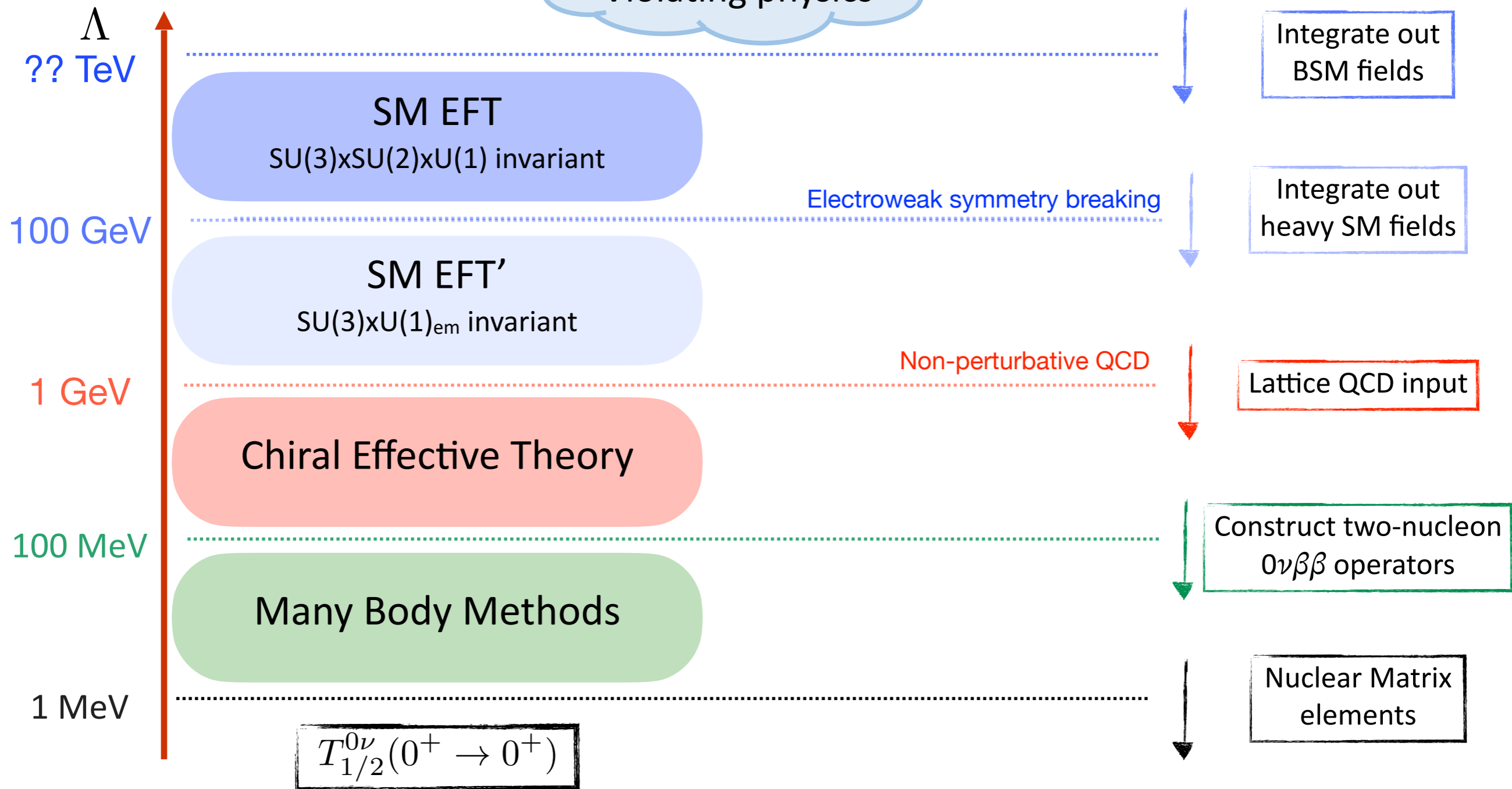
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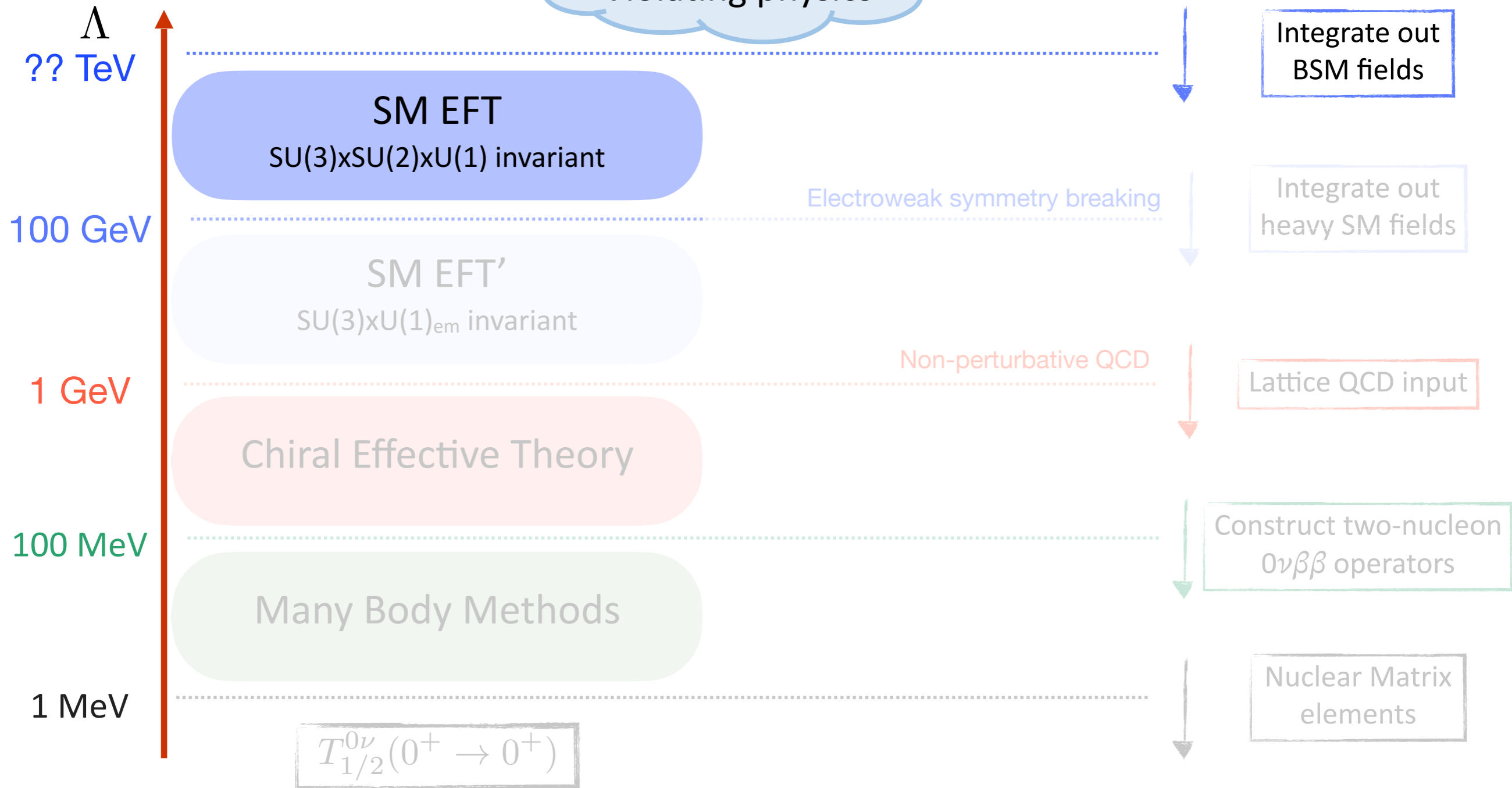
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- Many possible scenarios
 - Sterile neutrinos
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- How to describe all LNV sources systematically?

Outline



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Effective Field Theory

Heavy $\Delta L = 2$ physics

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \frac{c_i^{(5)}}{\Lambda} O_i^{(5)} + \frac{c_i^{(7)}}{\Lambda^3} O_i^{(7)} + \frac{c_i^{(9)}}{\Lambda^5} O_i^{(9)} + \dots$$

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- 12 $\Delta L=2$ operators

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- Consider subset of operators

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Liao and Ma '20; Li et al '20;

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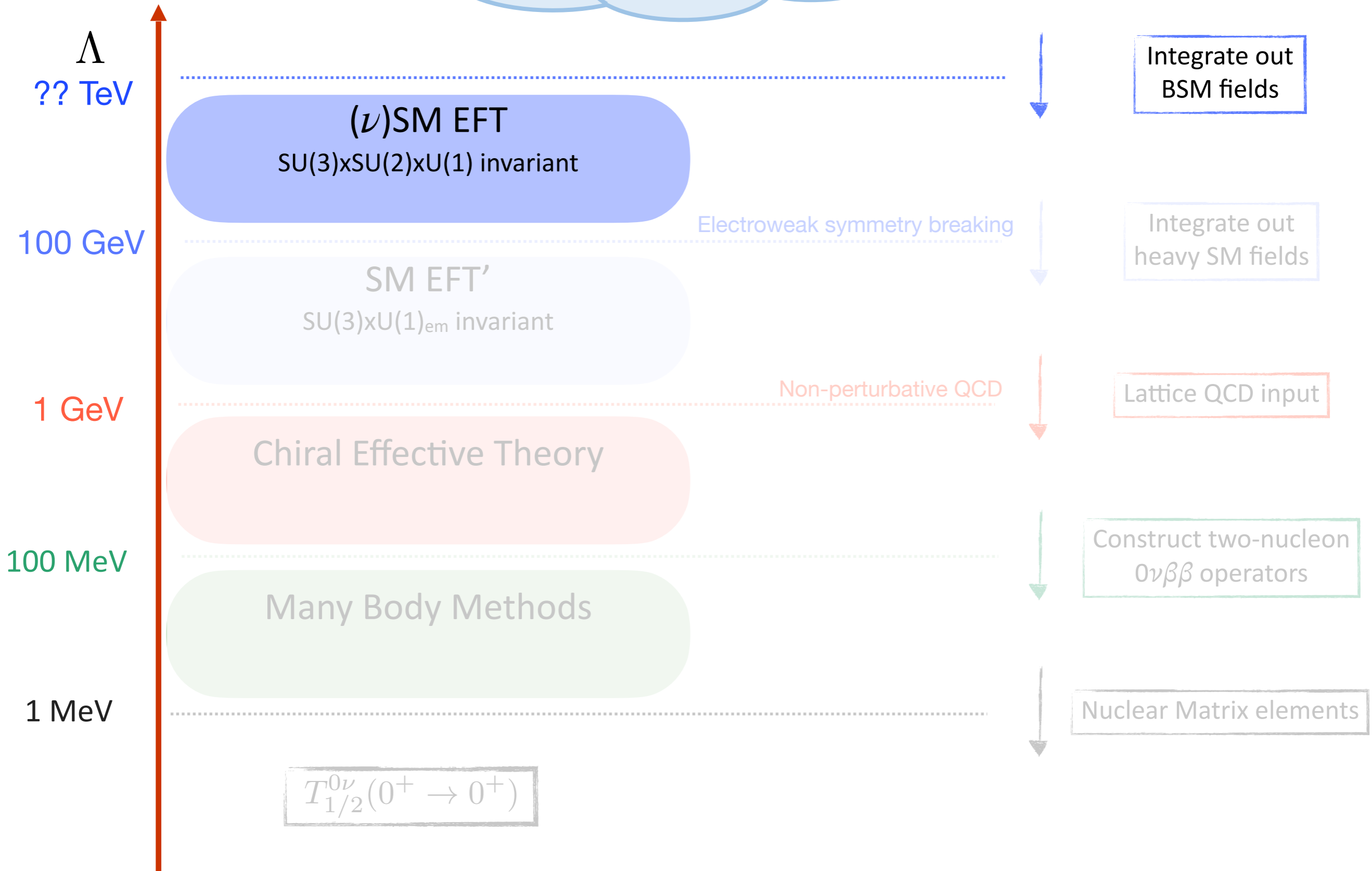
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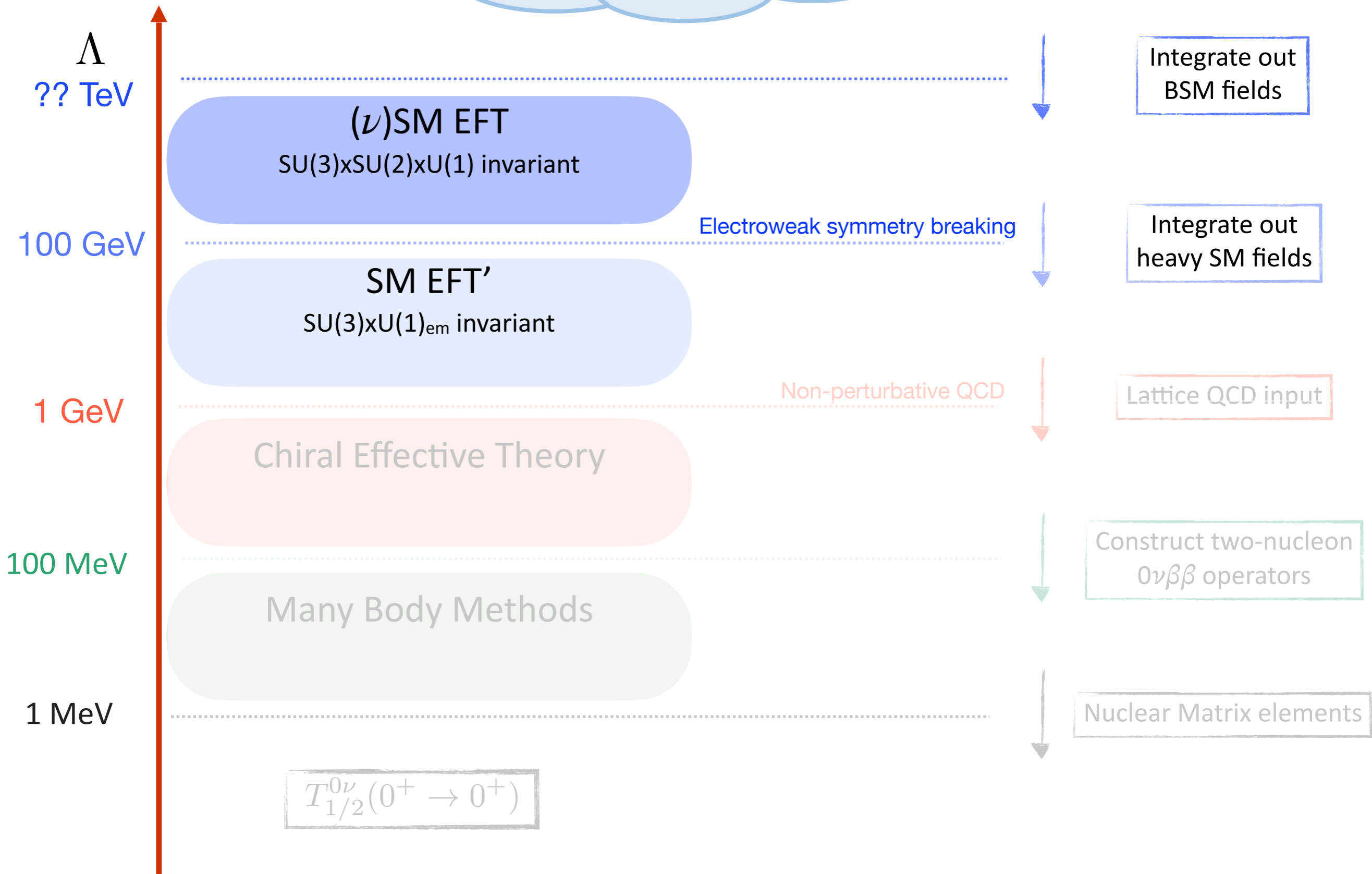
Outline

Lepton-number violation:
seesaw, left-right model, leptoquarks,...



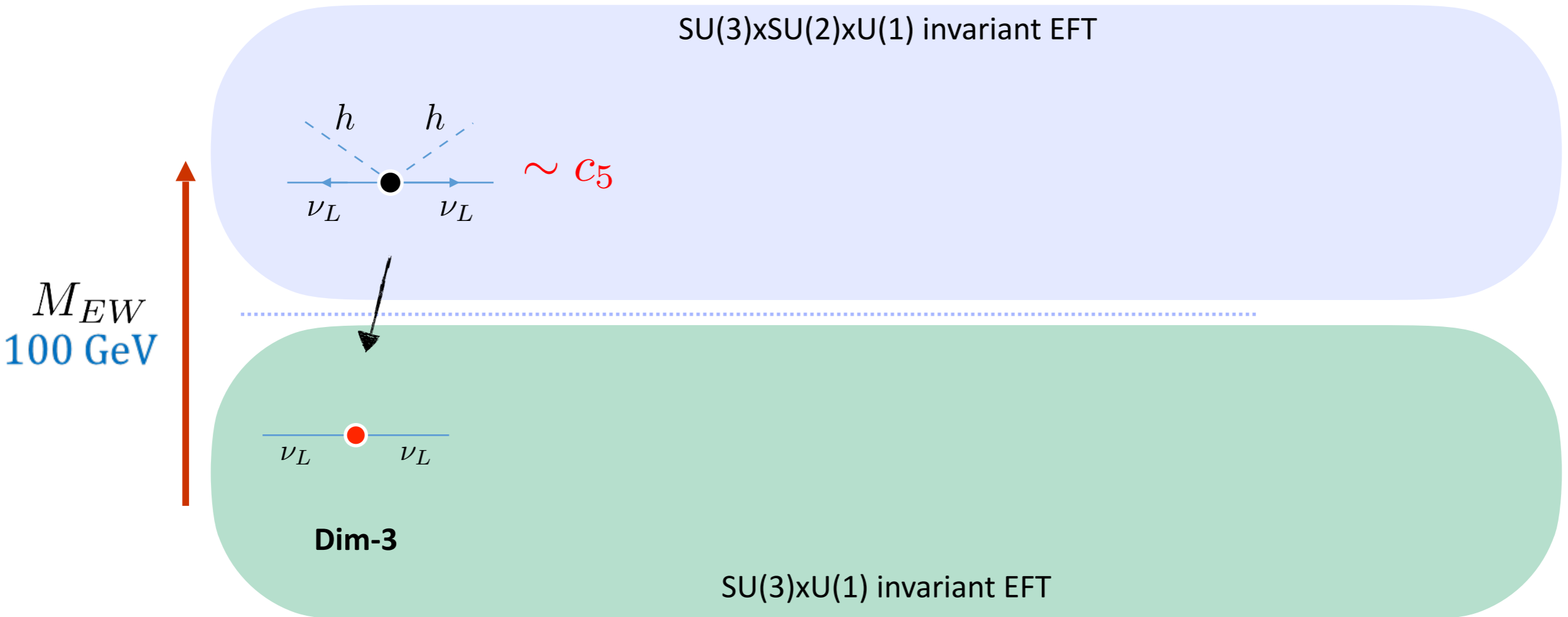
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Low-energy operators

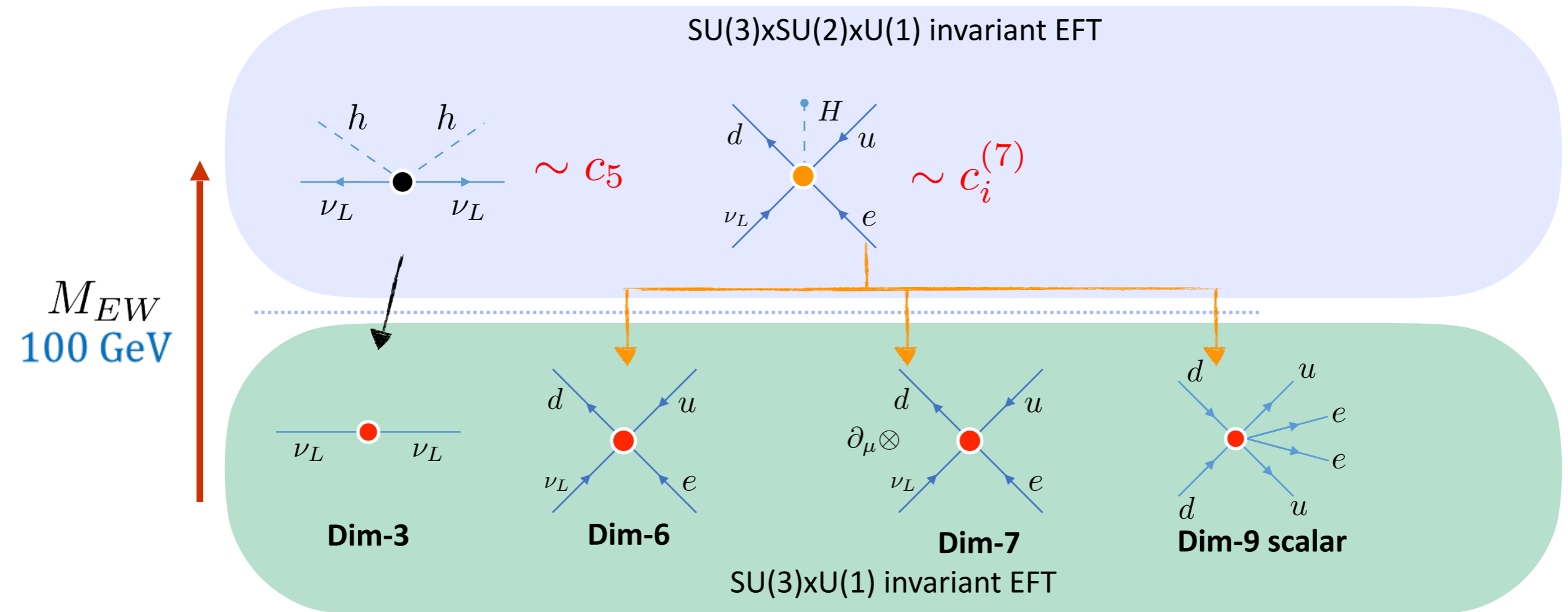
At/below the weak scale*



* very similar for operators involving ν_R

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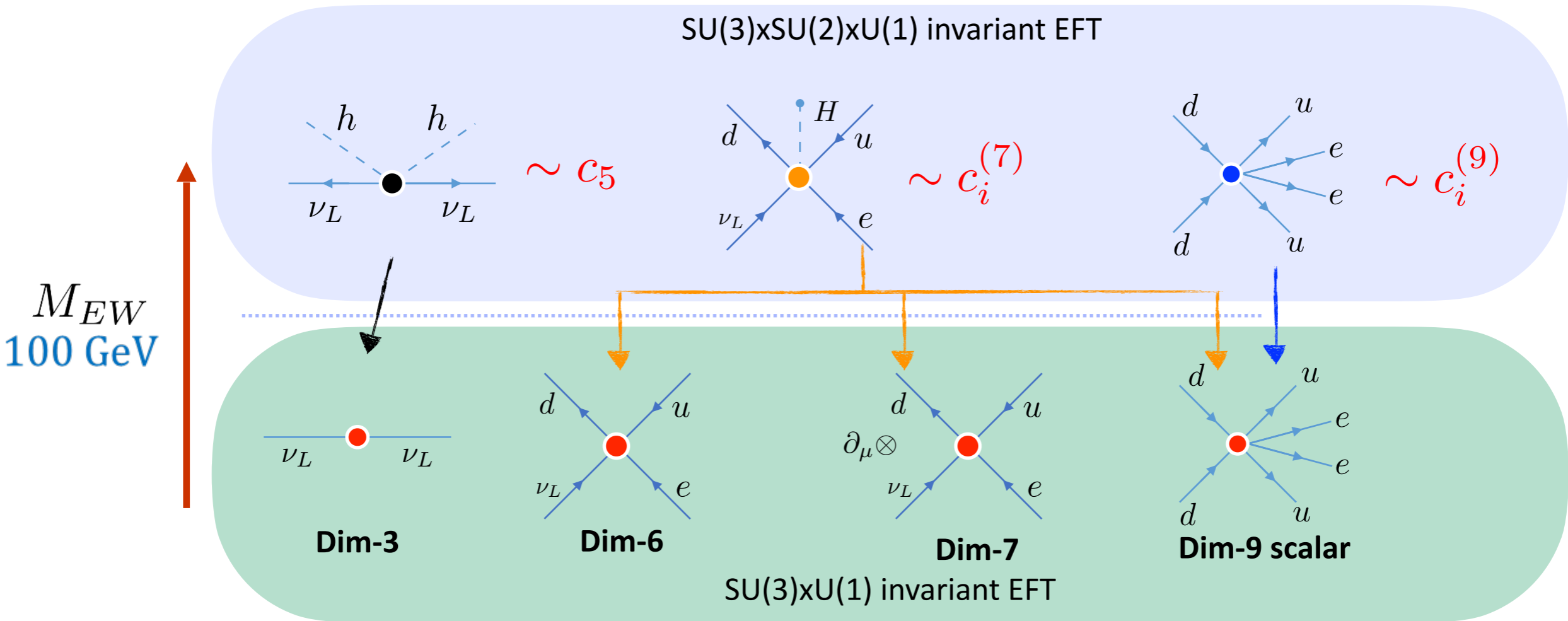
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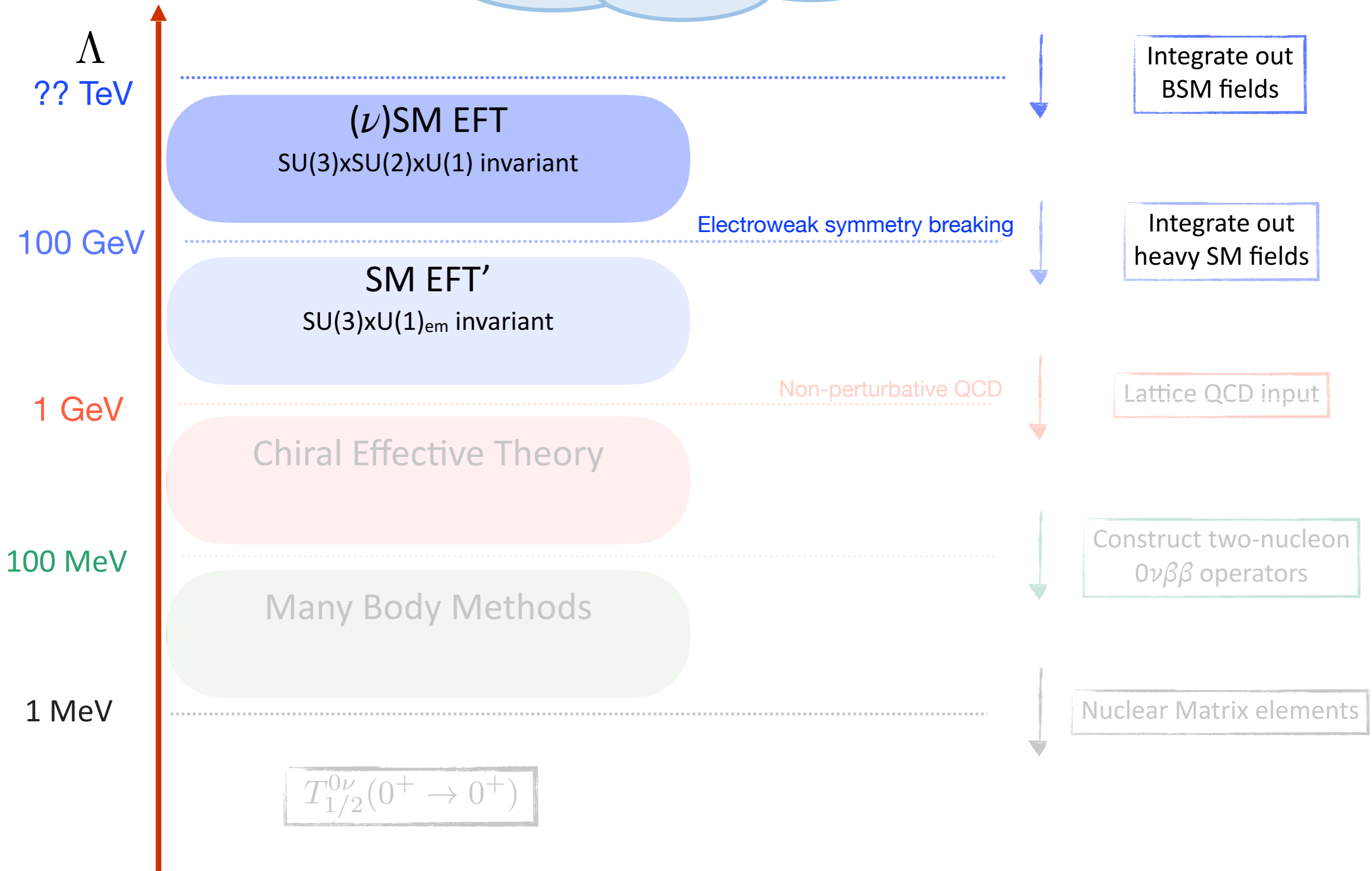
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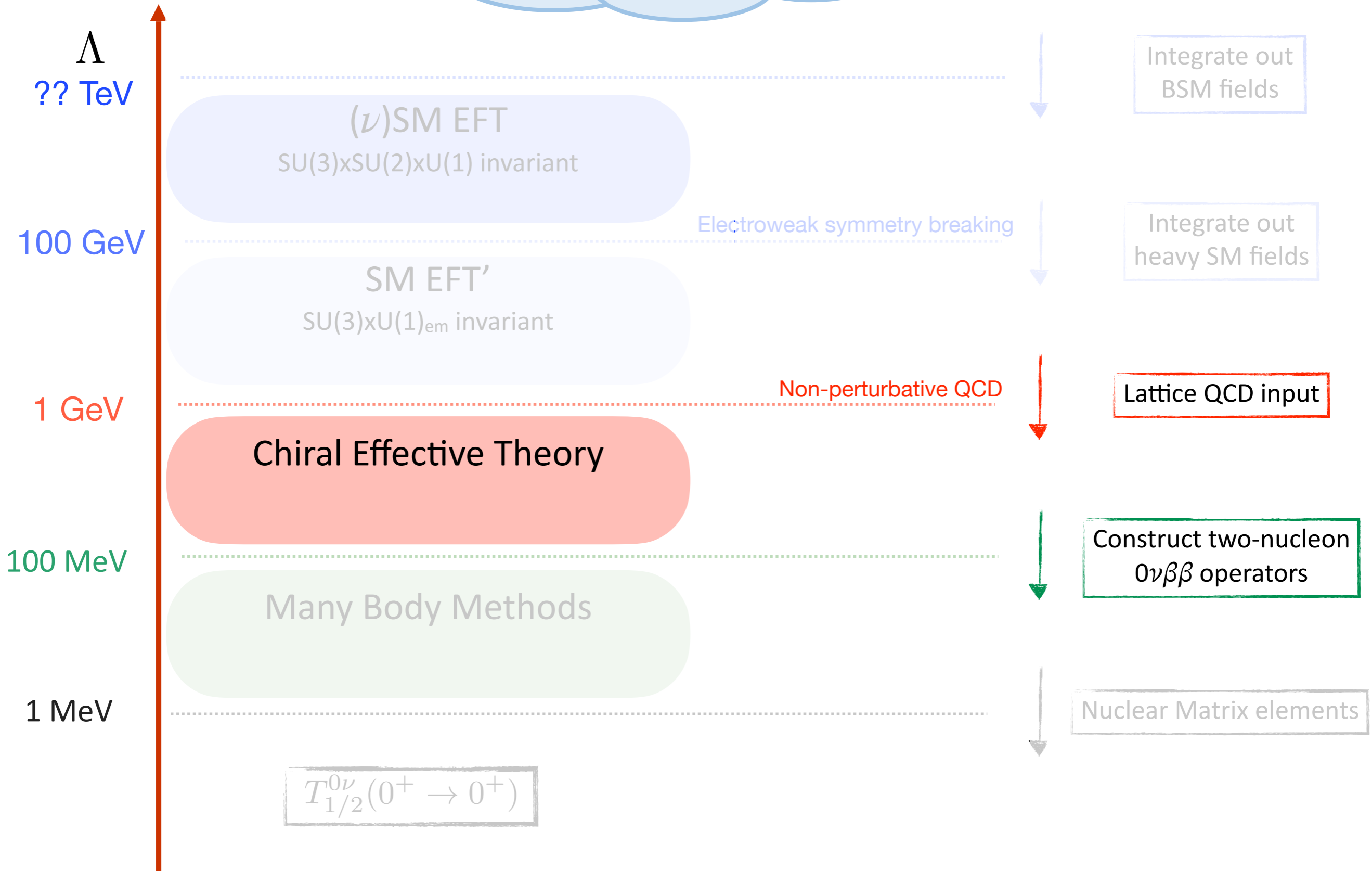
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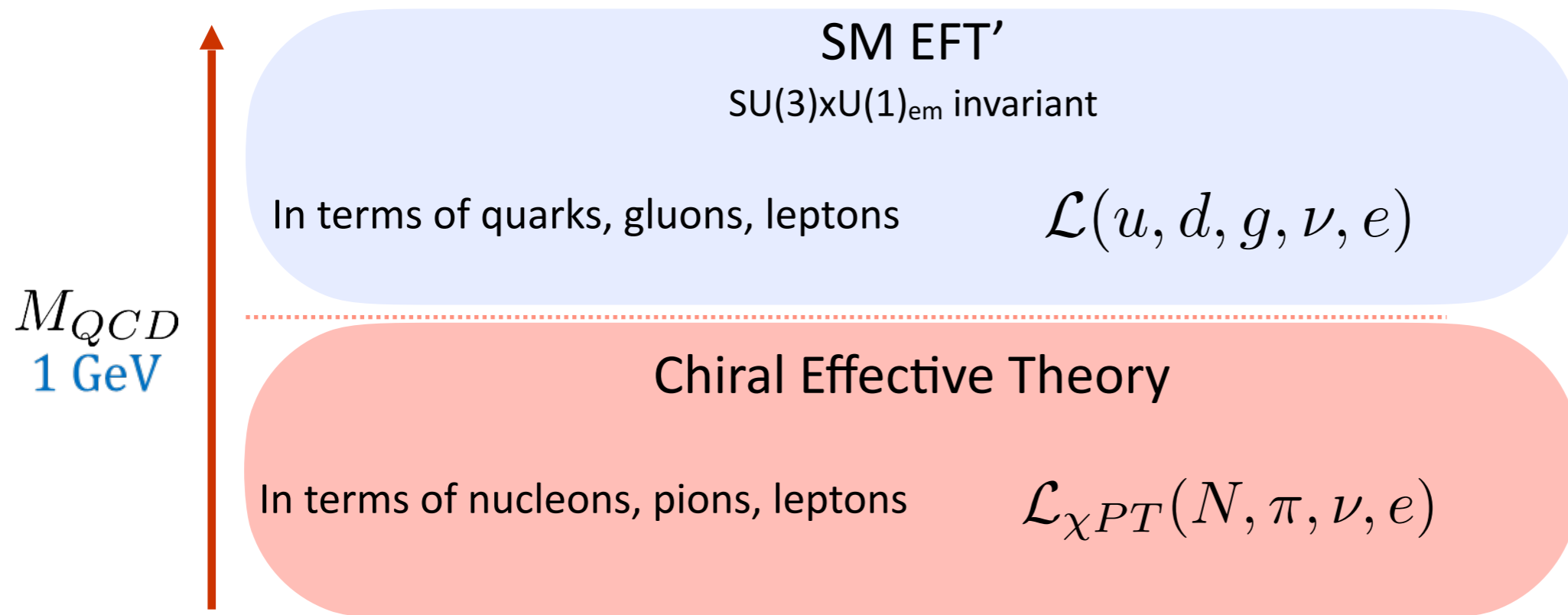


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Matching to Chiral EFT



Form of operators determined by chiral symmetry

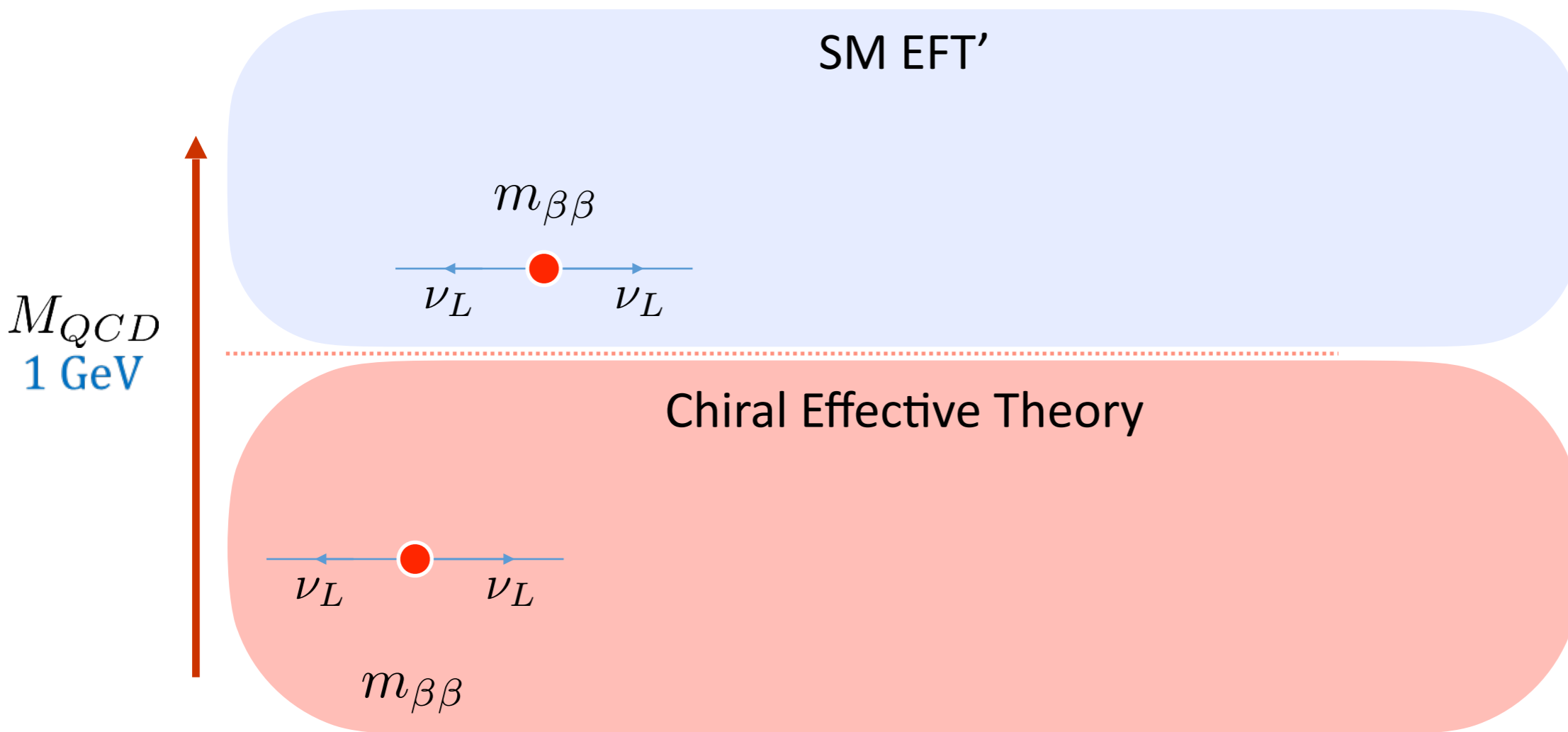
The operators come with unknown constants (LECs)

Need a power-counting scheme

- Often used: Weinberg counting / Naive dimensional analysis (NDA)

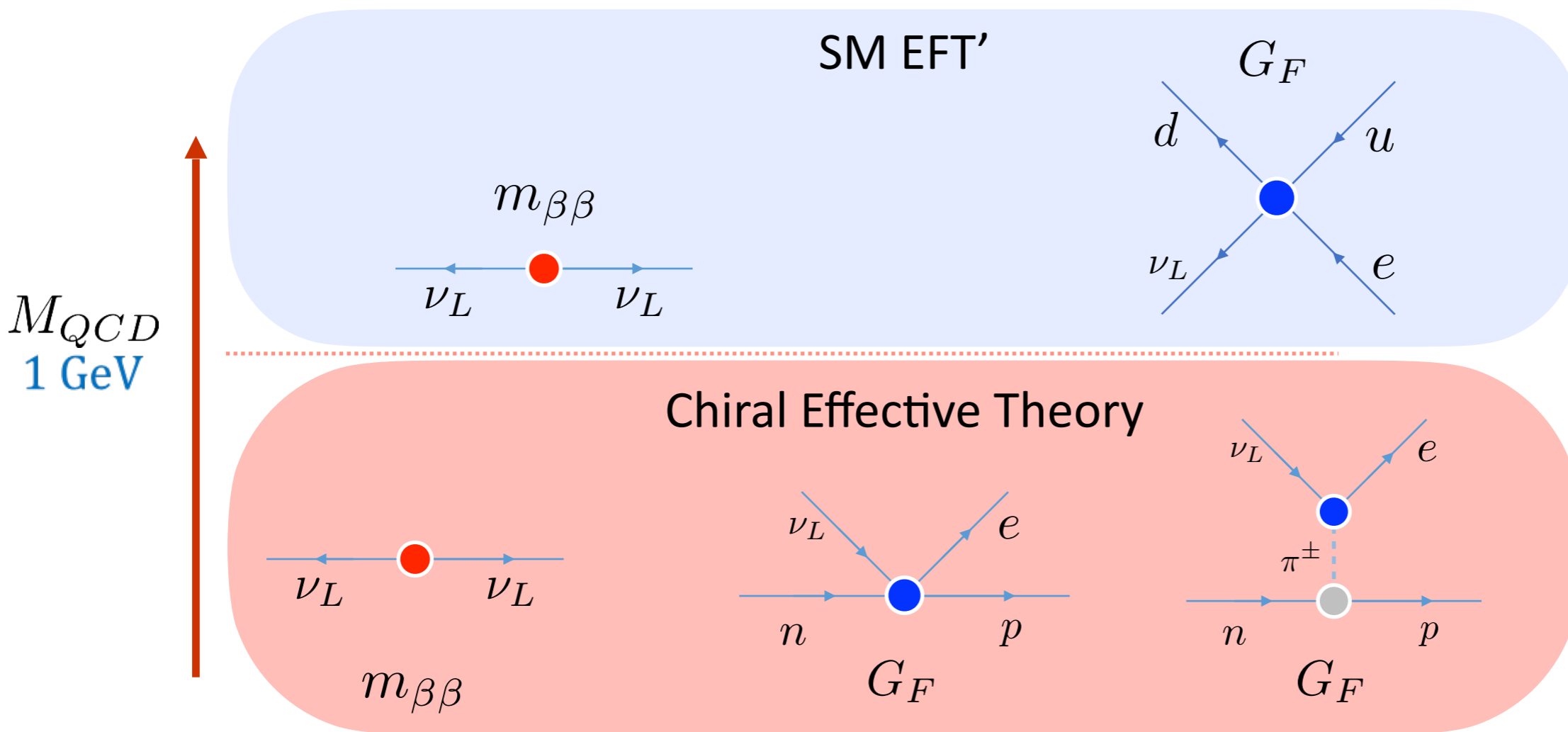
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Example: dimension-3 LNV



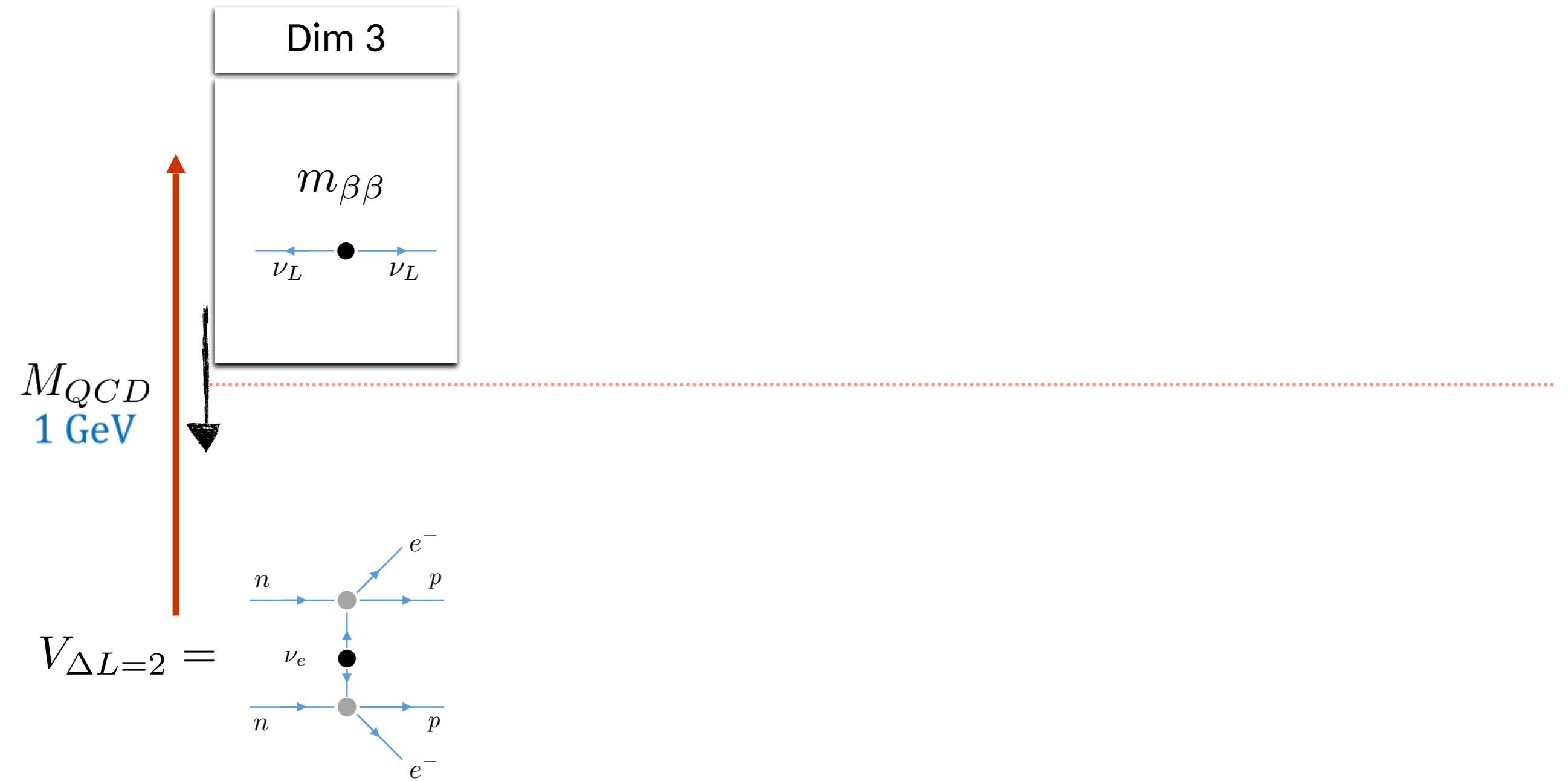
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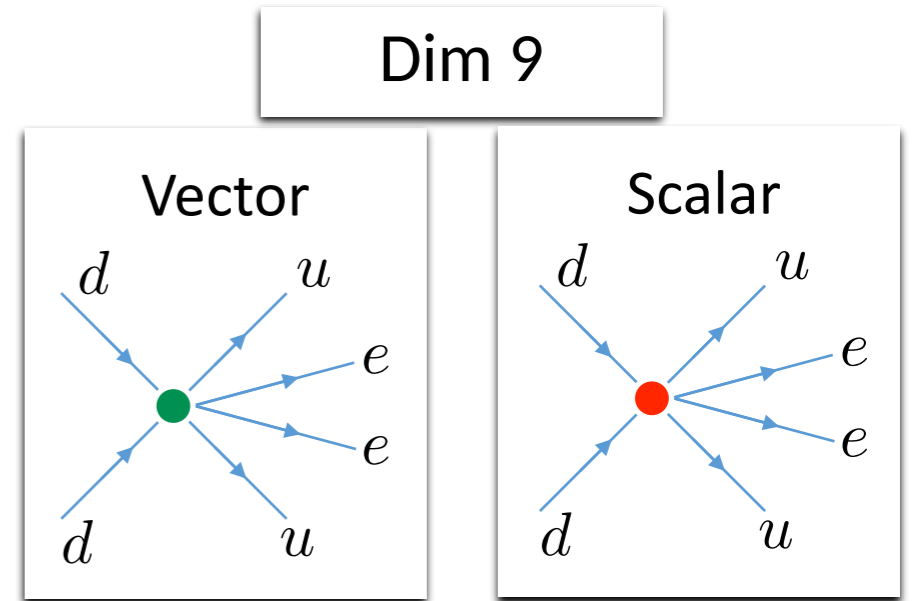
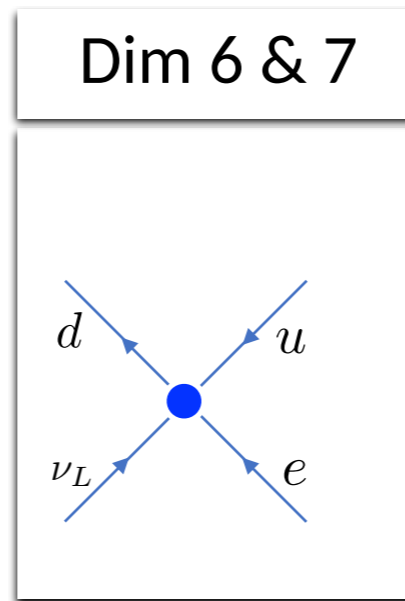
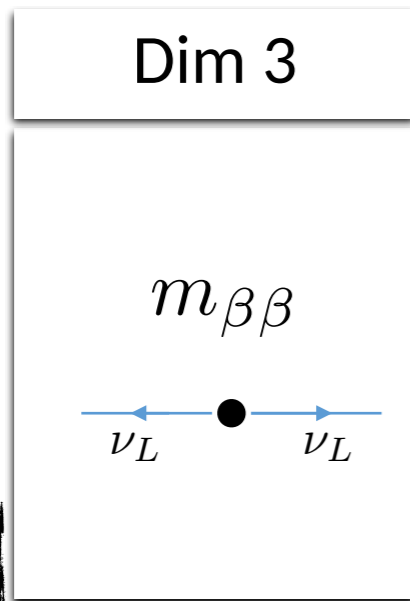


- At LO in Weinberg counting, only need the nucleon one-body currents
 - All needed low-energy constants are known

Chiral EFT

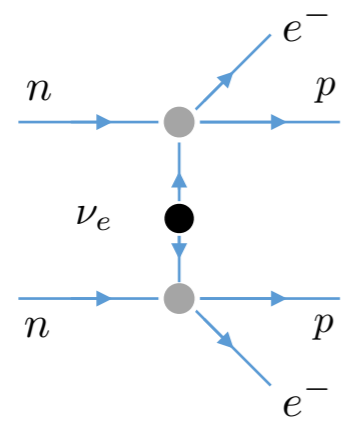


Chiral EFT



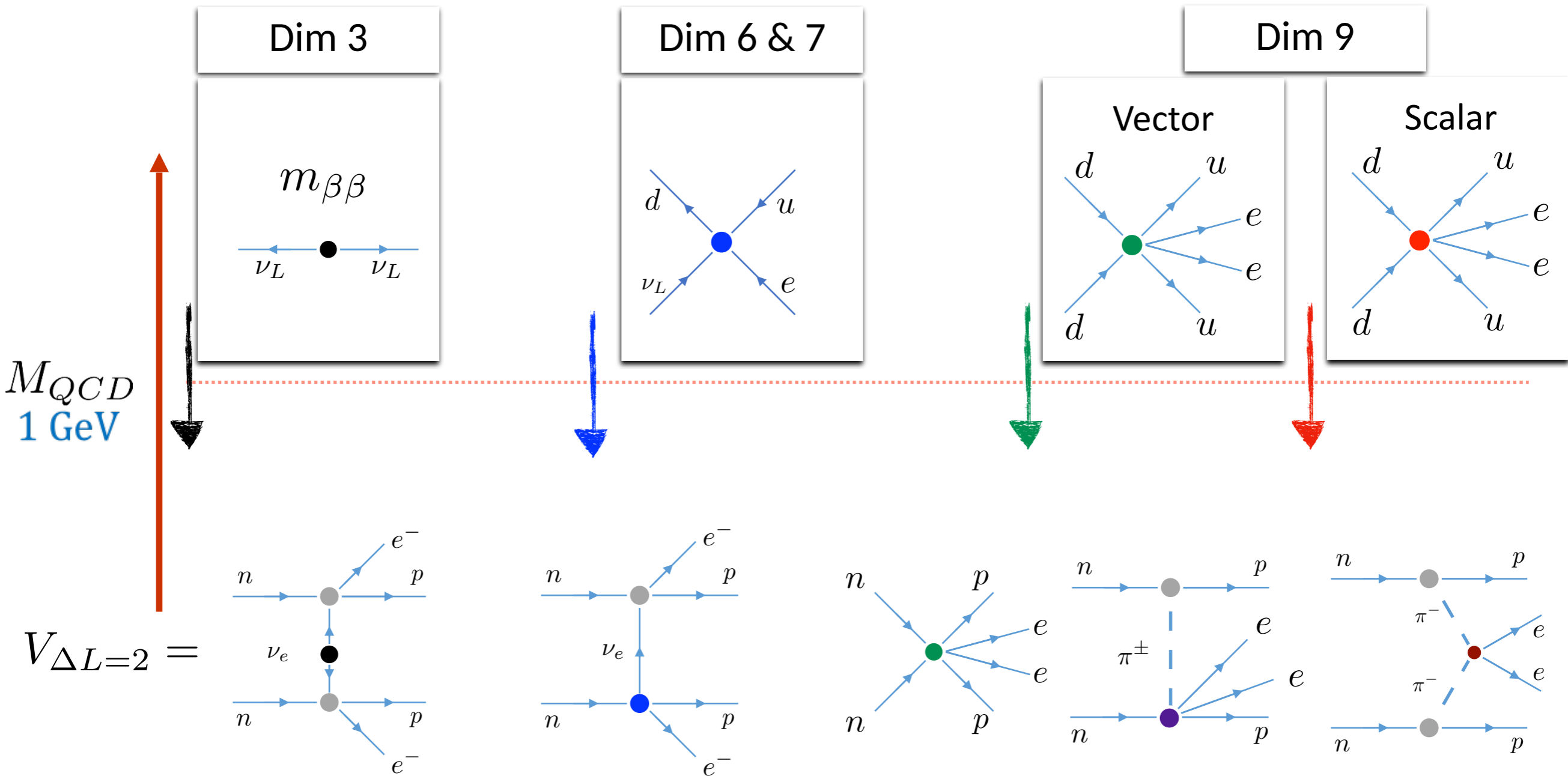
M_{QCD}
1 GeV

$V_{\Delta L=2} =$



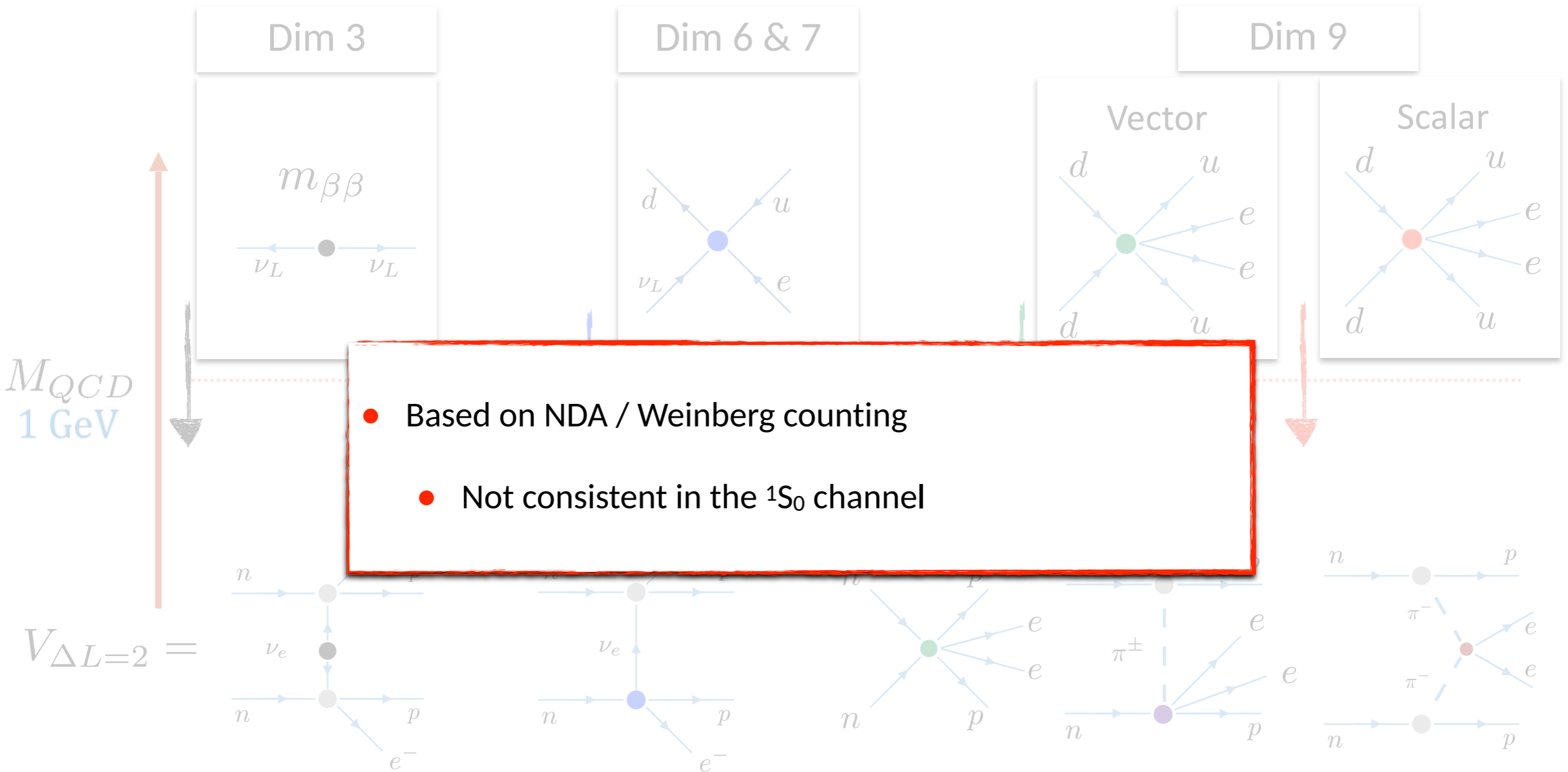
- Contributions of dimension-6,7,9 operators

Chiral EFT



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 - Give additional interactions and LECs
 - LECs for the **nucleon currents** and $\pi\pi$ interactions are partially known

Chiral EFT



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Checking the power counting

Dimension-3

Check that $\mathcal{A}(nn \rightarrow ppee)$ is finite

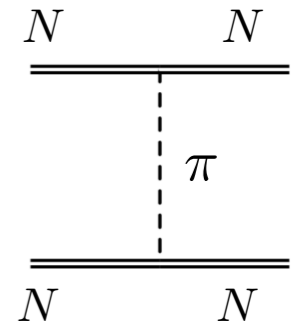
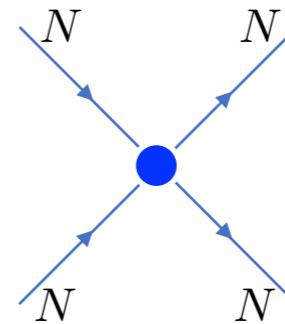
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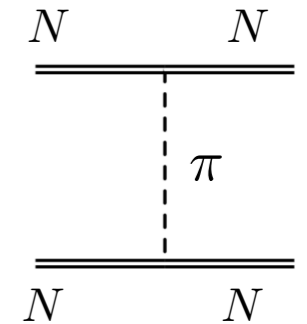
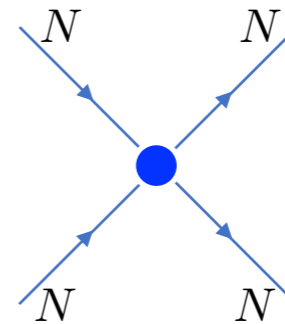
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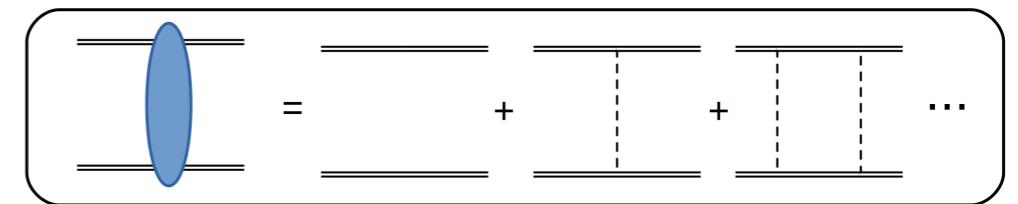
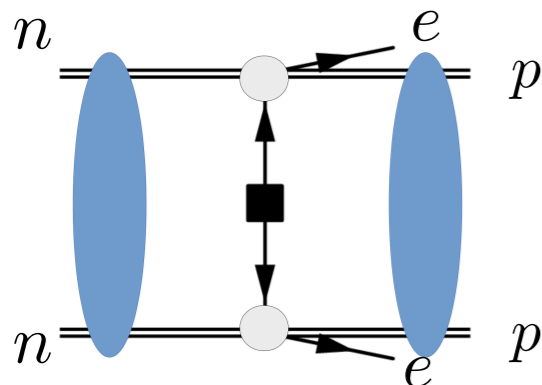
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Dress the $\Delta L=2$ potential with (renormalized) strong interactions:



✓ finite

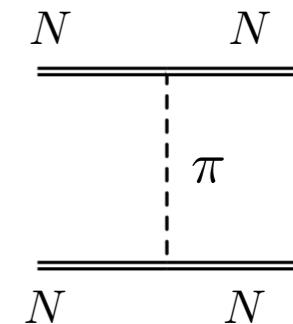
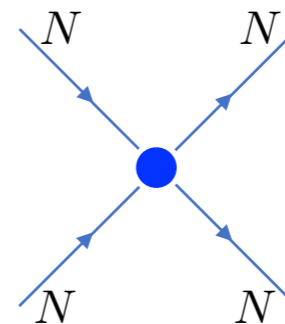
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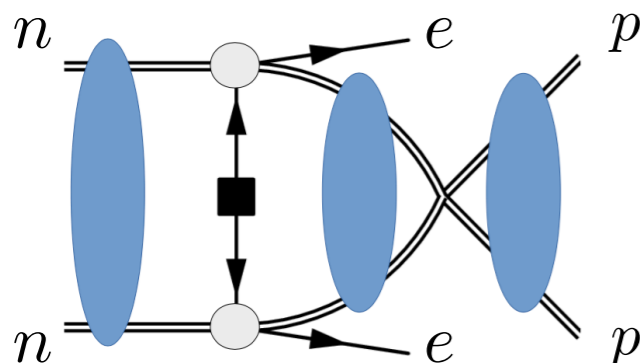
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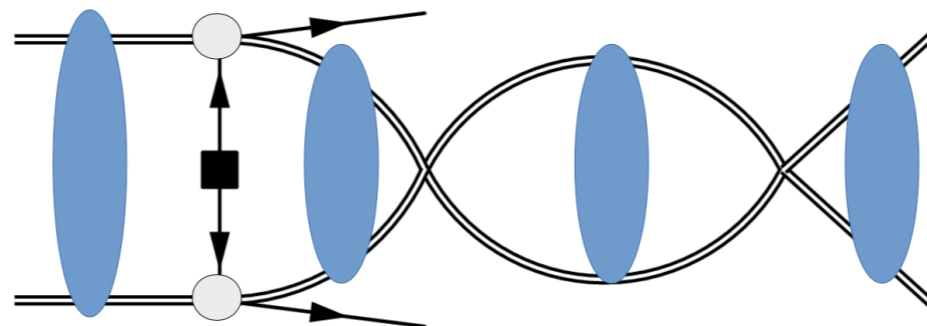
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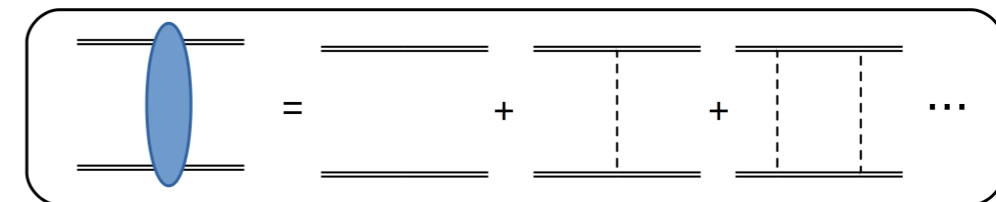


+



+

...



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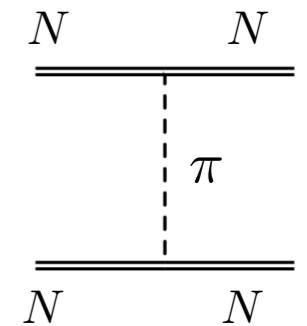
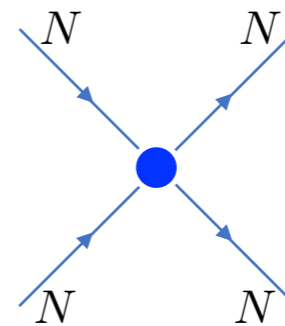
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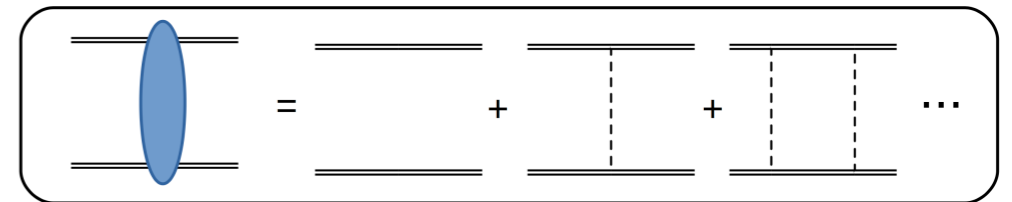
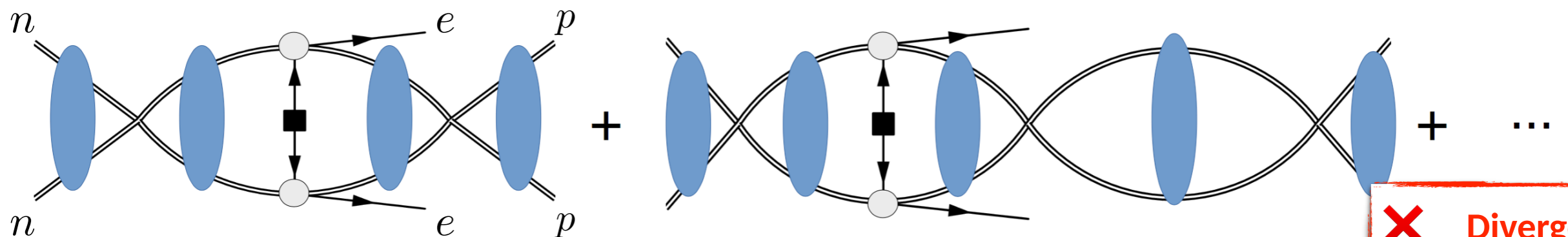
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✗ Divergent

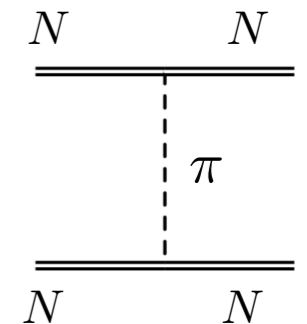
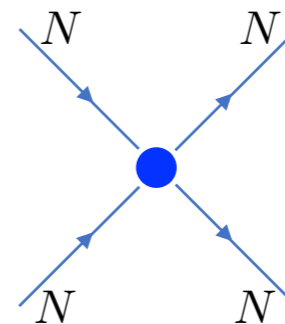
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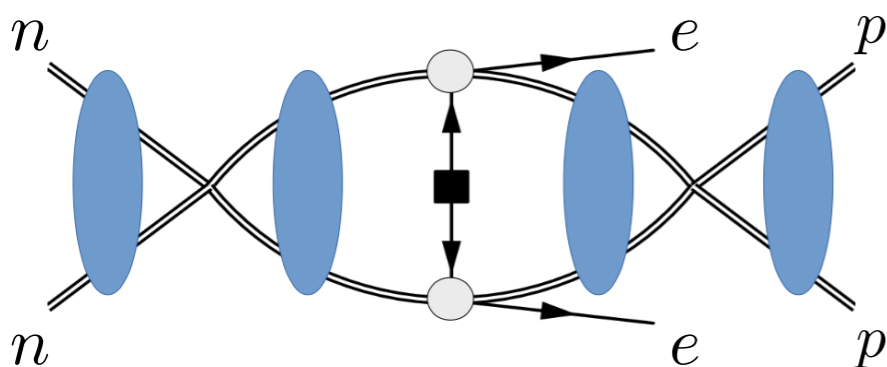
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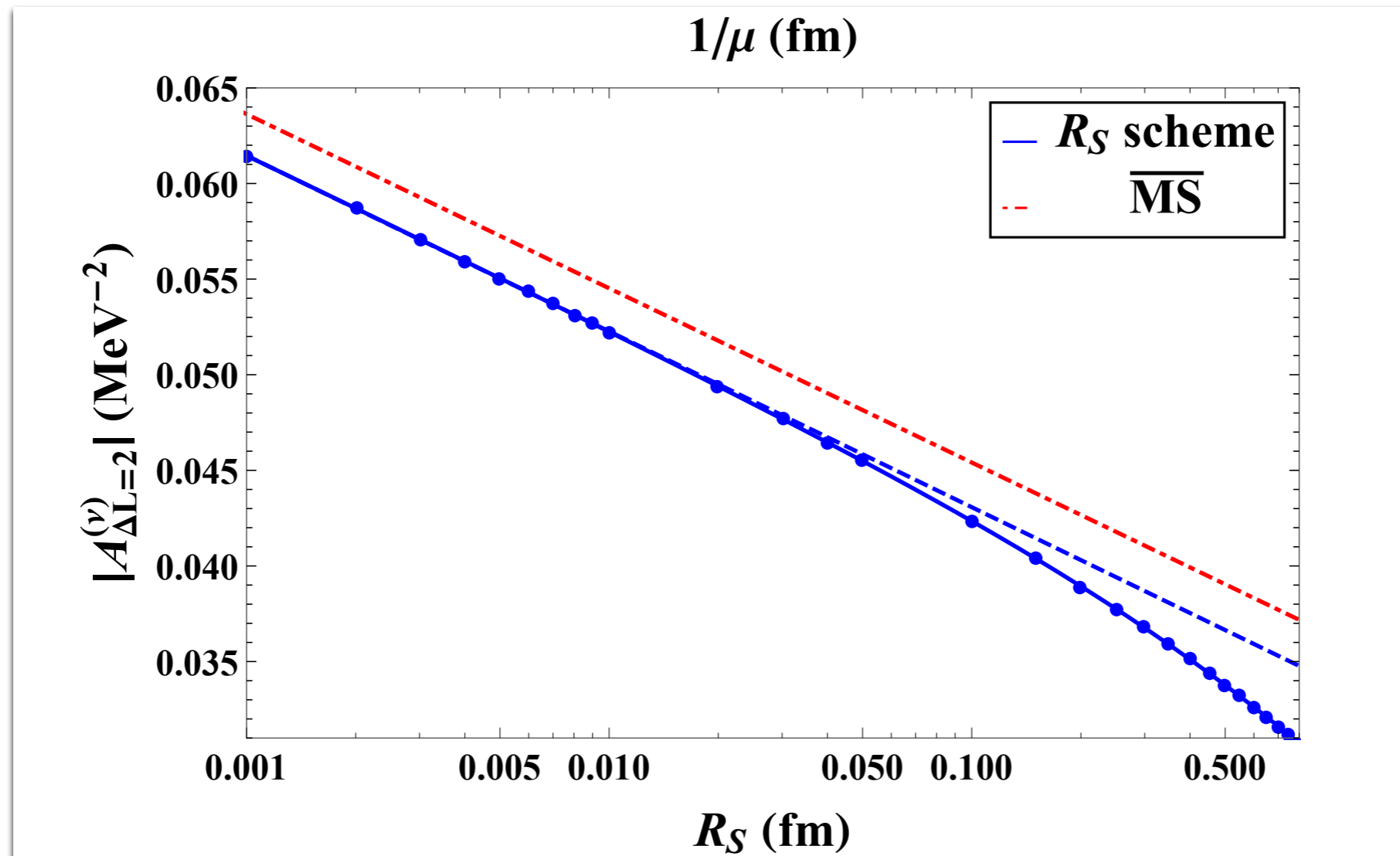
In MS-bar:



$$= - \left(\frac{m_N}{4\pi} \right)^2 (1 + 2g_A^2) \frac{1}{2} \left(\log \frac{\mu^2}{-(|\mathbf{p}| + |\mathbf{p}'|)^2 + i0^+} + 1 \right) + \text{finite}$$

Regulator dependent

Numerical results



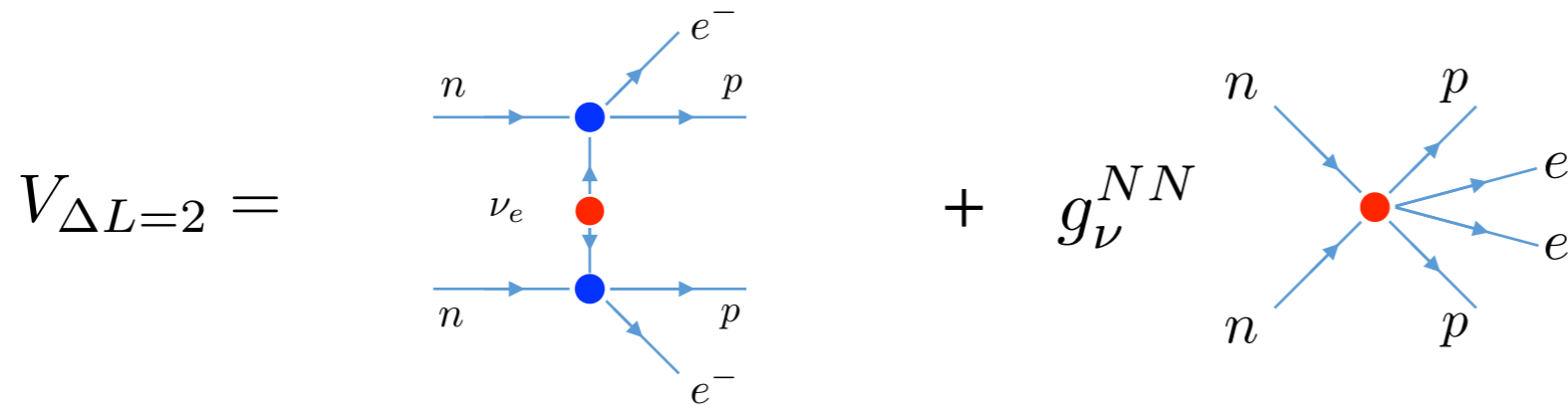
- Amplitudes obtained using
 - MS-bar
 - Coordinate-space cut-off

• Clear μ or R_S dependence

$$\tilde{C} \delta^{(3)}(\mathbf{r}) \rightarrow \frac{\tilde{C}(R_S)}{(\sqrt{\pi}R_S)^3} \exp\left(-\frac{r^2}{R_S^2}\right)$$

Need for a counter term

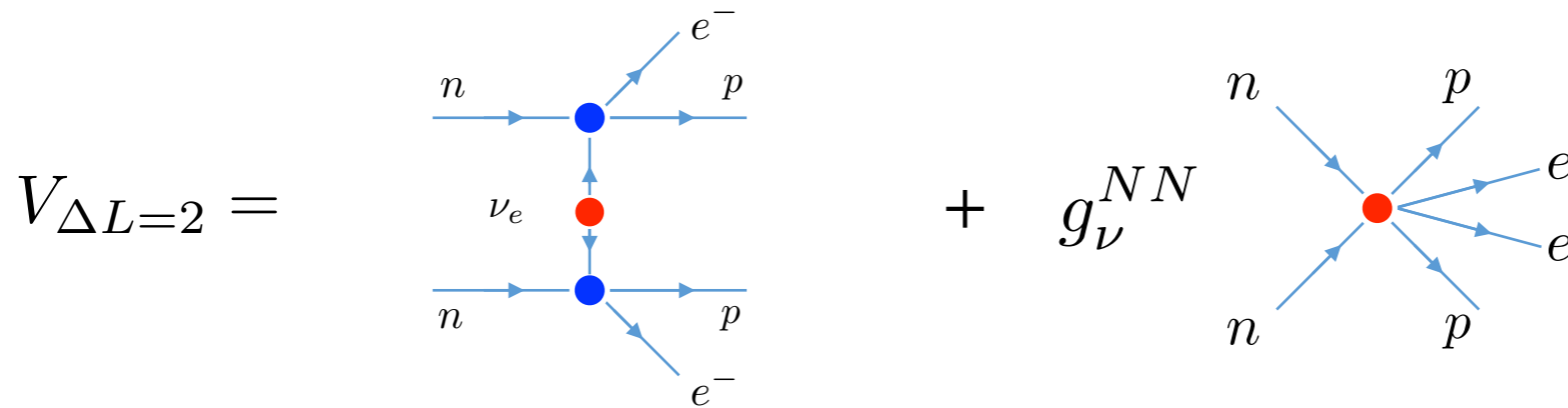
New interaction needed at leading order to get physical amplitudes:



$$\mathcal{L} \sim g_\nu^{NN} G_F^2 m_{\beta\beta} (\bar{N}\tau^+N)(\bar{N}\tau^+N) \bar{e}_L e_L^c$$

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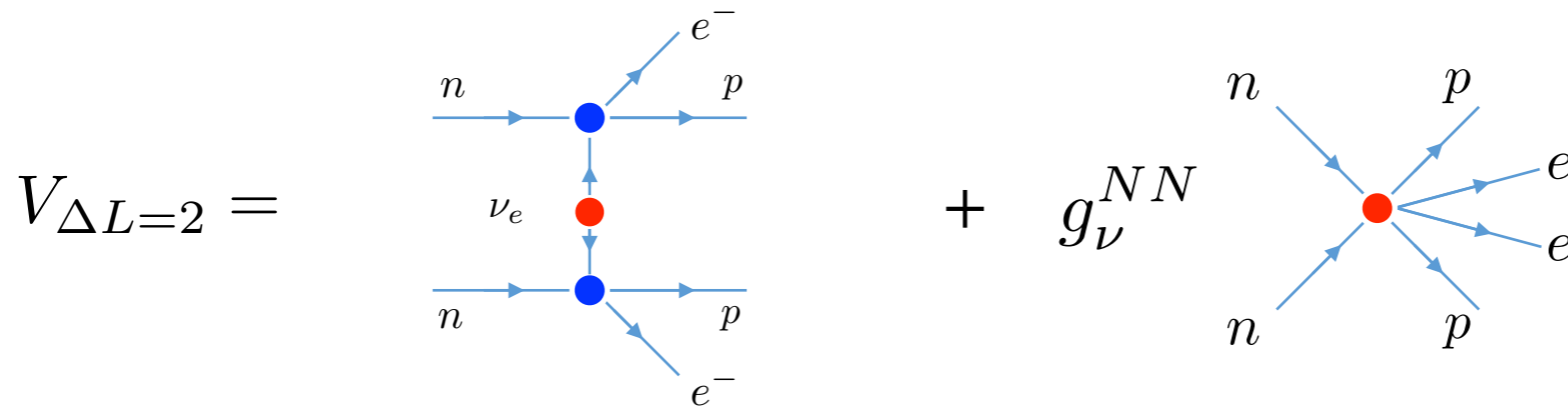
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 - Active area of research

Davoudi & Kadam, '20, '21

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[See backup](#)

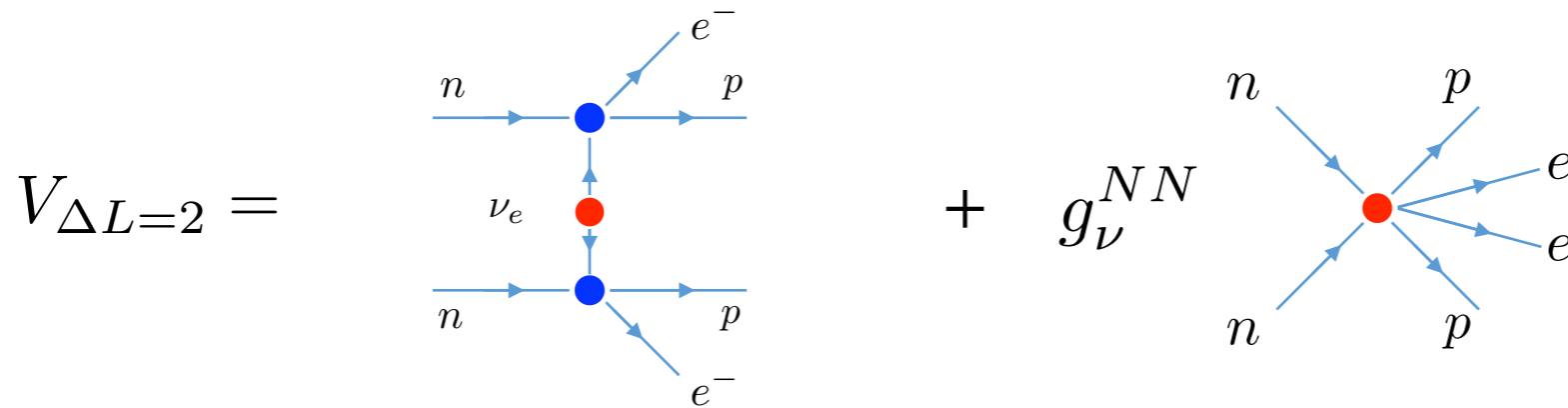
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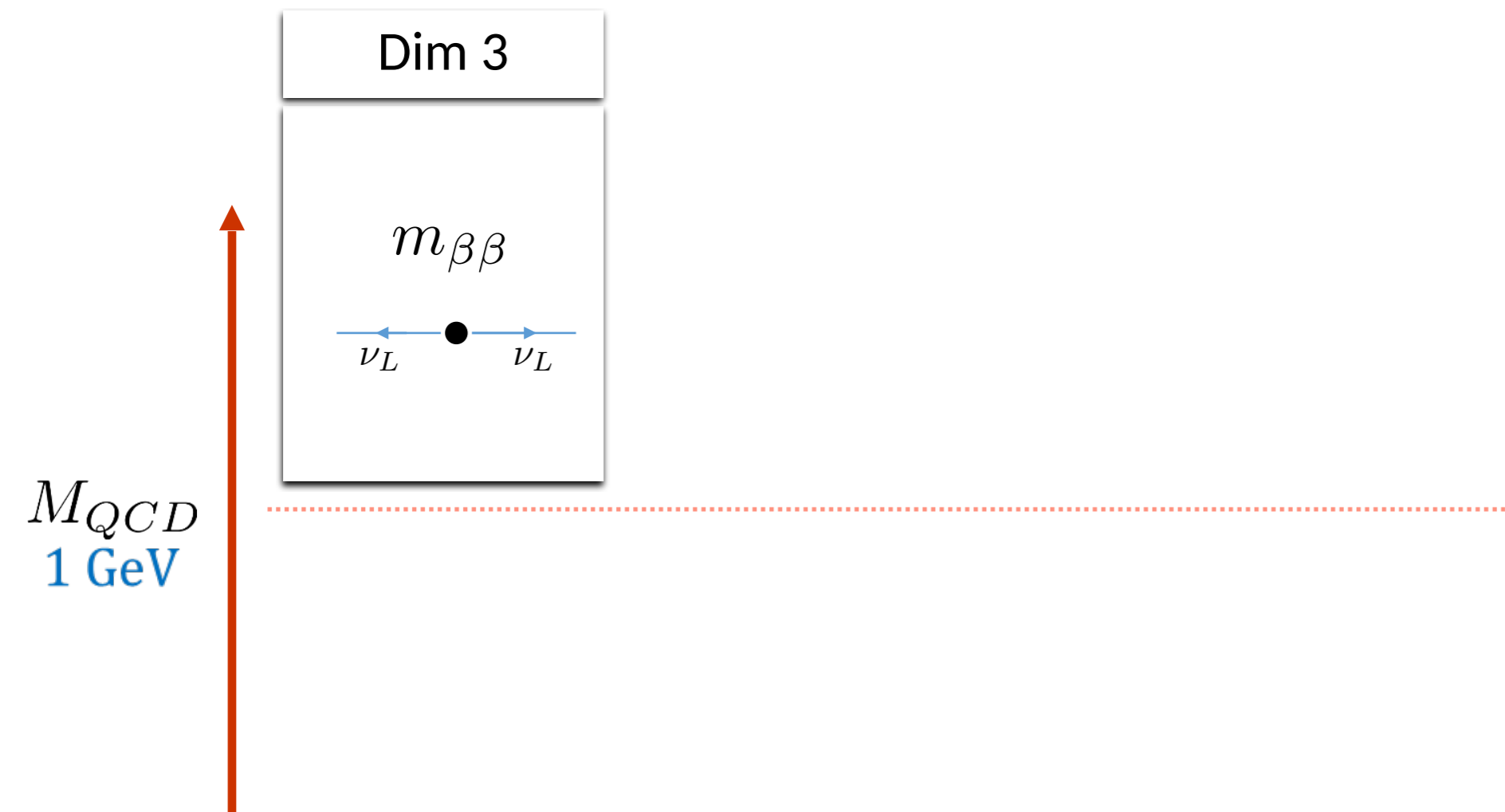
Richardson et al, '21

All give

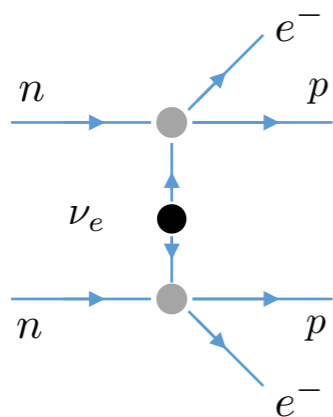
$$\tilde{g}_\nu^{NN} = \mathcal{O}(1)$$

Chiral EFT

'Non-Weinberg' counting

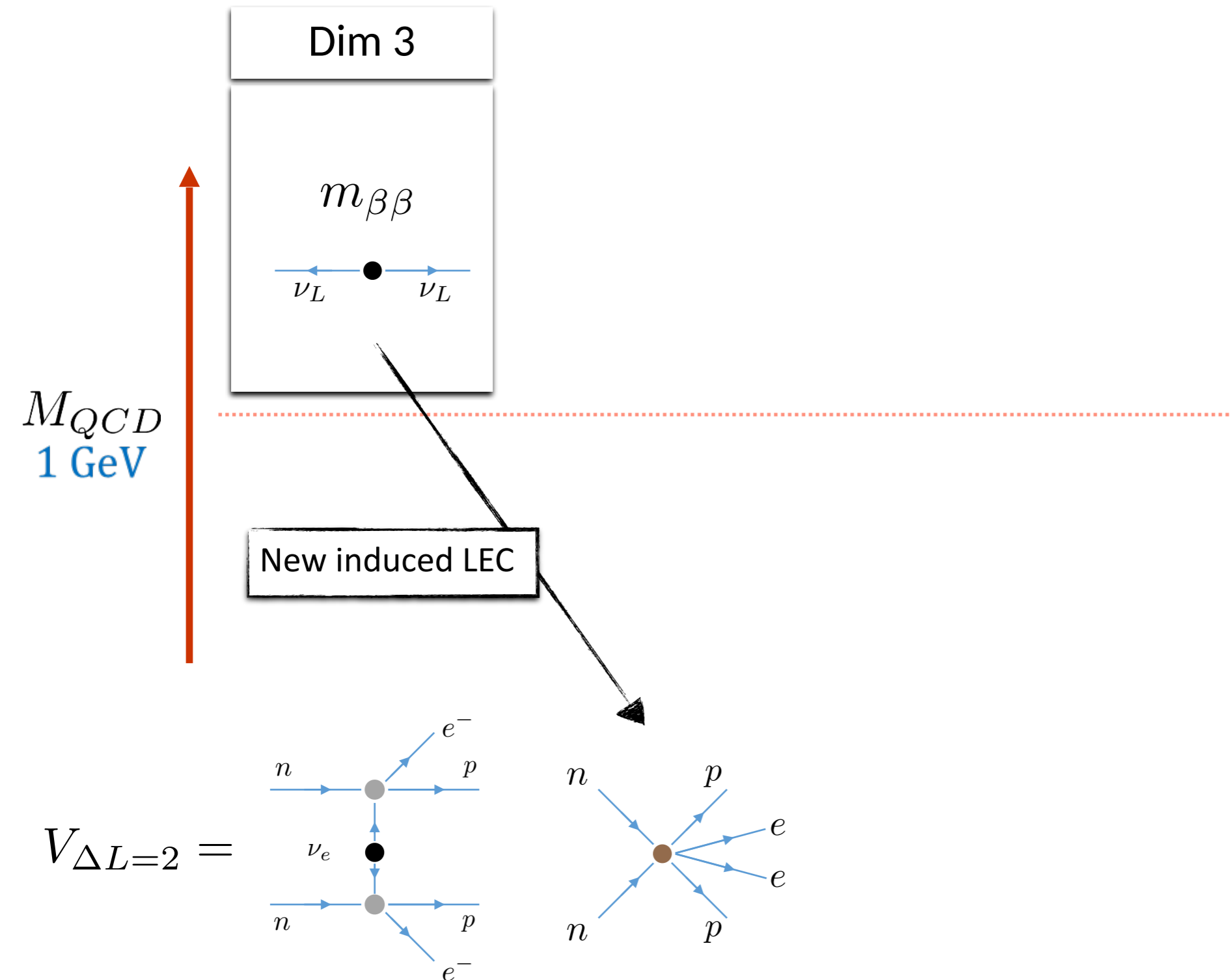


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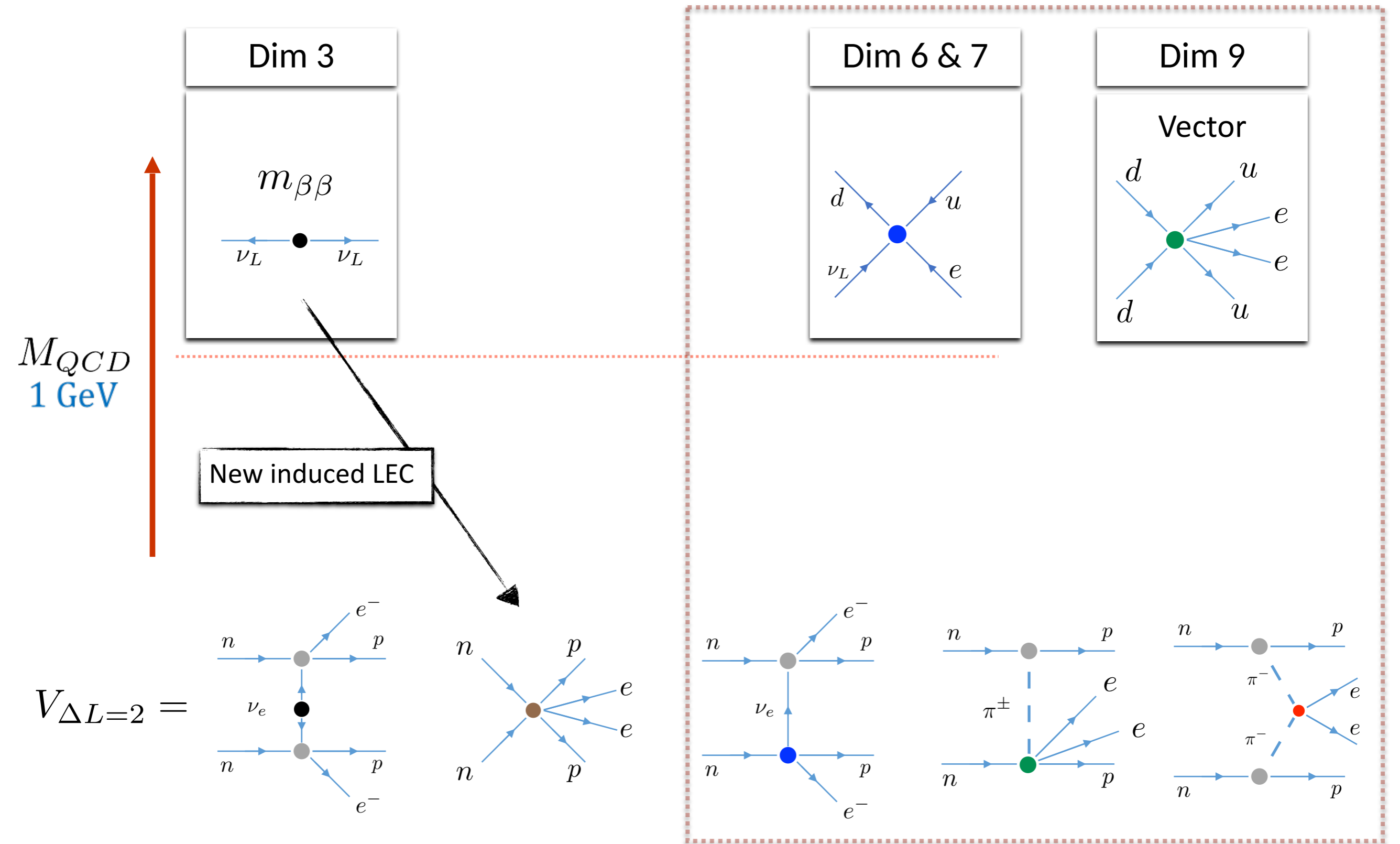
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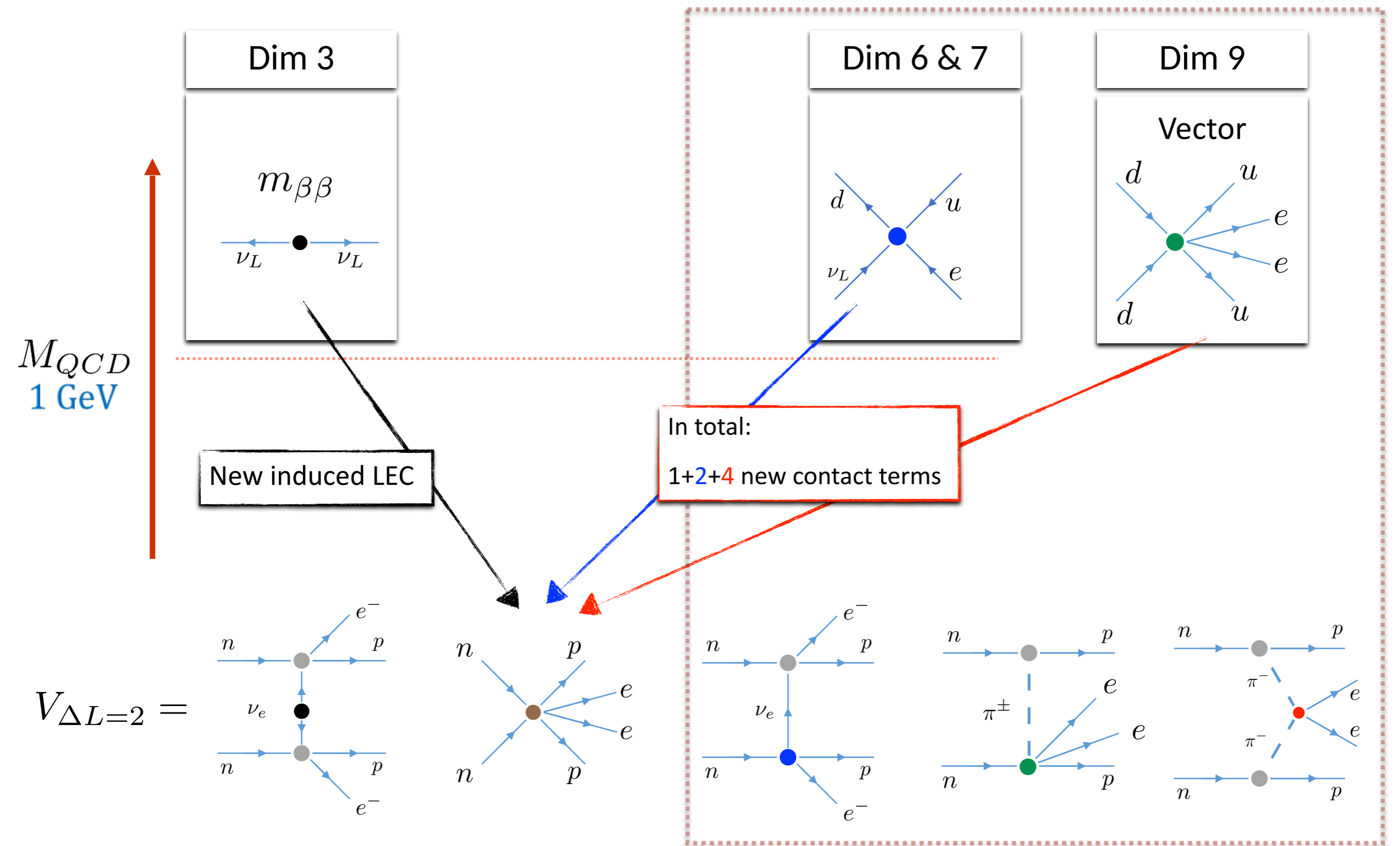
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'Non-Weinberg' counting affects higher dimensional interactions as well



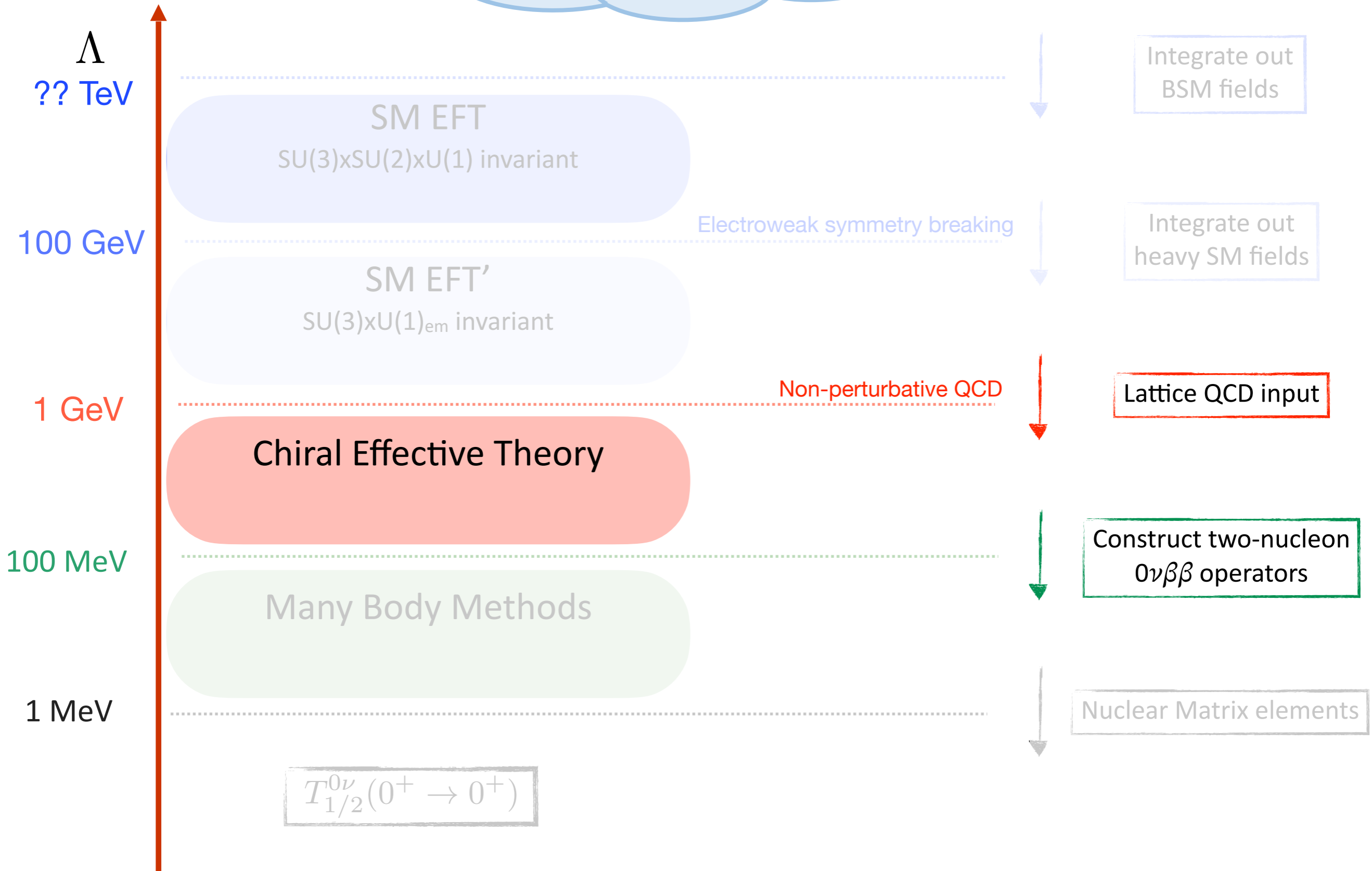
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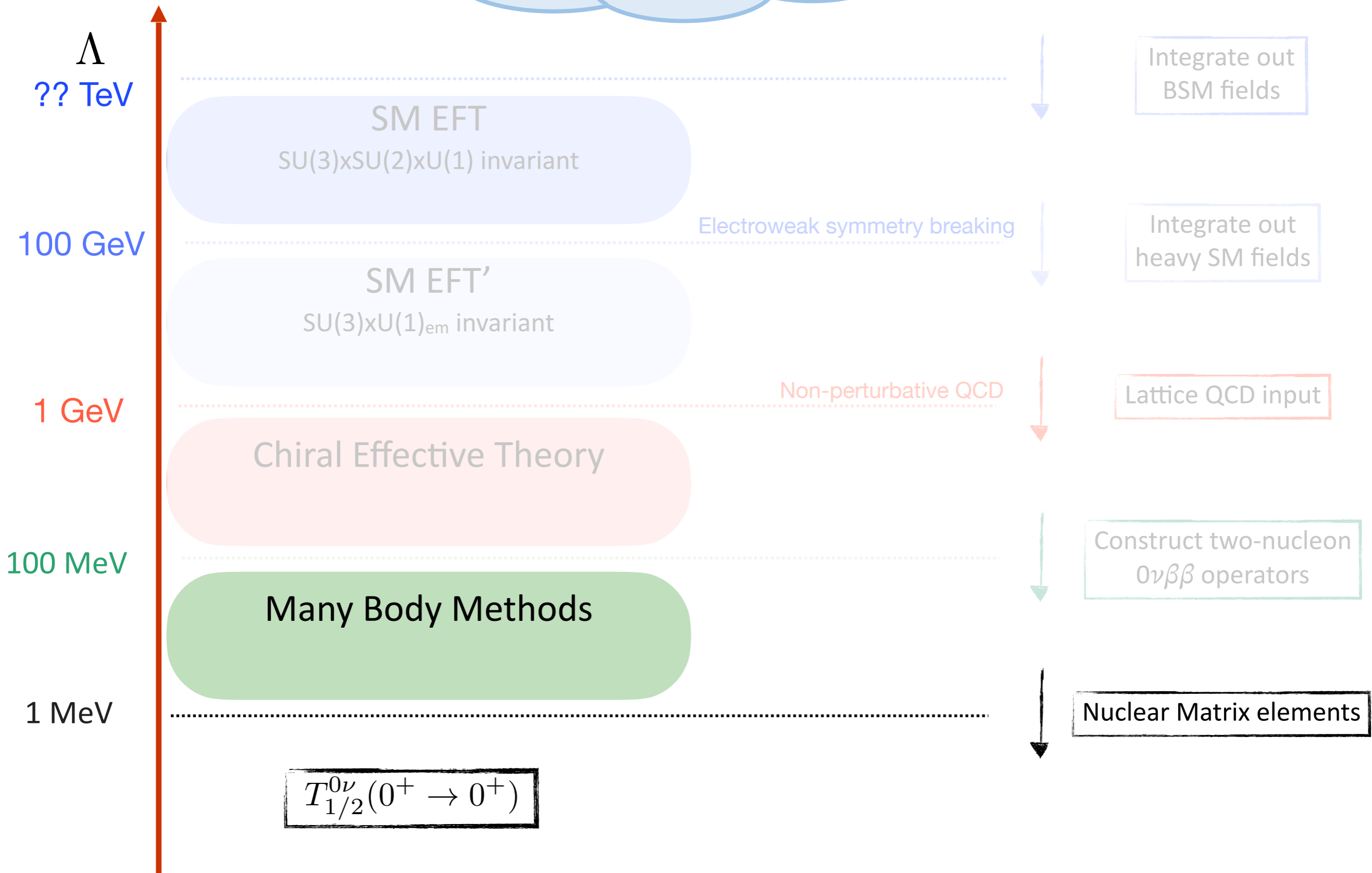
Outline

Lepton-number violation:
seesaw, left-right model, leptoquarks,...



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Nuclear matrix elements

- All NMEs can be obtained from literature*
 - 9 long-distance & 6 short-distance
- Follow LO ChiPT relations fairly well

NMEs	⁷⁶ Ge			
	[74]	[31]	[81]	[82, 83]
M_F	-1.74	-0.67	-0.59	-0.68
M_{GT}^{AA}	5.48	3.50	3.15	5.06
M_{GT}^{AP}	-2.02	-0.25		
M_{GT}^{PP}	0.66	0.33		
M_{GT}^{MM}	0.51	0.25		
M_T^{AA}	—	—		
M_T^{AP}	-0.35	0.01		
M_T^{PP}	0.10	0.00		
M_T^{MM}	-0.04	0.00		

NMEs	⁷⁶ Ge			
$M_{F, sd}$	-3.46	-1.55	-1.46	-1.1
$M_{GT, sd}^{AA}$	11.1	4.03	4.87	3.62
$M_{GT, sd}^{AP}$	-5.35	-2.37	-2.26	-1.37
$M_{GT, sd}^{PP}$	1.99	0.85	0.82	0.42
$M_{T, sd}^{AP}$	-0.85	0.01	-0.05	-0.97
$M_{T, sd}^{PP}$	0.32	0.00	0.02	0.38

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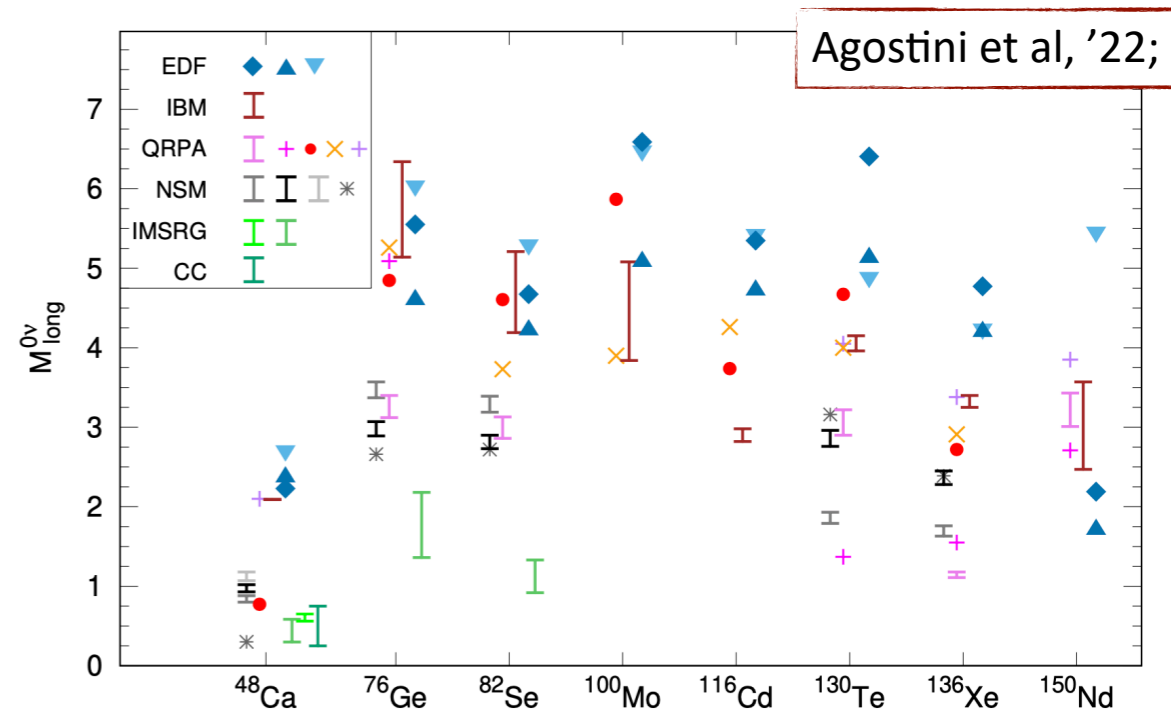
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- The NMEs differ by a factor 2-3 between methods
- Ab initio* NMEs for $A \geq 48$ are starting to appear

Belley et al '23,'20; Yao et al '20; Wirth, Yao, Hergert '21

Estimate effect of g_ν^{NN} to be $\sim 40 - 90 \%$



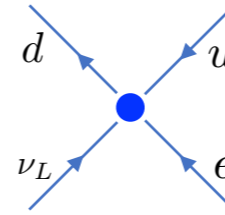
Phenomenology



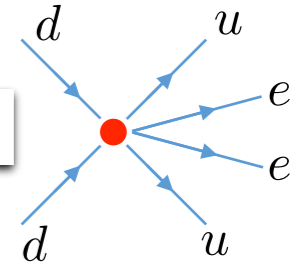
Phenomenology

From heavy new physics

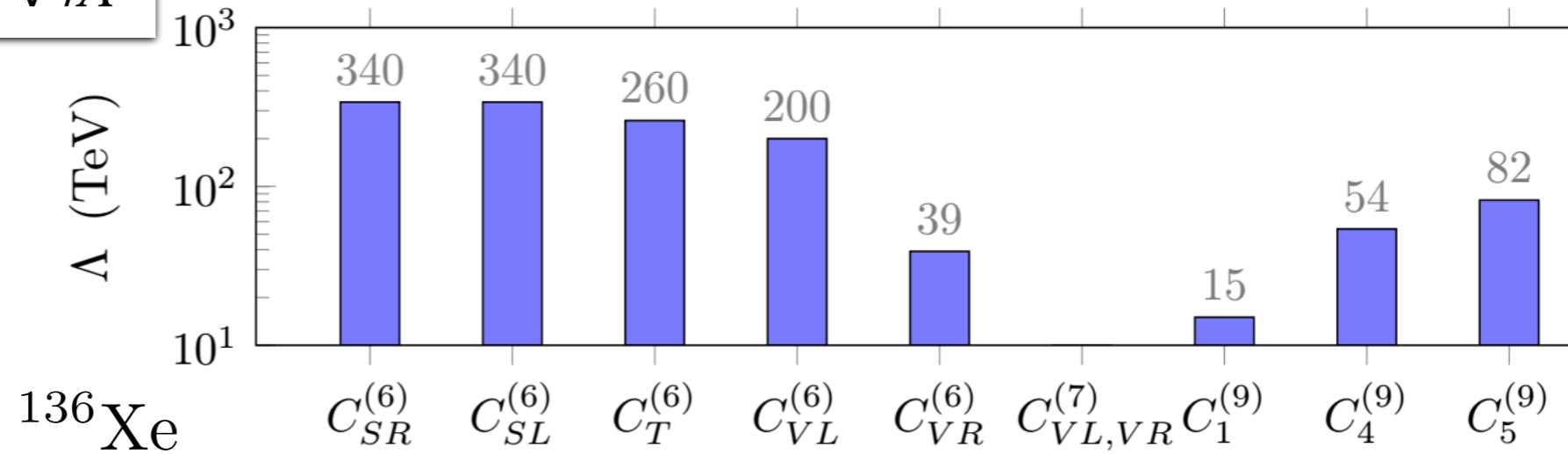
Dim 6 & 7



Dim 9



- Couplings with $C_i \sim v^3/\Lambda^3$

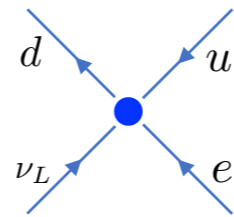


- O(1) uncertainties:
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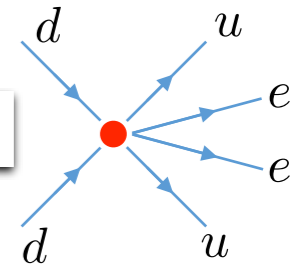
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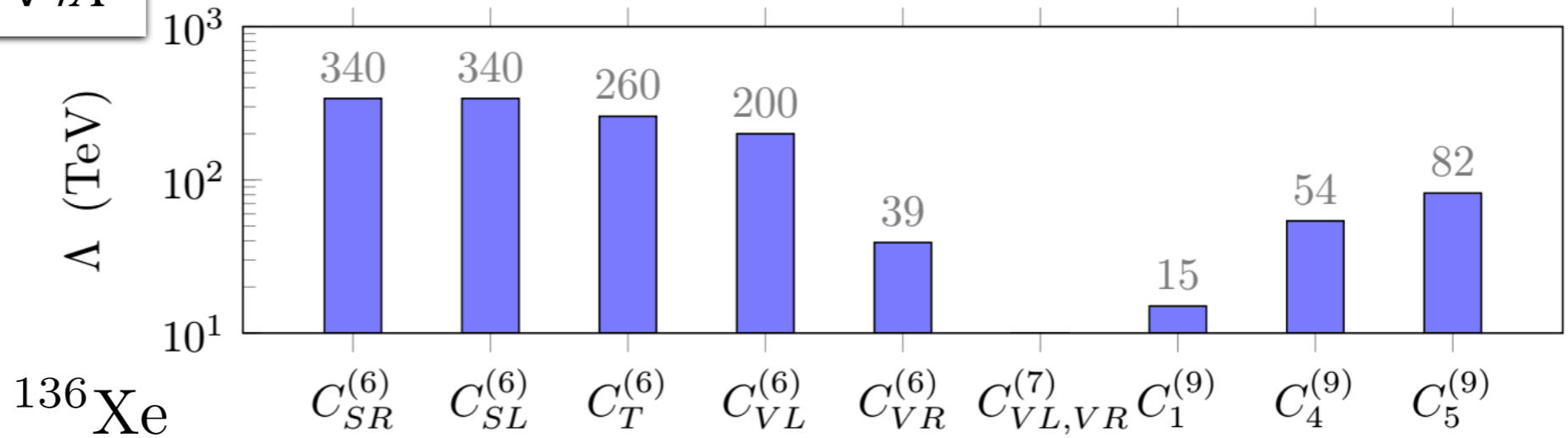
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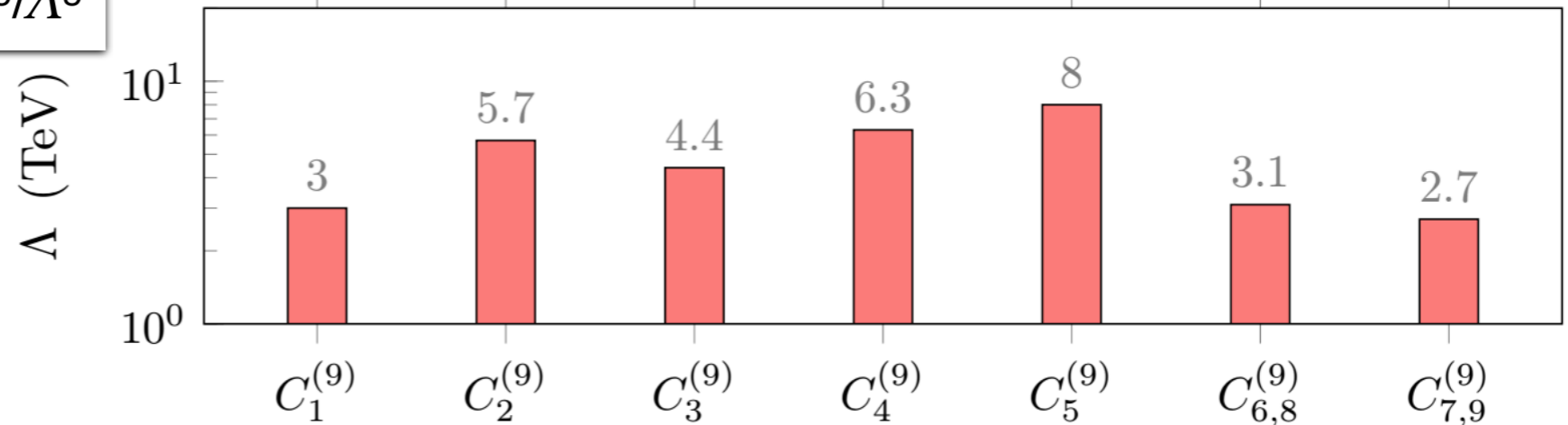
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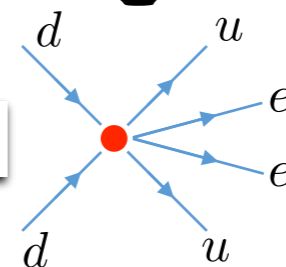


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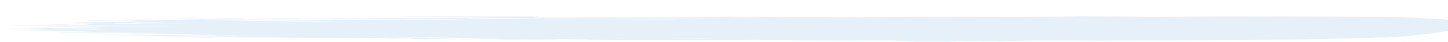


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Dim 9



Light lepton-number
violation: ν_R



Including sterile neutrinos

- ν_R 's can help solve several SM deficiencies:
 - Neutrino masses
 - Leptogenesis
 - Dark matter candidate
- Appear in numerous BSM models: Left-Right/Leptoquarks/GUTs..

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- Add n singlets, ν_R , to the SM-EFT:

$$\mathcal{L}_{\nu_R} = i\bar{\nu}_R \not{\partial} \nu_R - \frac{1}{2} \bar{\nu}_R^c M_R \nu_R - \bar{L} \tilde{H} Y_D \nu_R + \mathcal{L}_{\nu_R}^{(6)} + \mathcal{L}_{\nu_R}^{(7)}$$

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- Majorana mass
(L violating)

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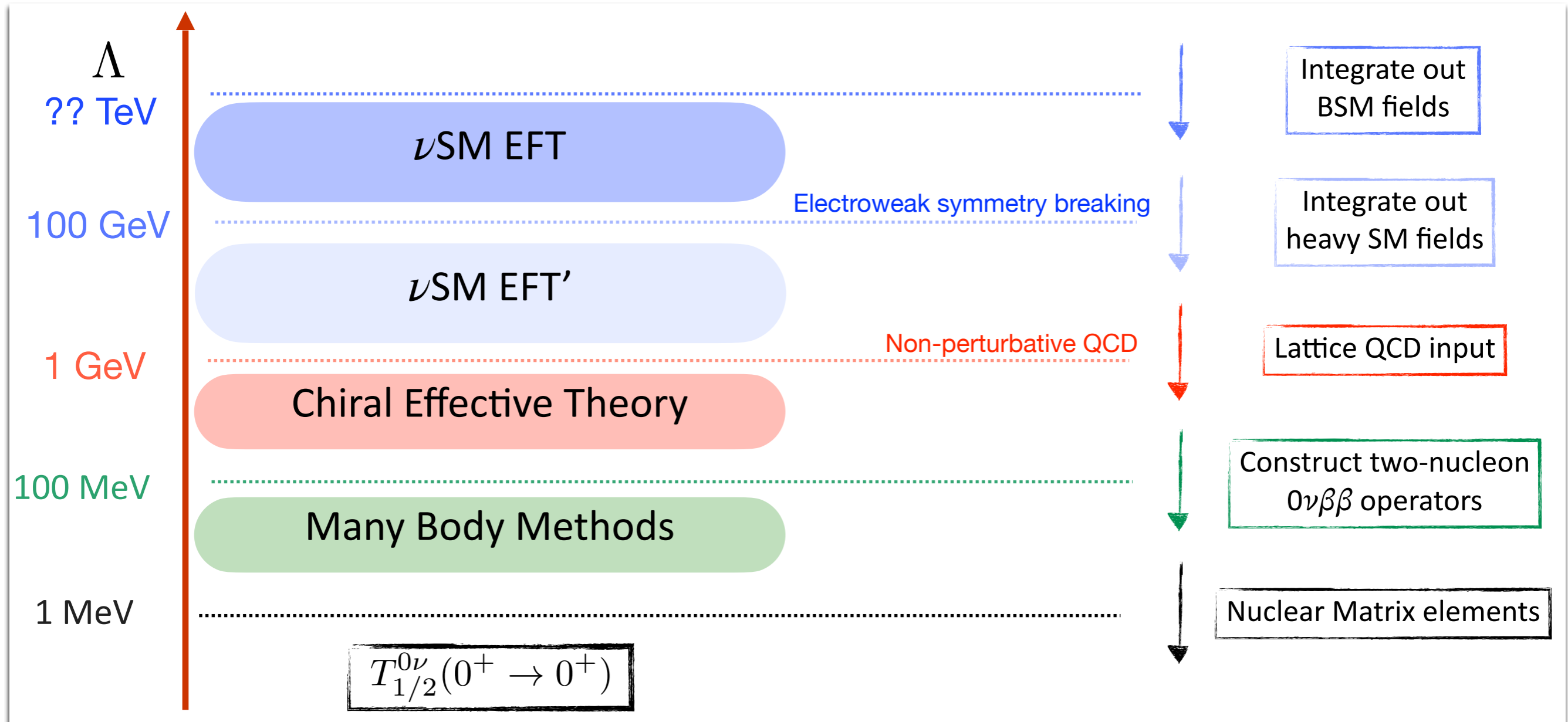
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- Higher-dimensional operators
 - Induced by heavy BSM physics

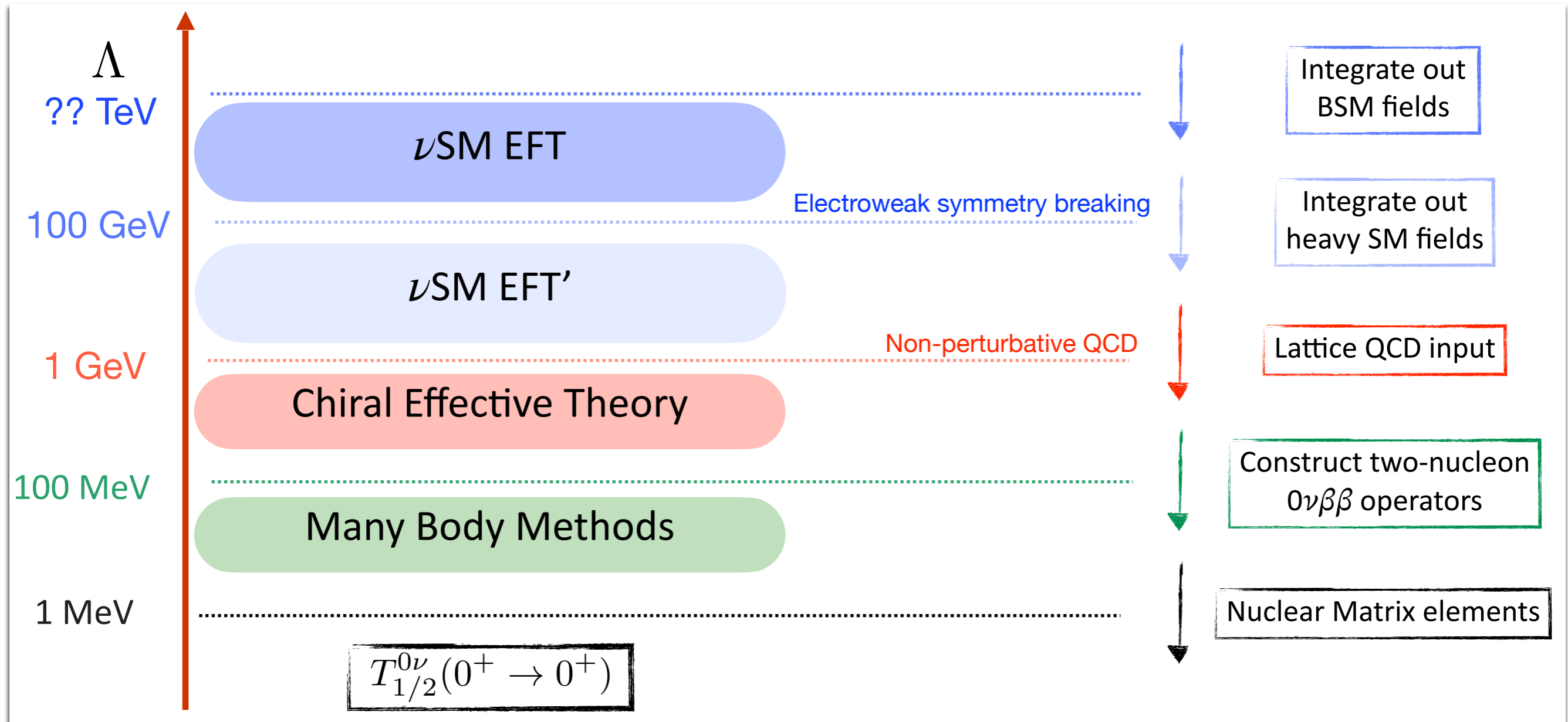
Sterile neutrinos

Can now go through the same steps as before:



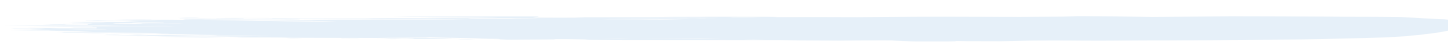
Sterile neutrinos

Can now go through the same steps as before:



- When/if ν_R can be integrated out depends on m_{ν_R}
- LECs and NMEs now depend on m_{ν_R}

Example:
minimal ν_R scenario



Minimal ν_R scenario

- Add n singlets, ν_R , to the SM:

$$\mathcal{L}_{\nu_R} = i\bar{\nu}_R \not{\partial} \nu_R - \frac{1}{2} \bar{\nu}_R^c M_R \nu_R - \bar{L} \tilde{H} Y_D \nu_R + \cancel{\mathcal{L}_{\nu_R}^{(6)}} + \cancel{\mathcal{L}_{\nu_R}^{(7)}}$$

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$$\mathcal{L}_{\nu_R} \xrightarrow{\text{EWSB}} -\frac{1}{2} \bar{N}^c M_\nu N$$

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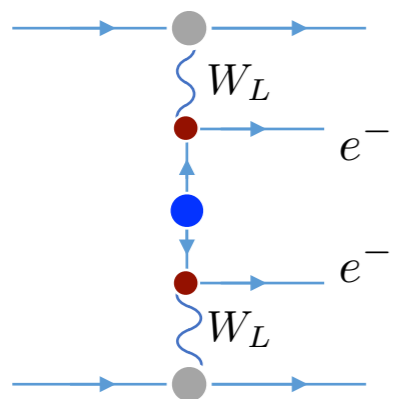
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$$\propto \sum_{i=1}^{3+n} \frac{m_i}{q^2 - m_i^2} U_{ei}^2$$

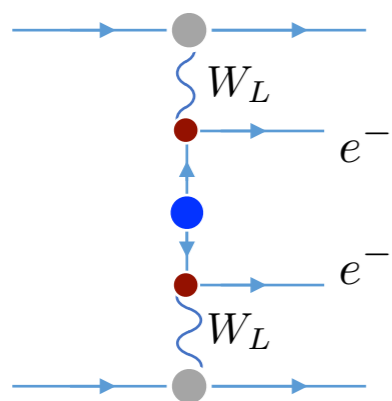
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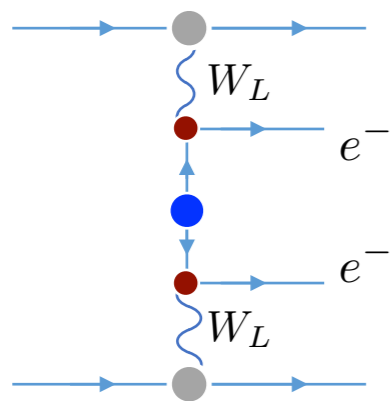
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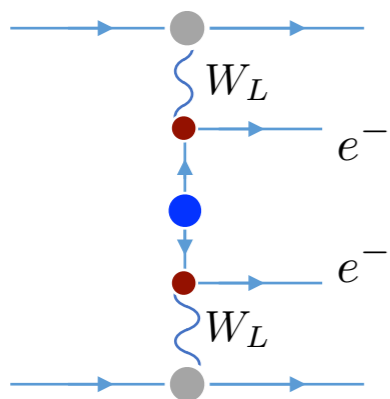
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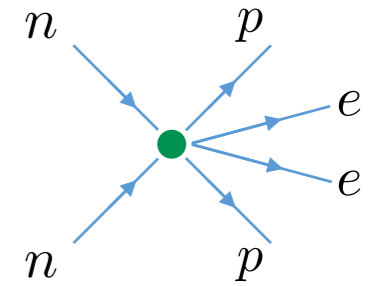
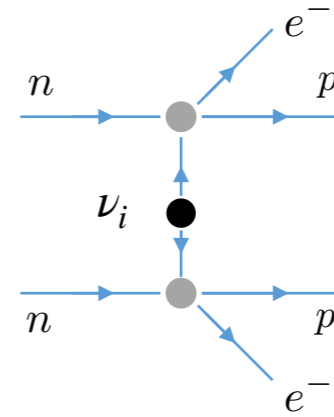
Need to keep track of m_i dependence!

\mathcal{V}_i contributions

'Usual' contributions:

- Similar to $m_{\beta\beta}$ case:
 - NMEs and LECs now m_i dependent

$$V_{\Delta L=2} =$$

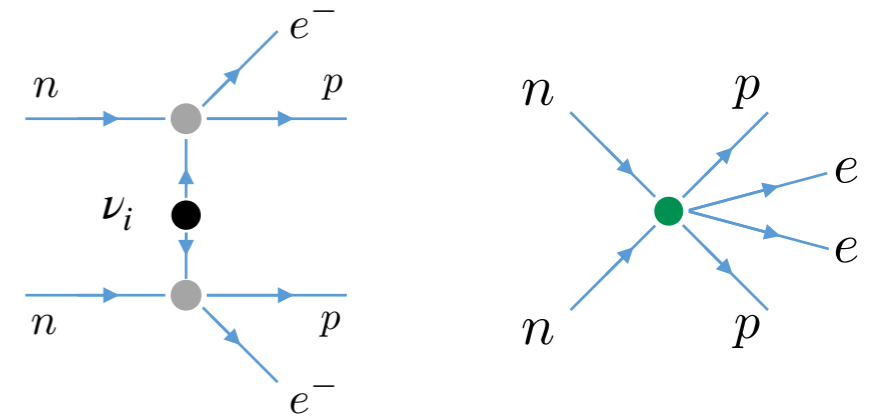


ν_i contributions

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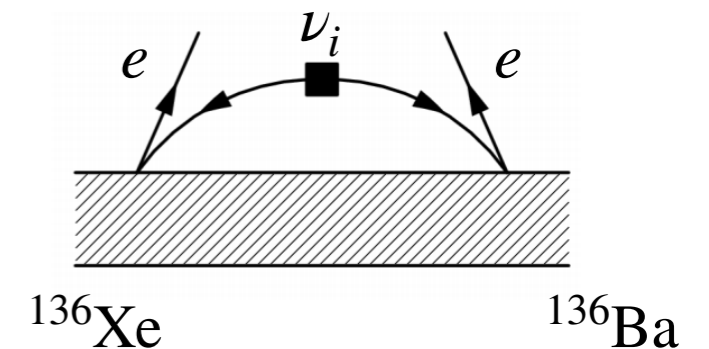


New: 'Ultrasoft' neutrinos

- Neutrinos with momenta $q^0 \sim \vec{q} \sim k_F^2/m_N$
 - See to the nucleus as a whole
 - Usually N2LO effect, now leading order

Cirigliano et al, '17

G. Zhou, J. de Vries, E. Mereghetti, J. Menéndez, P. Soriano, WD '23

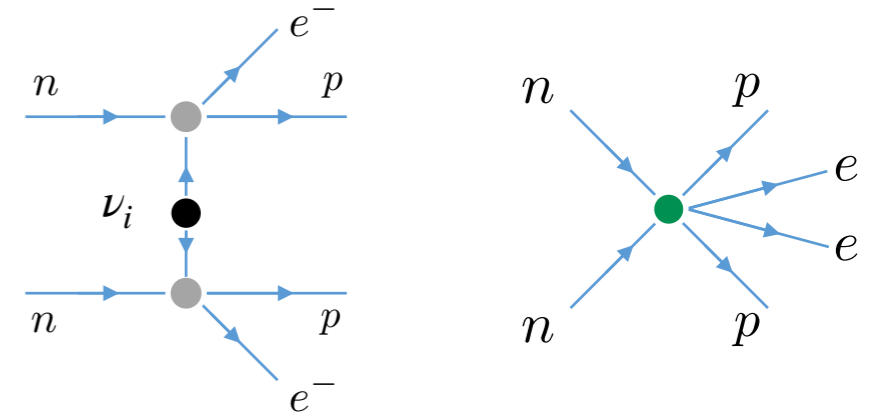


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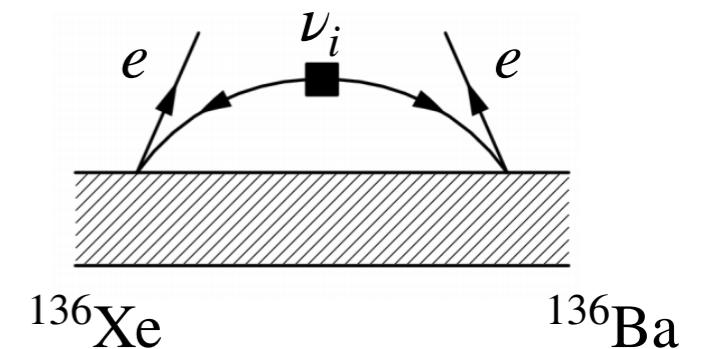


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Cirigliano et al, '17



$$A_{\nu}^{\text{usoft}} \sim \sum_n \langle f | J_{\mu} | n \rangle \langle n | J^{\mu} | i \rangle \times \begin{cases} \frac{m_i}{k_F}, & \Delta E \lesssim m_i \lesssim k_F \\ \frac{m_i^2}{4\pi k_F \Delta E} \ln \frac{m_i}{\Delta E}, & m_i \lesssim \Delta E \end{cases}$$

- Depends on intermediate state energies, $\Delta E \equiv E_n + E_e - E_i$
- Overlap integrals

Phenomenology: A toy model

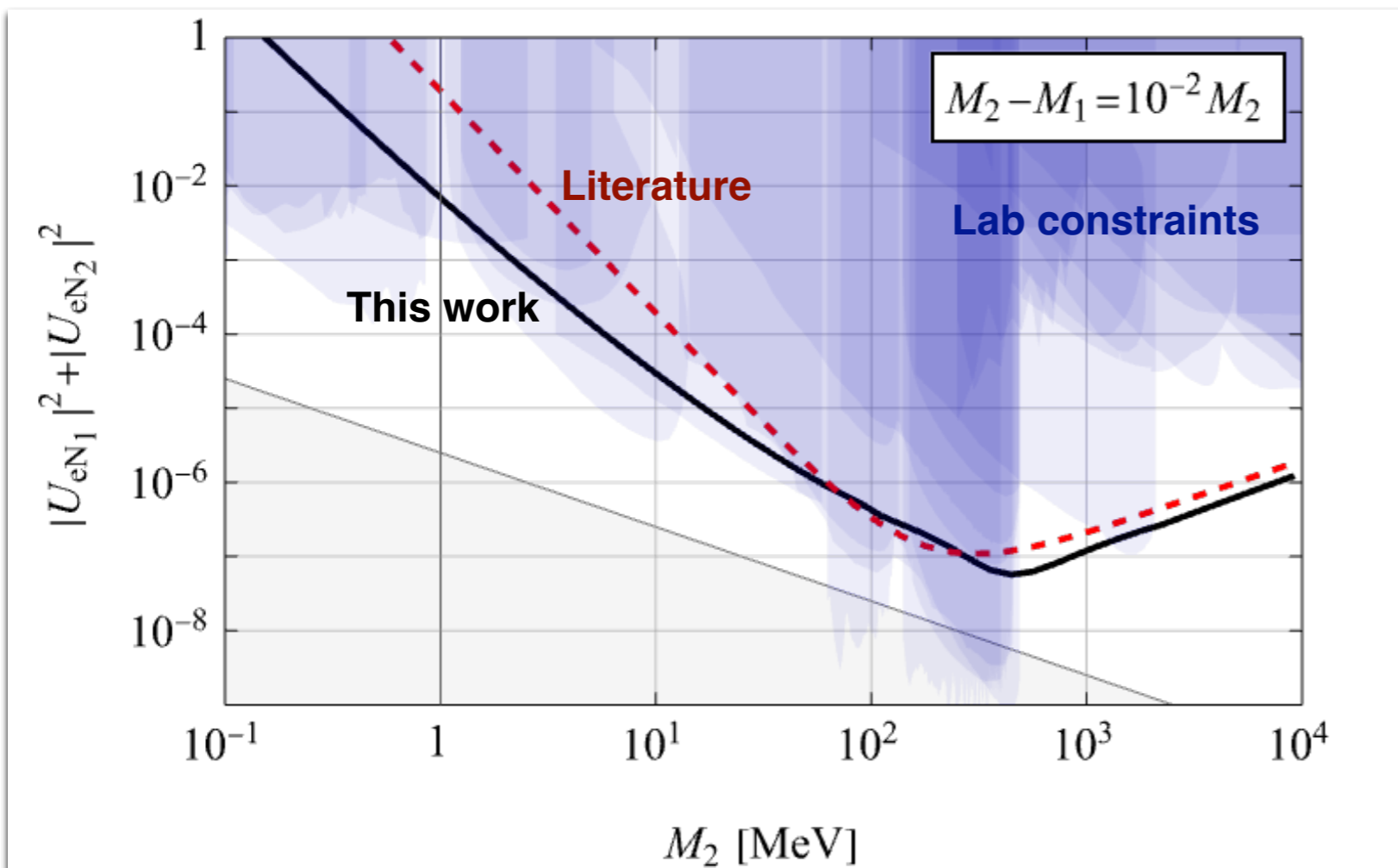


Toy model: 1+1+1 pseudo-Dirac

- Involves 1 active, two sterile neutrinos
 - Assume steriles much heavier than the active neutrinos; $M_1 \simeq M_2 \gg m_\nu$
 - Two heavier ν 's, form a pseudo-Dirac pair
 - Light neutrino mass proportional to LNV parameter (opposite to seesaw)

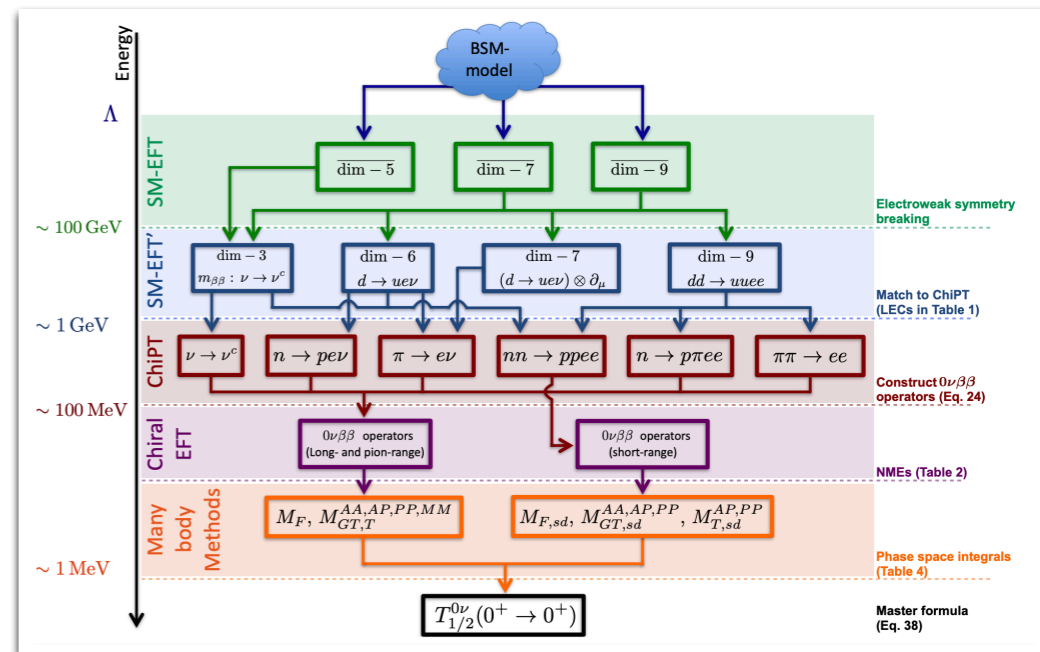
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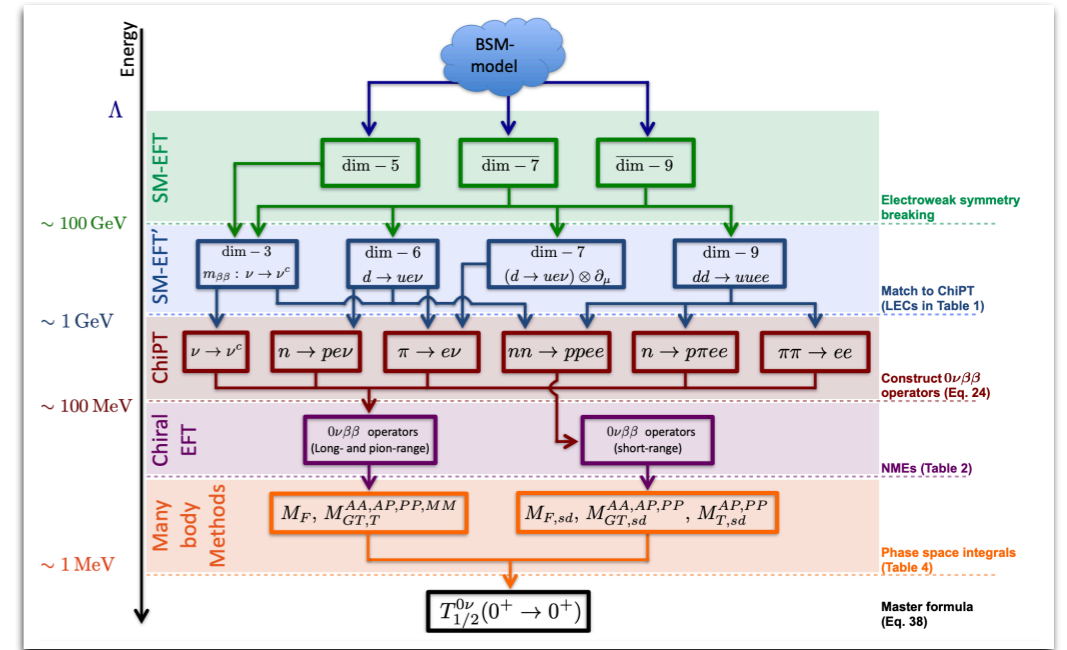
Summary

- EFTs allow one to systematically describe $\Delta L=2$ sources
- Standard mechanism (dim-5)
- Dimension-7 & -9 sources
- Effects from ν_R

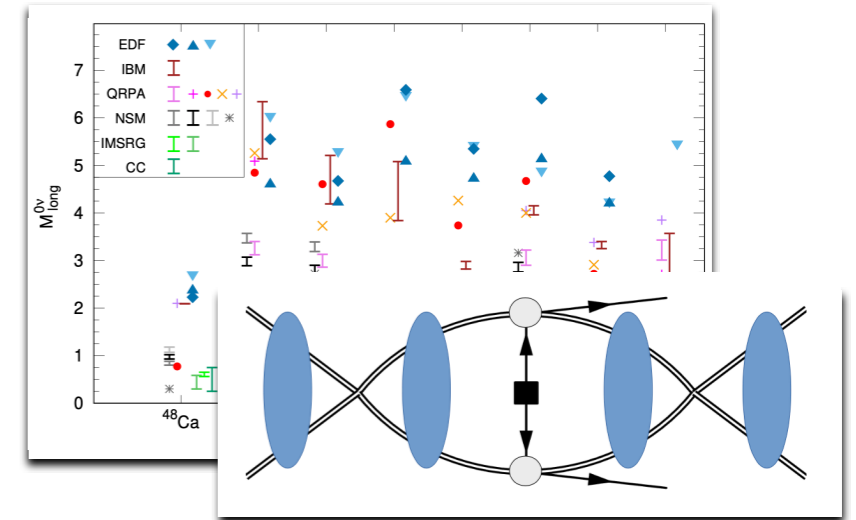


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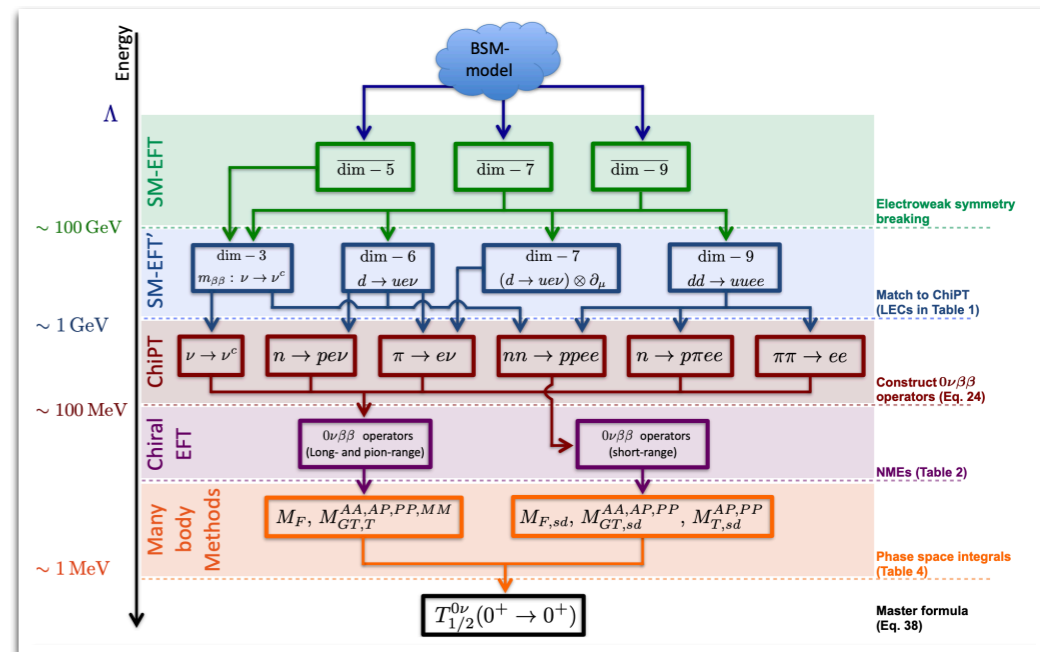


- Matching to chiral EFT involves unknown LECs
- Renormalization requires terms beyond usual counting
- Needed Nuclear Matrix Elements determined in literature

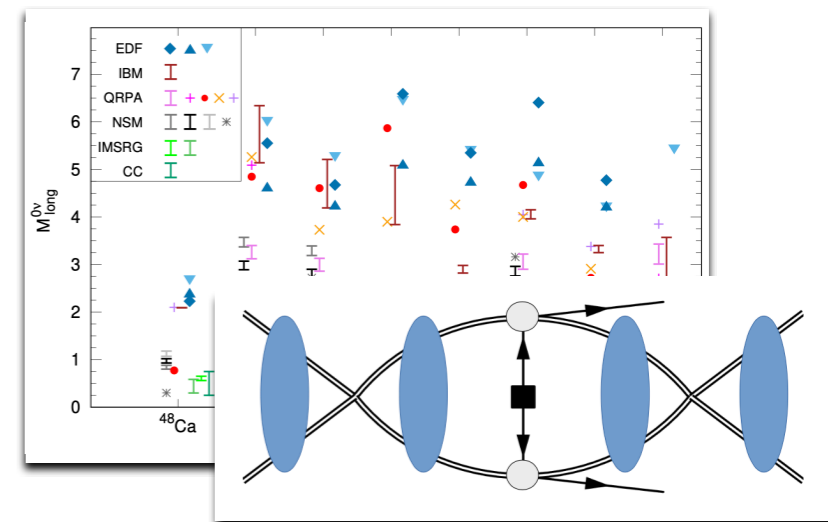


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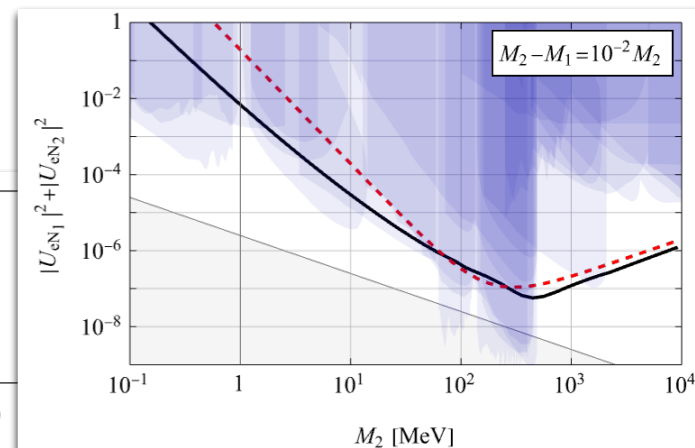
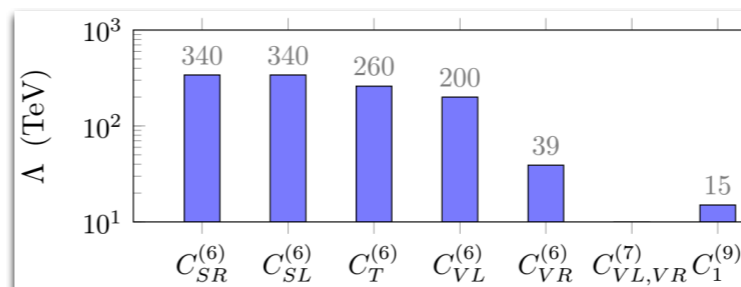
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- Needed Nuclear Matrix Elements determined in literature



- $0\nu\beta\beta$ probes
- Up to $O(100)$ TeV scales heavy BSM
- Light sterile ν_R interactions



Back up slides



Why dim 7, 9?



Effective Field Theory

Naive scaling of Dimension 5, 7, 9 operators

$$A_{0\nu\beta\beta} \sim \frac{c_5}{\Lambda} \left[1 + \left(\frac{v}{\Lambda}\right)^2 \frac{c_7}{c_5} + \left(\frac{v}{\Lambda}\right)^4 \frac{c_9}{c_5} \right]$$

- $v/\Lambda \ll 1$ So why keep dimension 7 & 9?

$m_\nu \sim c_5 v^2 / \Lambda$ Allows for relative enhancement:

- $c_5 \ll O(1)$, $\Lambda = \mathcal{O}(1 - 100)\text{TeV}$
 - Relative enhancement of higher-dimensional terms due to $c_{7,9}/c_5 \gg 1$
- Happens, for example, in the left-right model
- However, if $c_5 = \mathcal{O}(1)$, $\Lambda = 10^{15}\text{ GeV}$
 - dimension-7, -9 irrelevant in this case

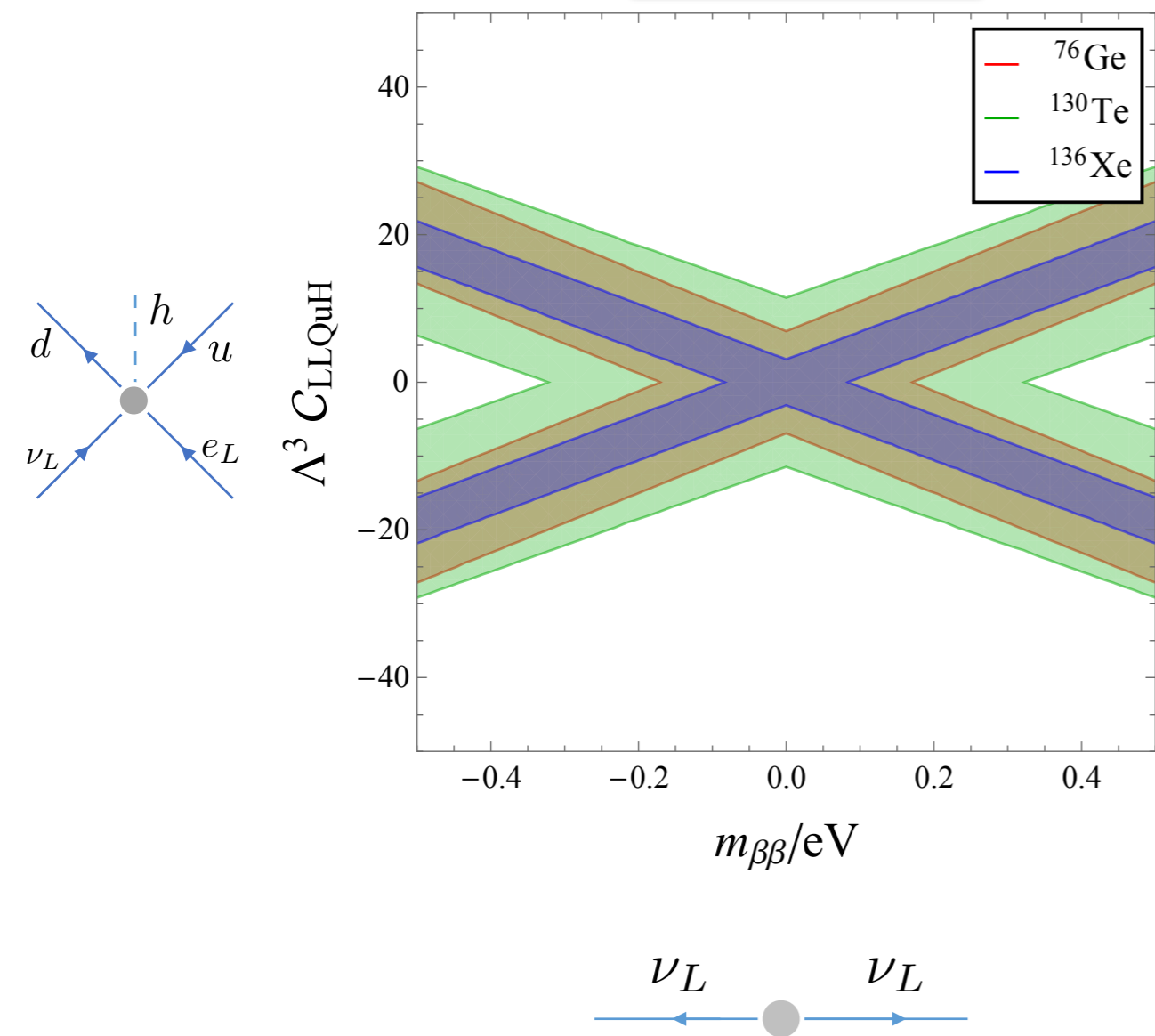
Disentangling operators



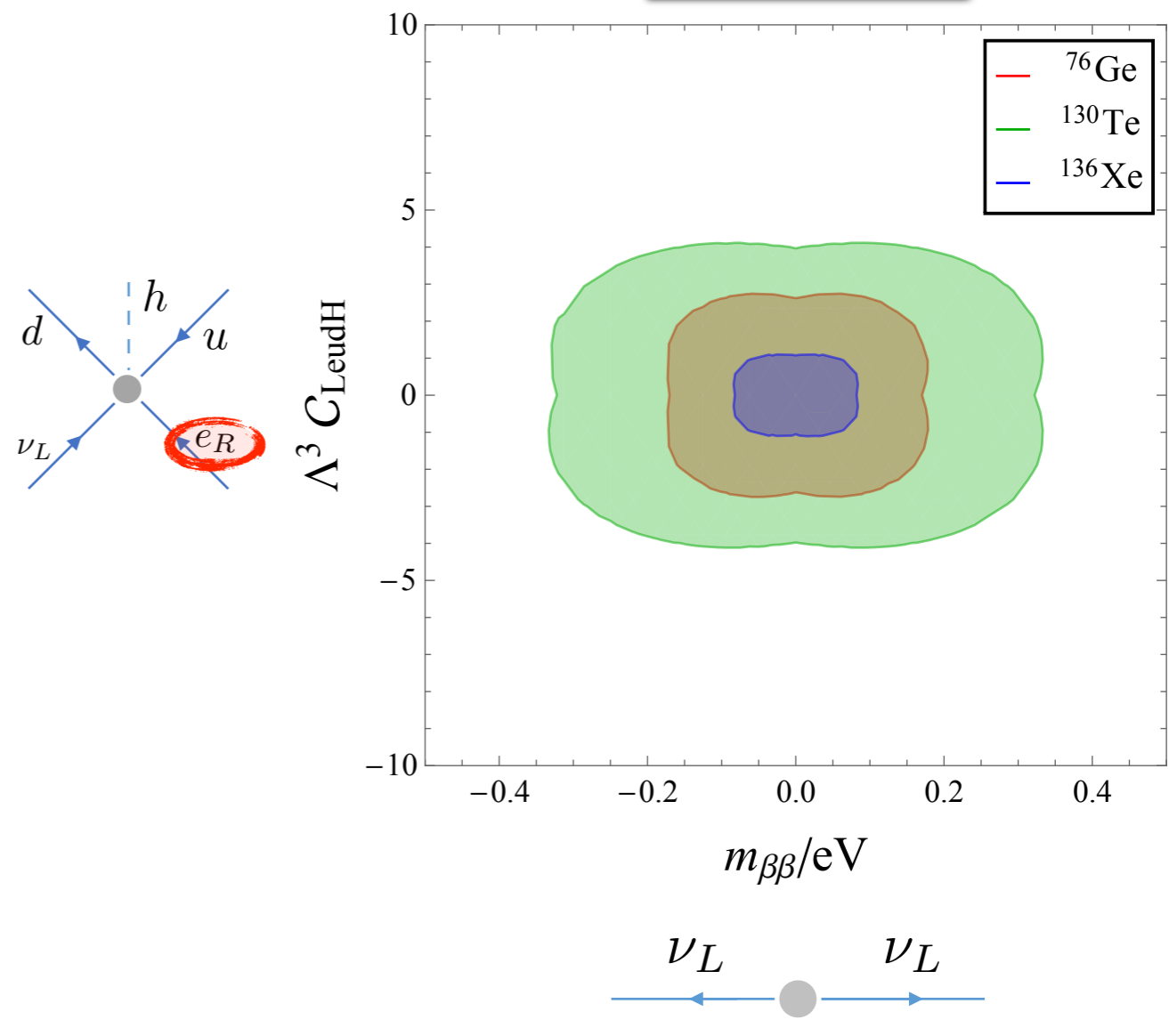
Phenomenology

From heavy new physics

$\Lambda=600$ TeV



$\Lambda=40$ TeV



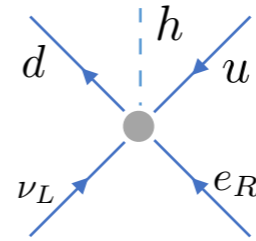
Disentangling operators

What if a $0\nu\beta\beta$ signal is measured?

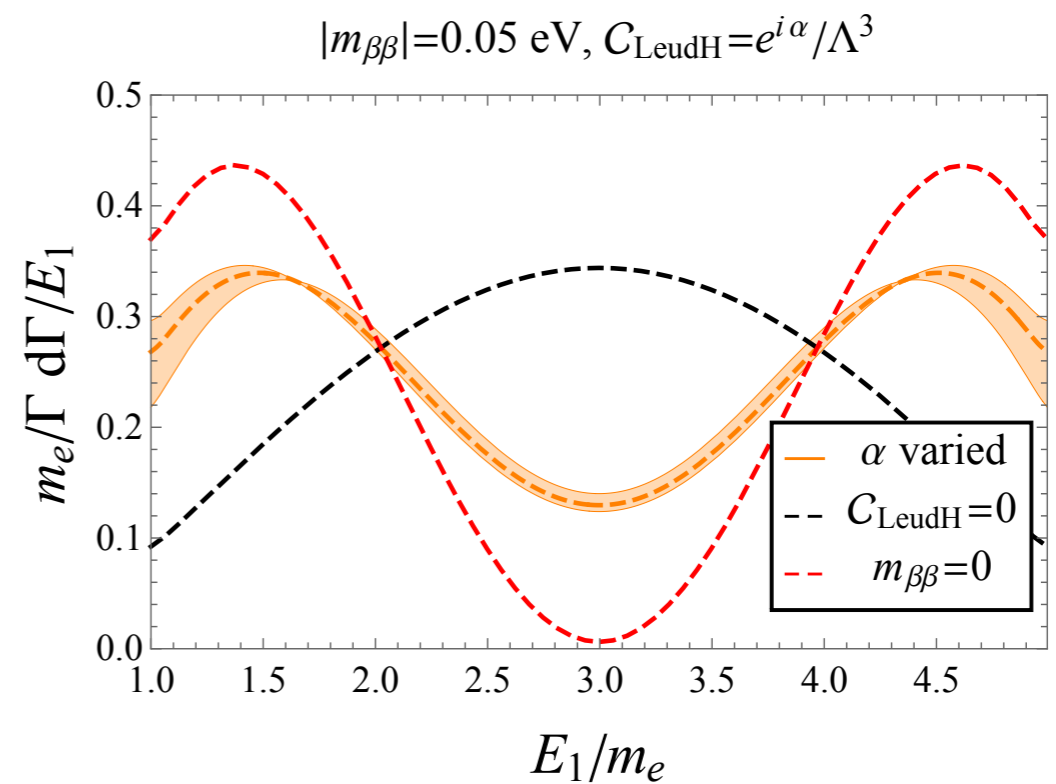
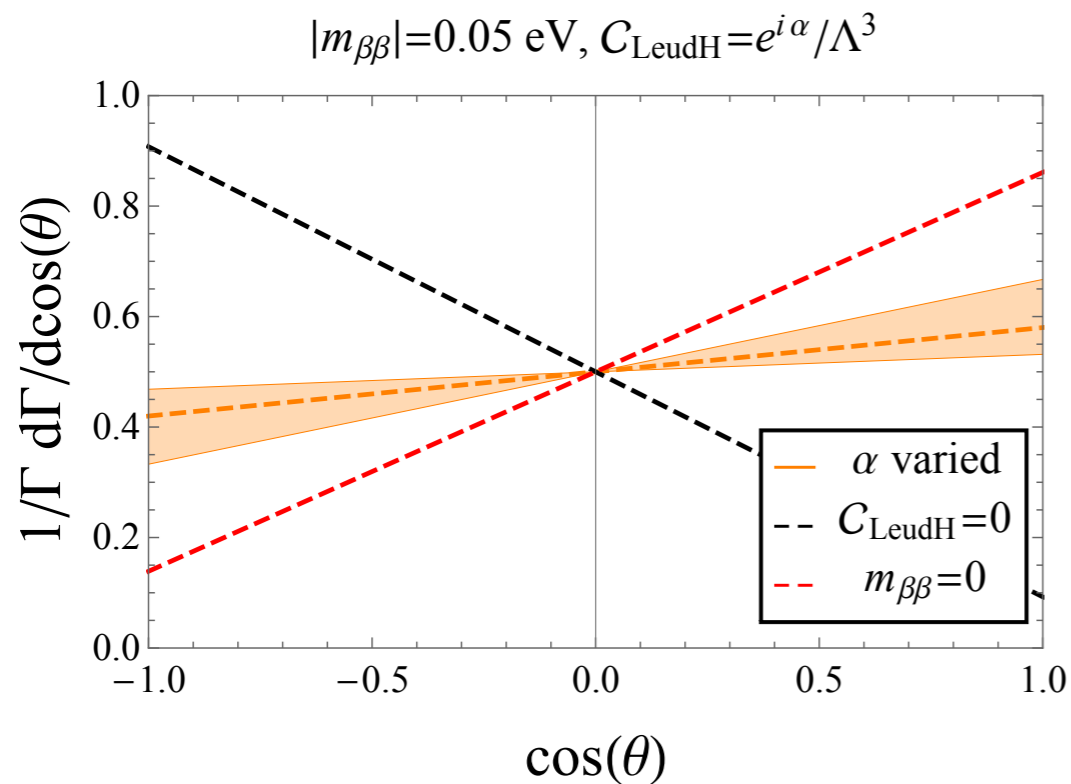
- Picking the allowed values



$$m_{\beta\beta} = 0.05 \text{ eV}$$



$$C_{\text{LeudH}} = e^{i\alpha} / \Lambda^3 \quad \Lambda = 40 \text{ TeV}$$

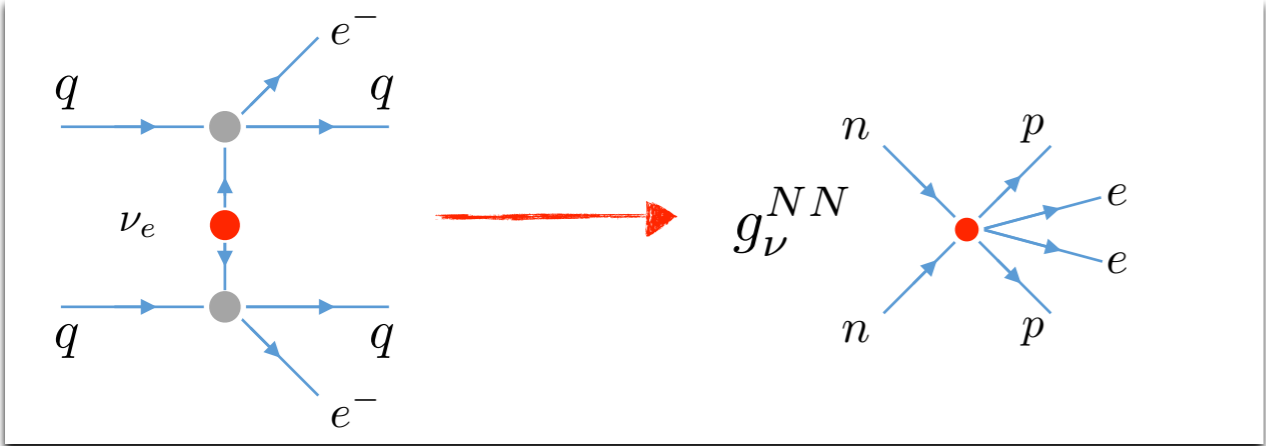


g_{ν}^{NN} : Relation to
electromagnetism

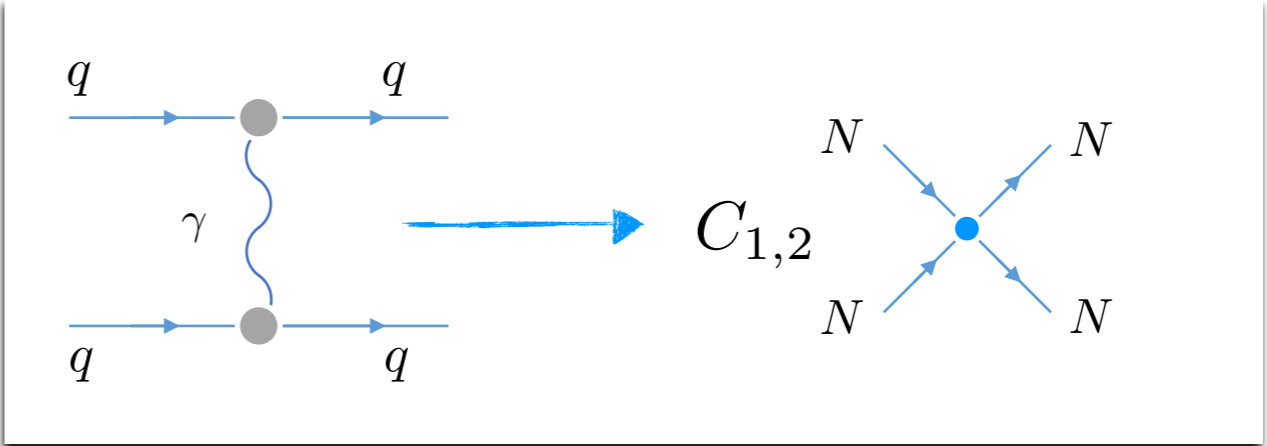


Relation to electromagnetism

LNV contact term



EM contact term



- Hard part of two Weak currents

$$\sim G_F^2 m_{\beta\beta} \langle NN | J_L^\mu(x) J_{L\mu}(y) | NN \rangle$$

$$\times \int \frac{d^4 q}{(2\pi)^4} \frac{e^{iq \cdot (x-y)}}{q^2}$$

- Leptonic part combines to boson propagator

- Hard part of two EM currents

$$\sim e^2 \langle NN | J_{EM}^\mu(x) J_{EM\mu}(y) | NN \rangle$$

$$\times \int \frac{d^4 q}{(2\pi)^4} \frac{e^{iq \cdot (x-y)}}{q^2}$$

- Non-hadronic part is the photon propagator

The appearance of the photon propagator allows one to relate the two!

Relation to electromagnetism

- Only two $\Delta I=2$ operators can be induced

$$O_1 = \bar{N} Q_L N \bar{N} Q_L N - \frac{\text{Tr } Q_L^2}{6} \bar{N} \vec{\tau} N \bar{N} \vec{\tau} N + (L \rightarrow R)$$

$$O_2 = \bar{N} Q_L N \bar{N} Q_R N - \frac{\text{Tr } Q_L Q_R}{6} \bar{N} \vec{\tau} N \bar{N} \vec{\tau} N + (L \leftrightarrow R)$$

with spurions

$$Q_L = u^\dagger Q_L u, \quad Q_R = u Q_R u^\dagger,$$

$$u = \exp(i\pi \cdot \tau / 2F_\pi)$$

EM

$$\mathcal{L}_{em} = e^2/4 (C_1 O_1 + C_2 O_2)$$

$$Q_L = Q_R = \tau^3/2$$

LNV

$$\mathcal{L}_{LNV} = g_\nu^{NN} G_F^2 m_{\beta\beta} O_1 \bar{e} e^c$$

$$Q_L = \tau^+, \quad Q_R = 0$$

Chiral symmetry

$$g_\nu^{NN} = C_1$$

Relation to electromagnetism

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EM

$$\mathcal{L}_{em} = e^2/4 (C_1 O_1 + C_2 O_2)$$

$$Q_L = Q_R = \tau^3/2$$

- EM induces an extra term
 - Equivalent up to 2 pions
 - Hard to disentangle

LNV

$$\mathcal{L}_{LNV} = g_\nu^{NN} G_F^2 m_{\beta\beta} O_1 \bar{e} e^c$$

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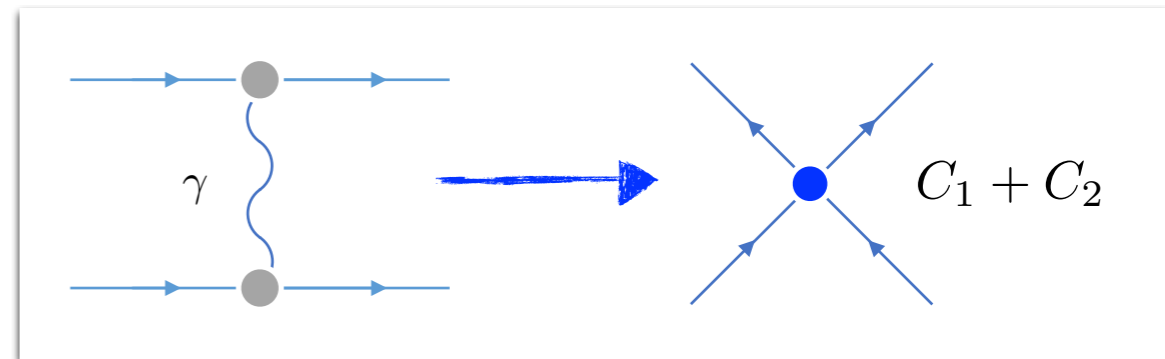
Chiral symmetry

$$g_\nu^{NN} = C_1$$

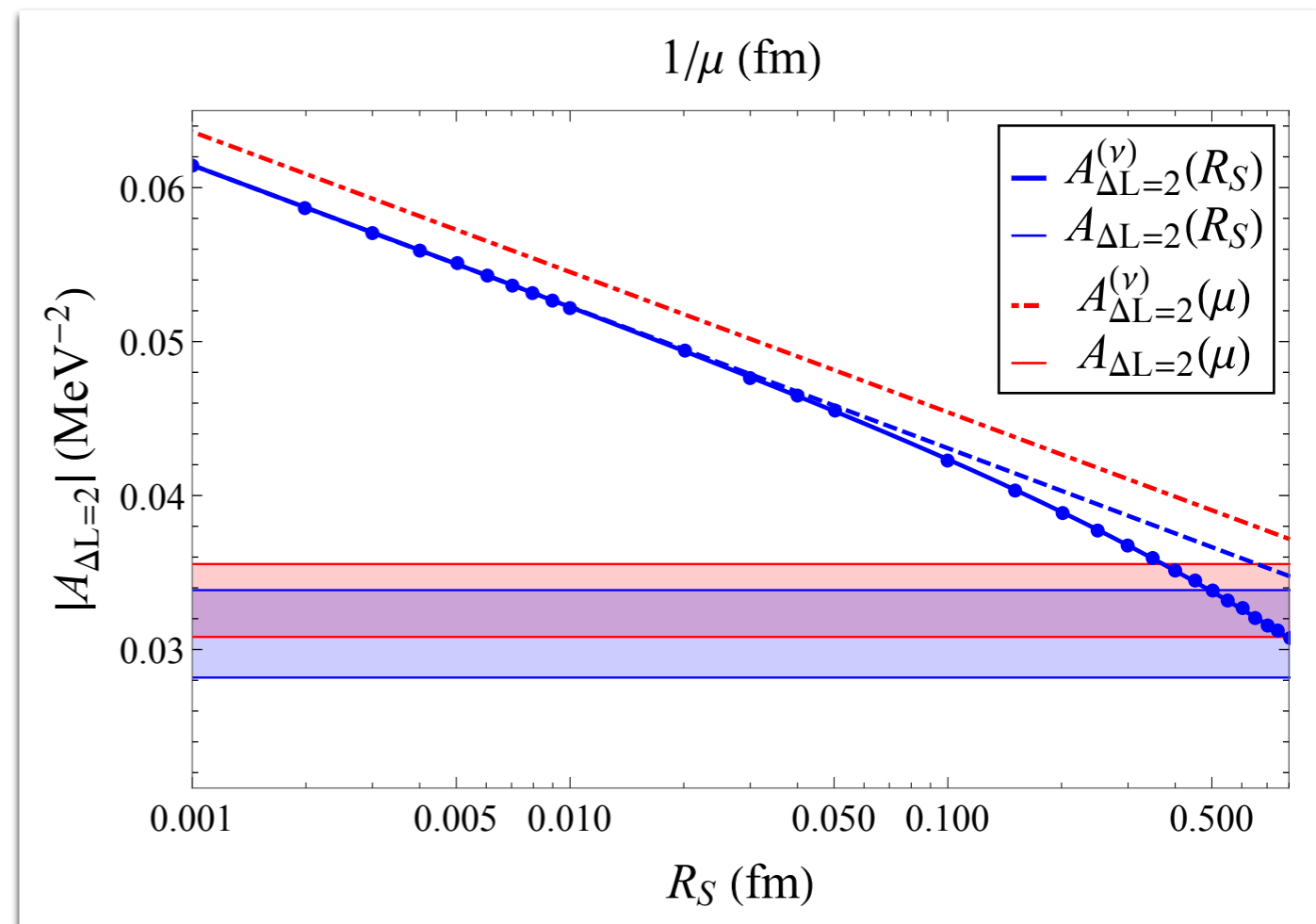
Relation to electromagnetism

- $\Delta l=2$ in NN scattering

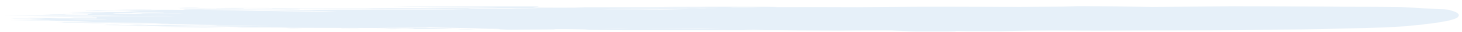
- Charge-independence breaking $(a_{nn} + a_{pp})/2 - a_{np}$
 - From photon exchange & the pion mass difference
 - $C_1 + C_2$ (needed at LO in isospin breaking)



- Allows an estimate of g_ν^{NN}
 - Extract $C_1 + C_2$ from CIB
 - Assume $g_\nu^{NN}(\mu) = \frac{C_1(\mu) + C_2(\mu)}{2}$
 - Roughly 10% effect for $R_S = 0.6$ fm
 - Uncontrolled error



g_{ν}^{NN} : Estimate from
Cottingham approach

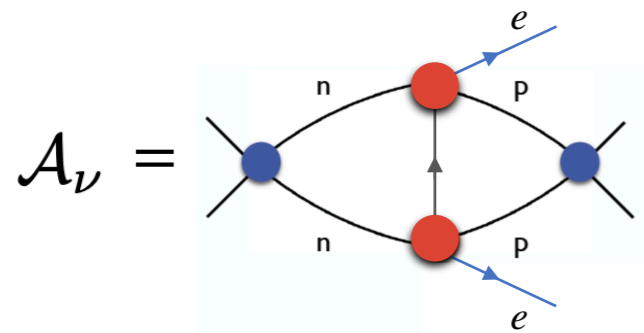


Determination of the counterterm

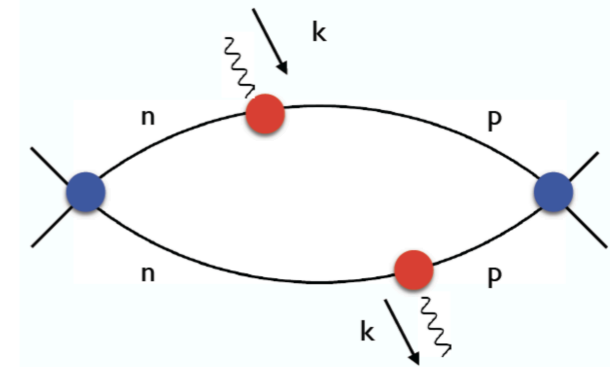
Cirigliano, (WD) et al, '20, '21

- Analogy to the Cottingham approach for pion/nucleon mass differences

$$A_\nu \propto \int \frac{d^4 k}{(2\pi)^4} \frac{g_{\mu\nu}}{k^2 + i\epsilon} \int d^4 x e^{ik \cdot x} \langle pp | T \{ j_W^\mu(x) j_W^\nu(0) \} | nn \rangle$$



$$A_\nu = \int dk a(k) = \int \frac{d^4 k}{(2\pi)^4} \frac{1}{k^2 + i\epsilon}$$

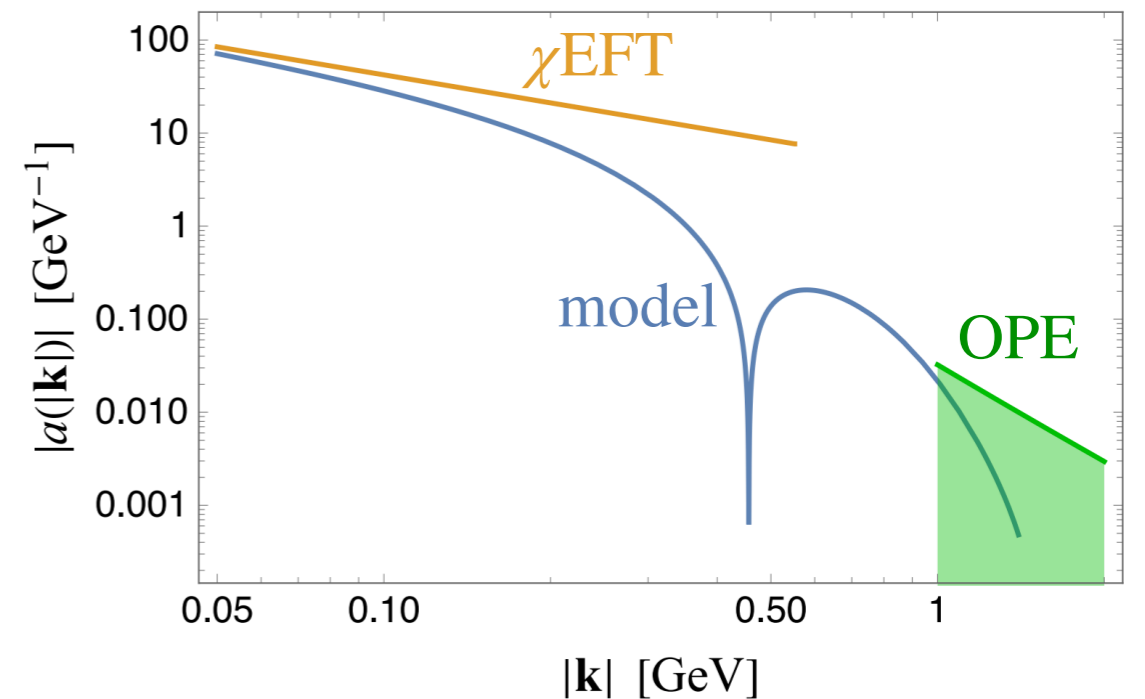


- Estimate the A_ν by constraining the **integrand**

- $k \ll \Lambda_\chi$ region determined by χ EFT
- $k \gg \text{GeV}$ region determined by OPE

- **Model** intermediate region using:

- Form factors
- Off-shell effects from NN intermediate states

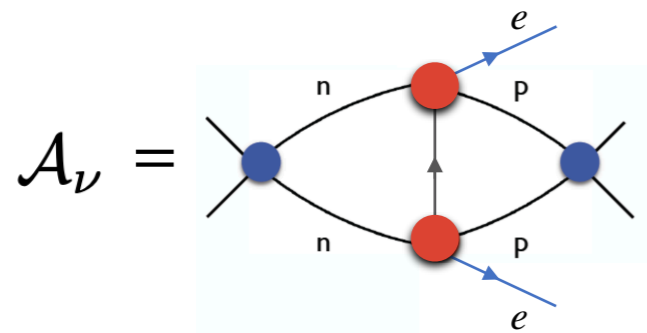


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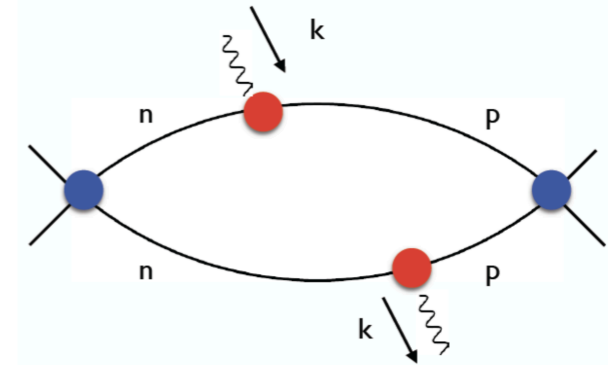
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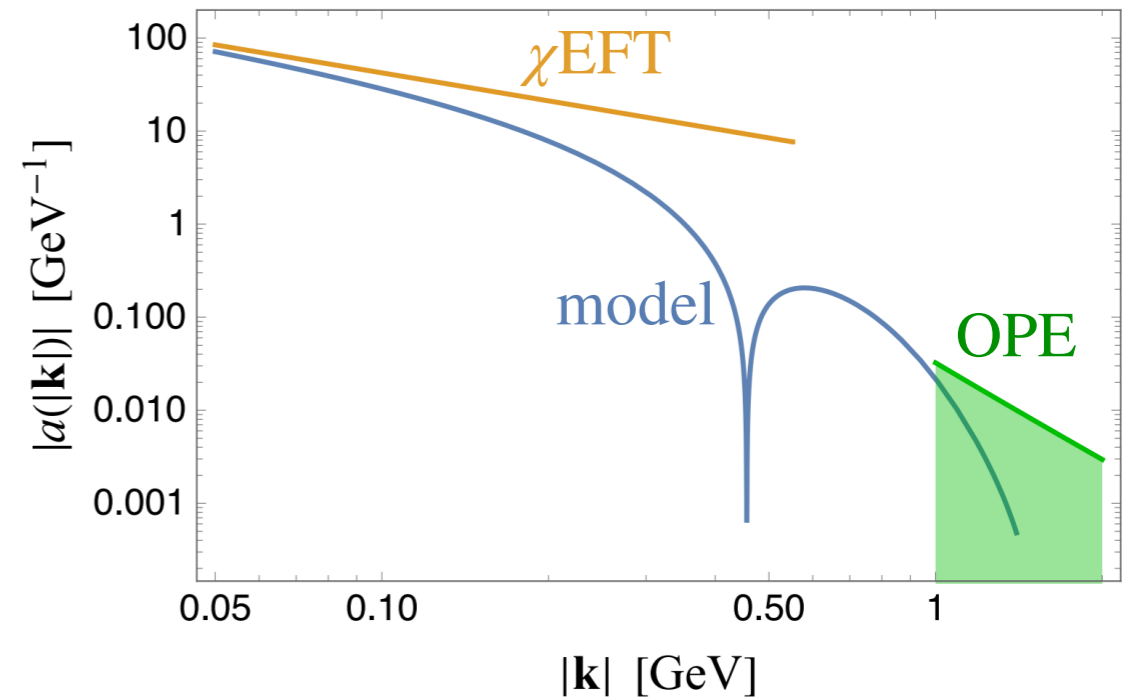
$$A_\nu \propto \int dk a(k) = \int \frac{d^4 k}{(2\pi)^4} \frac{1}{k^2 + i\epsilon}$$



- Gives $\tilde{g}_\nu^{NN}(\mu = m_\pi) = 1.3(6)$ in $\overline{\text{MS}}$

- Estimated 30% uncertainty
- Validated in isospin-breaking observables
- Consistent with large- N_c estimate

Richardson et al, '21



g_{ν}^{NN} : Impact in nuclei



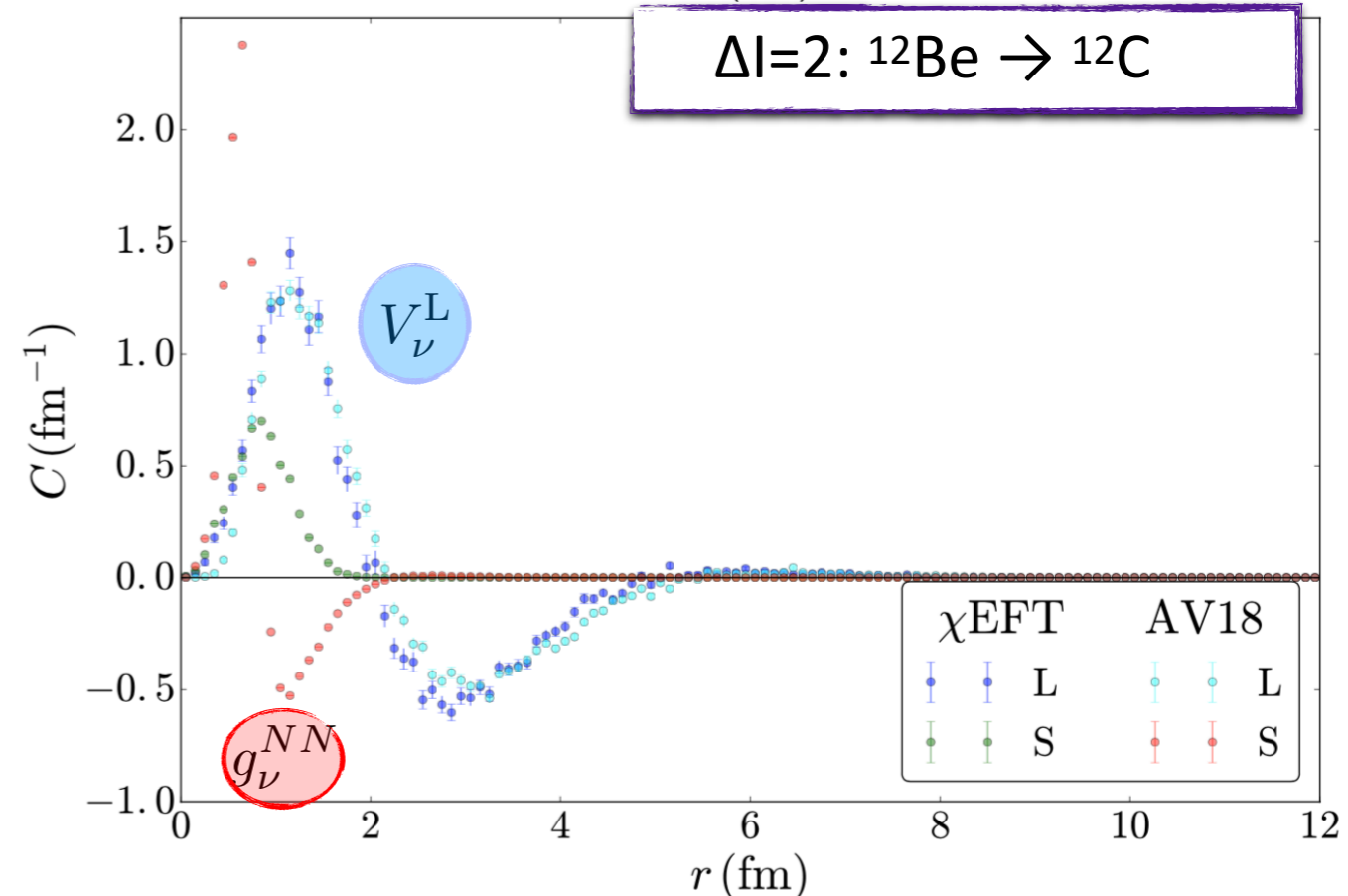
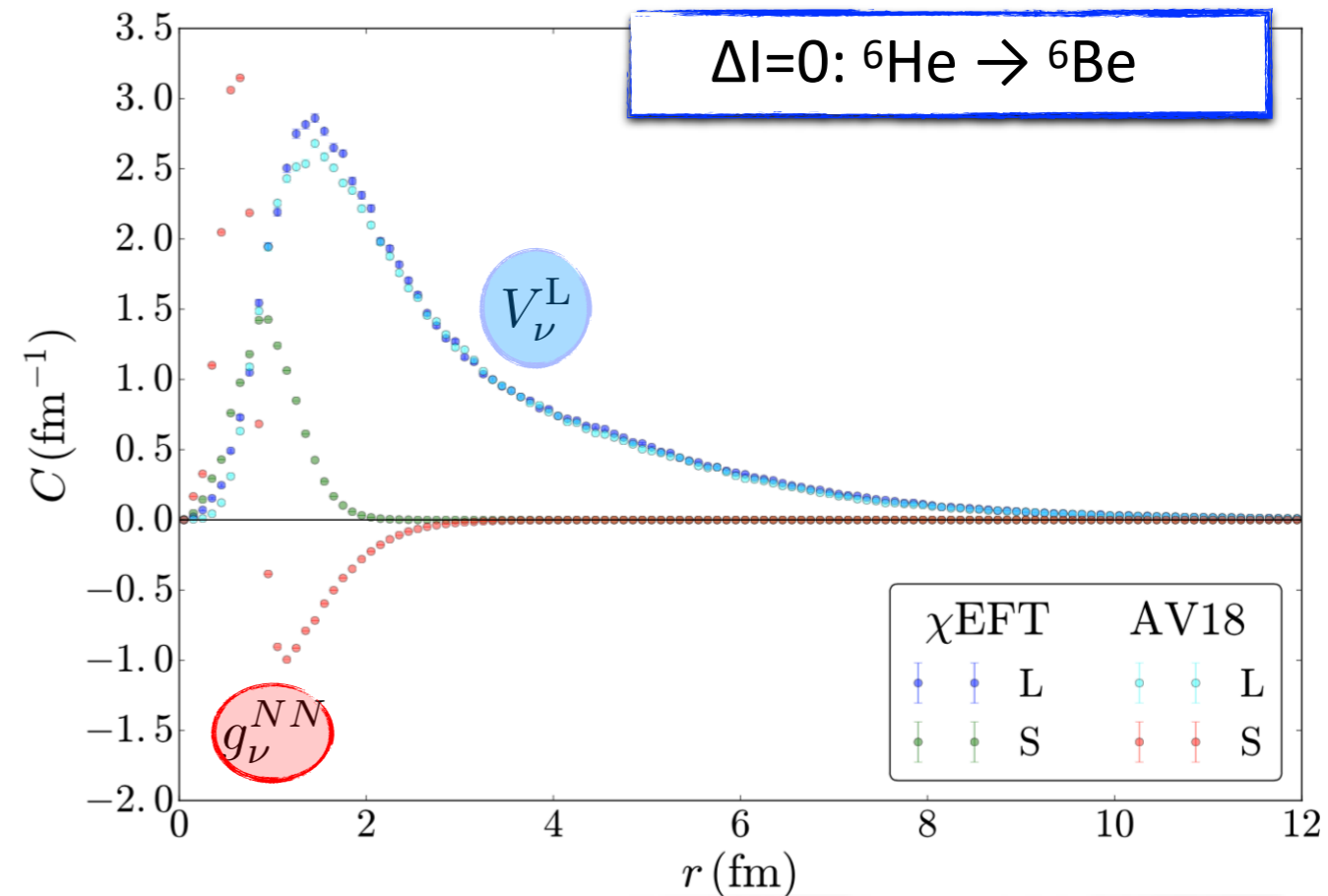
Estimate of impact

Light nuclei

M. Piarulli, R. Wiringa, S. Pastore

- Using $g_\nu = (C_1 + C_2)/2$
- With:
 - Chiral potential M. Piarulli et. al. '16
 - AV18 potential R. Wiringa, Stoks, Schiavilla, '95

- ~10% effect in ${}^6\text{He} \rightarrow {}^6\text{Be}$
- ~60% effect in ${}^{12}\text{Be} \rightarrow {}^{12}\text{C}$
 - Due to presence of a node
 - Feature in realistic $0\nu\beta\beta$ candidates



Estimate of impact

Heavy nuclei

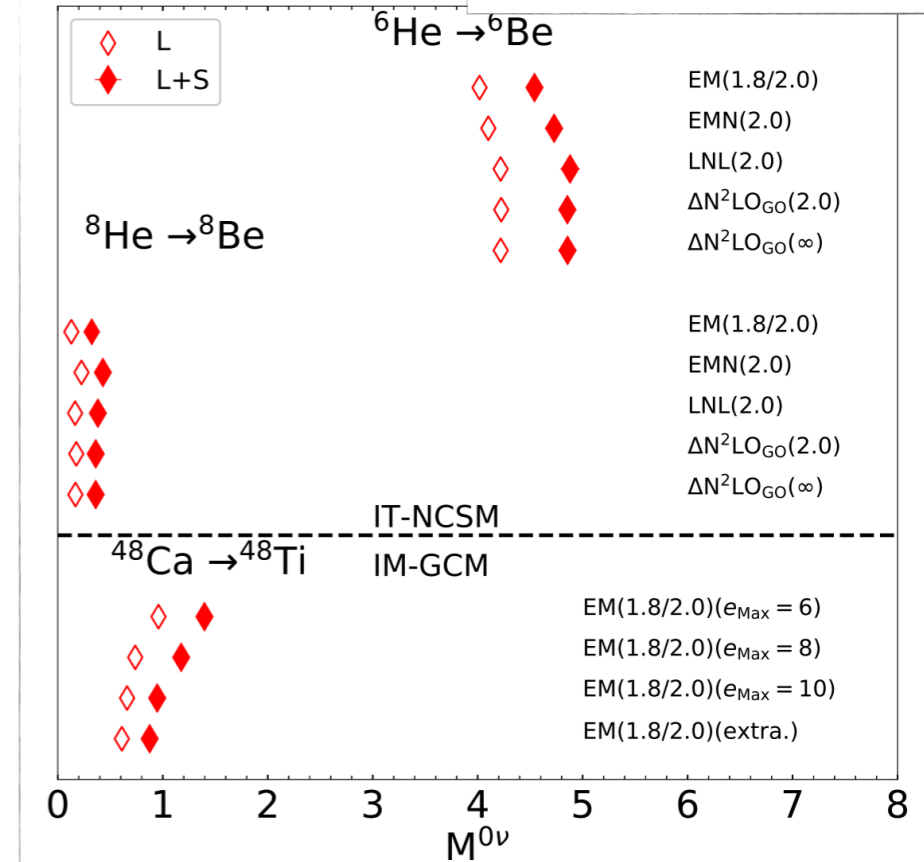
- *Ab initio* NMEs for $A \geq 48$ are starting to appear

Belley et al '23,'20; Yao et al '20; Wirth, Yao, Hergert '21

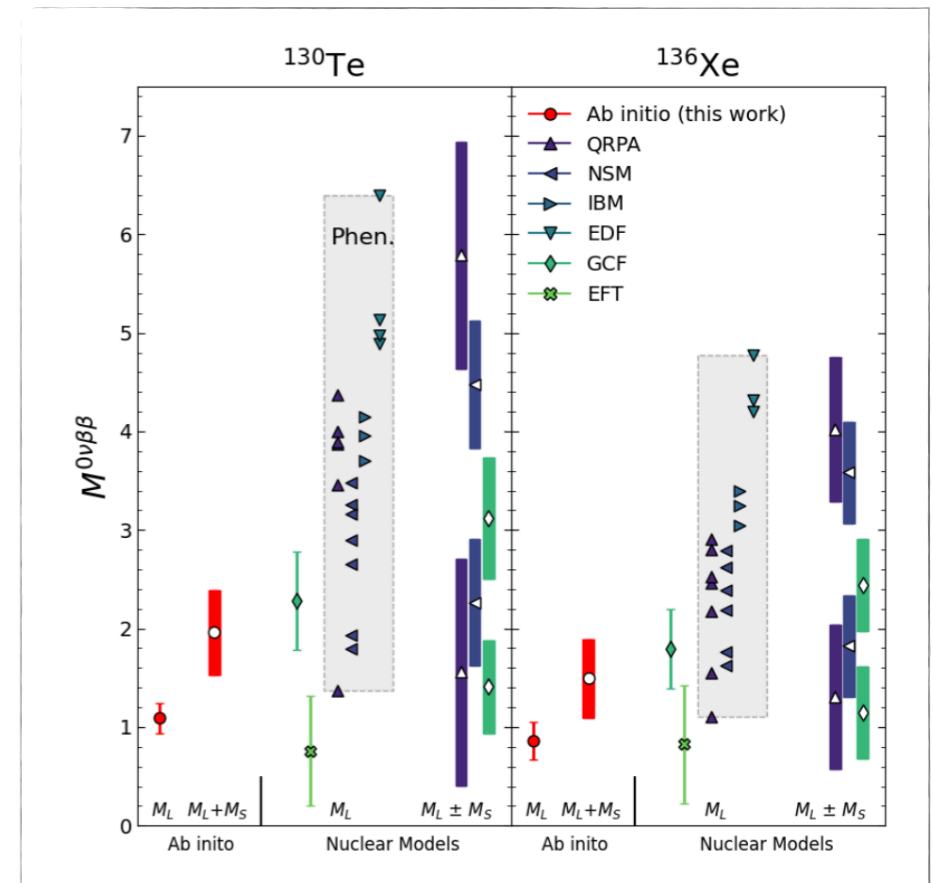
- Can estimate effect of g_ν^{NN} :

- ~40% effect in ^{48}Ca , assuming *Cottingham* estimate g_ν^{NN}
- ~60-90% in Te, Xe

Wirth, Yao, Hergert '21



Belley, Miyagi, Stroberg, Holt, '23

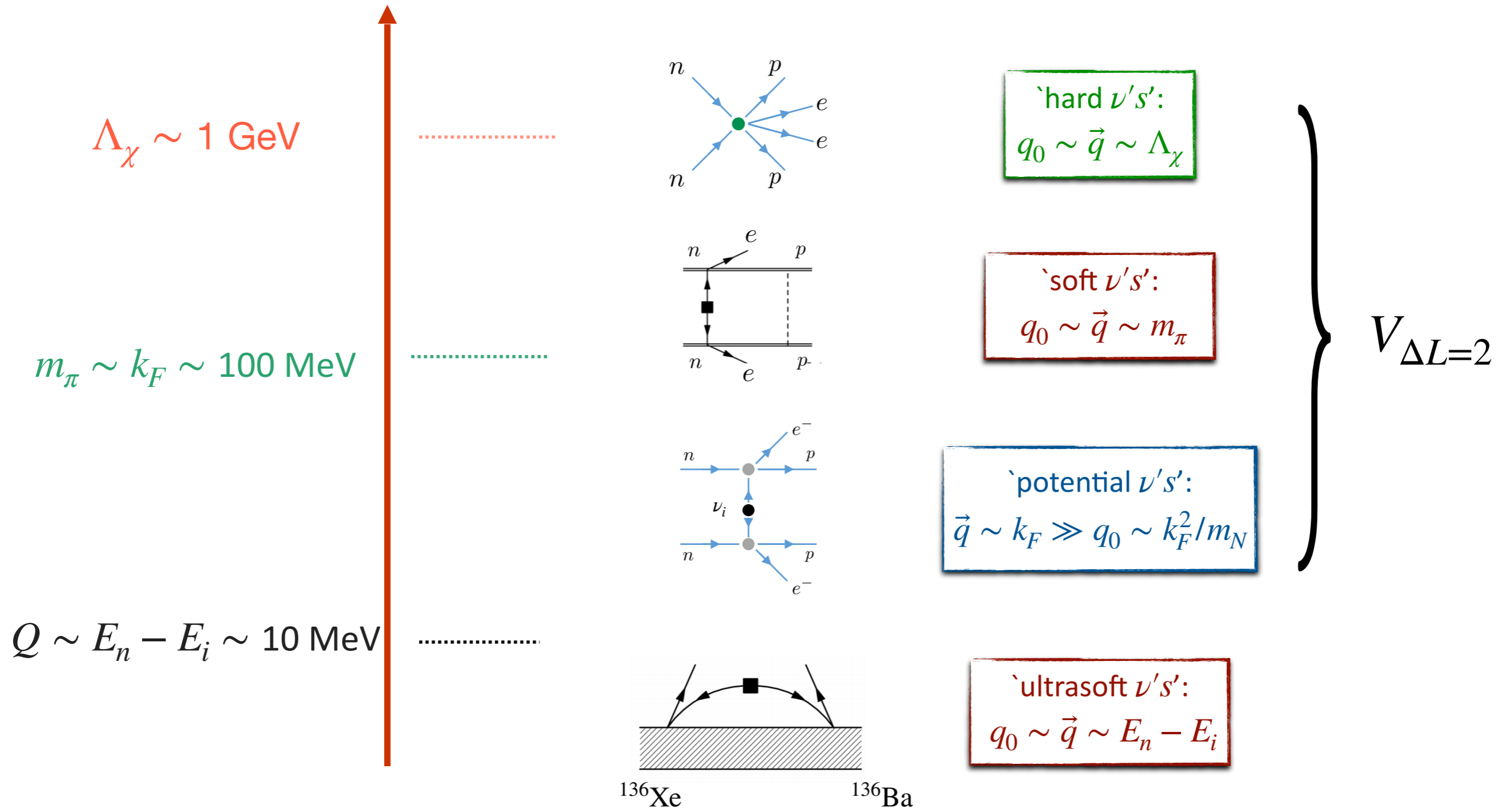


Sterile neutrinos



Momentum scales

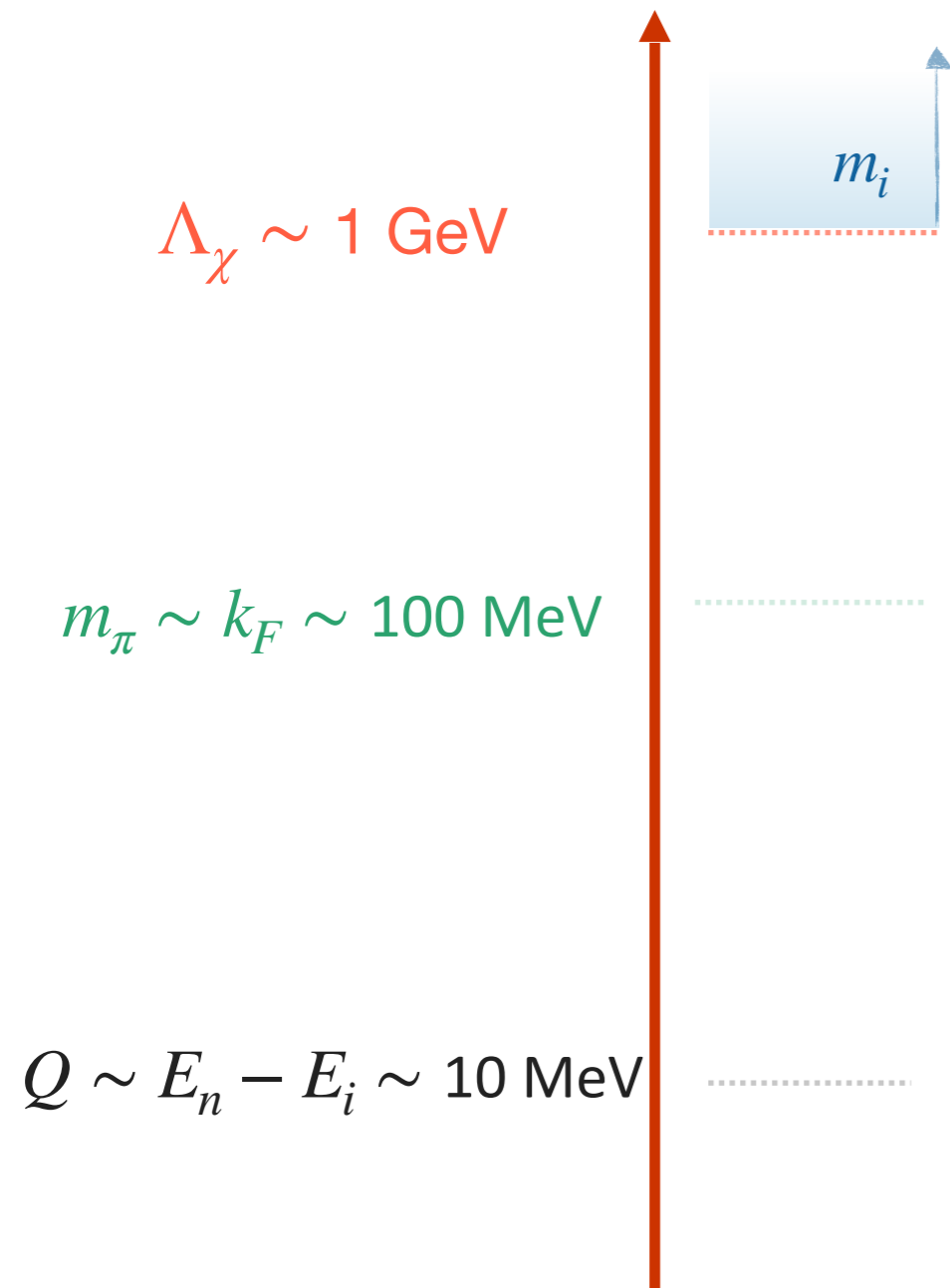
Active + sterile ν 's



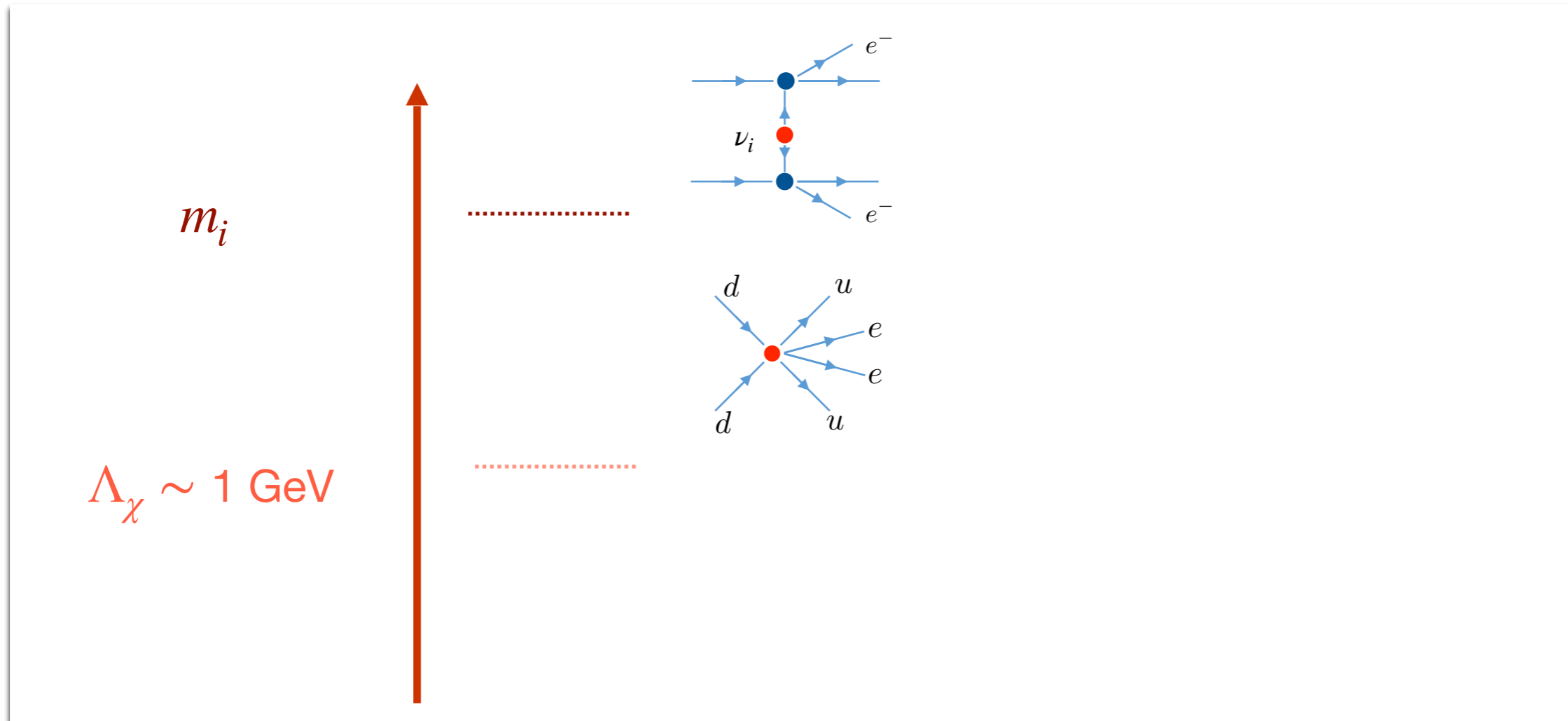
$$A_\nu = \langle ^{136}\text{Ba} | V_{\Delta L=2} | ^{136}\text{Xe} \rangle + A_\nu^{\text{usoft}}$$

EFT approach

One momentum scale at a time

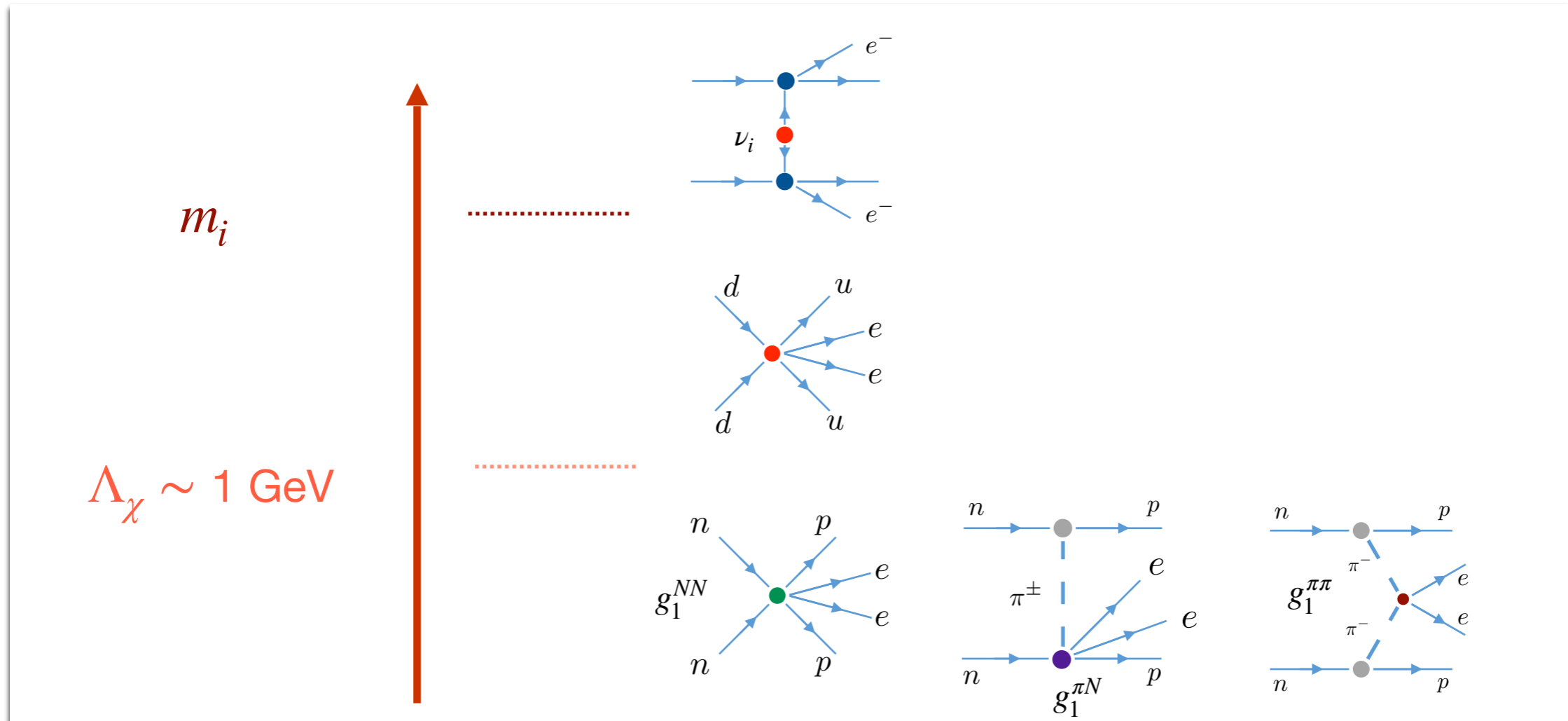


$$m_i \gg \Lambda_\chi$$



- ν_i can be integrated-out at quark level
- Determines m_i dependence: $A_\nu(m_i) \sim U_{ei}^2/m_i^2$

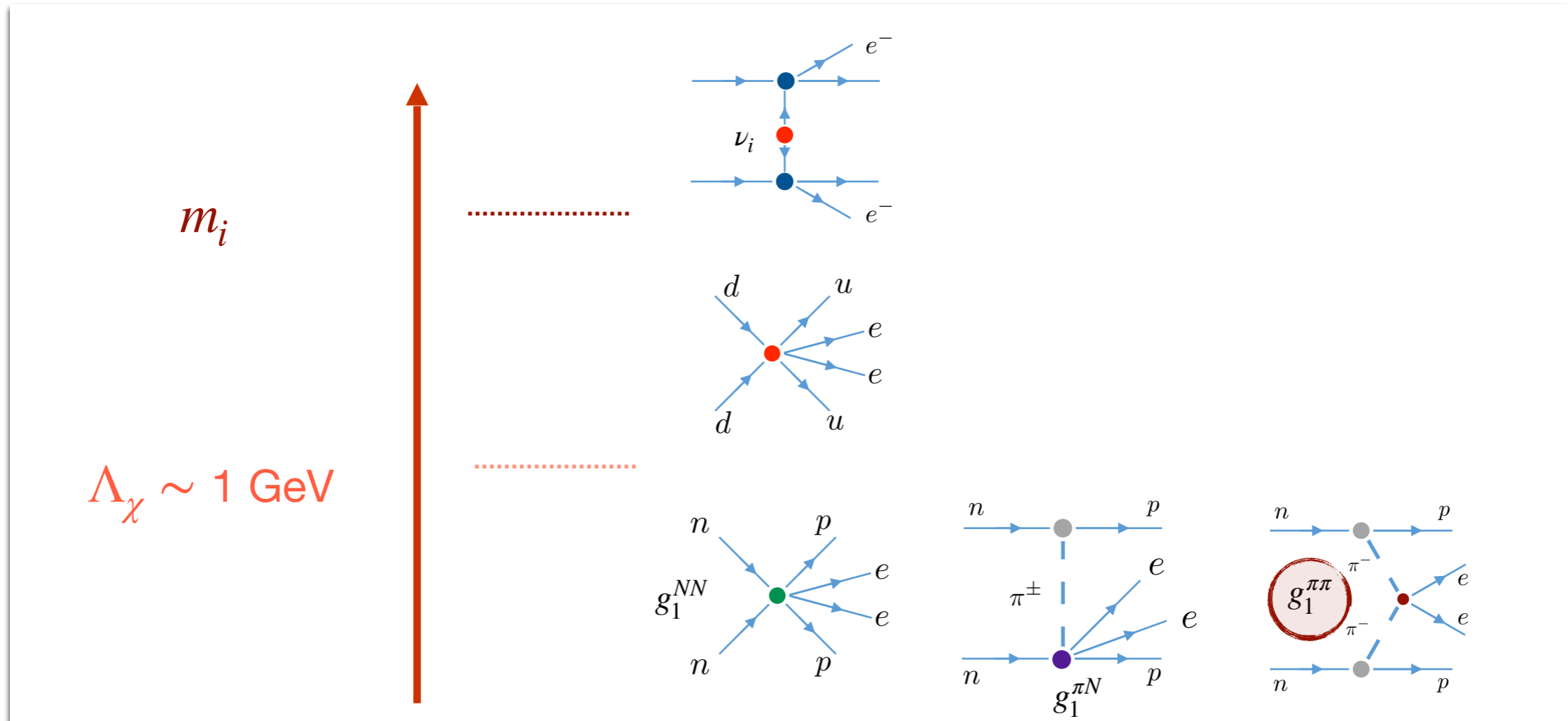
$$m_i \gg \Lambda_\chi$$



- ν_i can be integrated-out at quark level
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- Match to chiral EFT without ν_i
- Involves several LECs

$$m_i \gg \Lambda_\chi$$

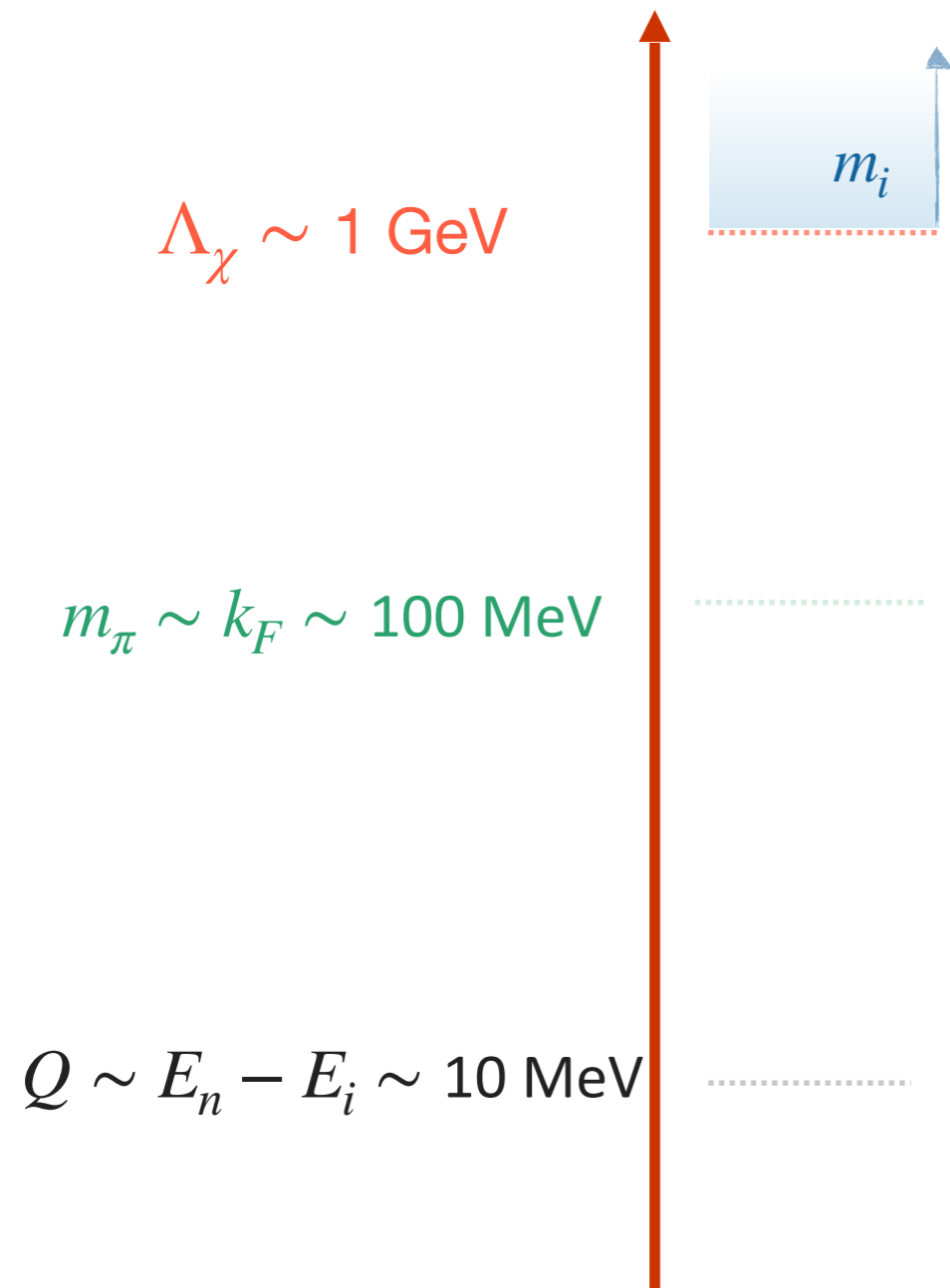


- ν_i can be integrated-out at quark level
- Determines m_i dependence: $A_\nu(m_i) \sim U_{ei}^2/m_i^2$

- Match to chiral EFT without ν_i
- Involves several LECs
 - Only $g_1^{\pi\pi}$ known

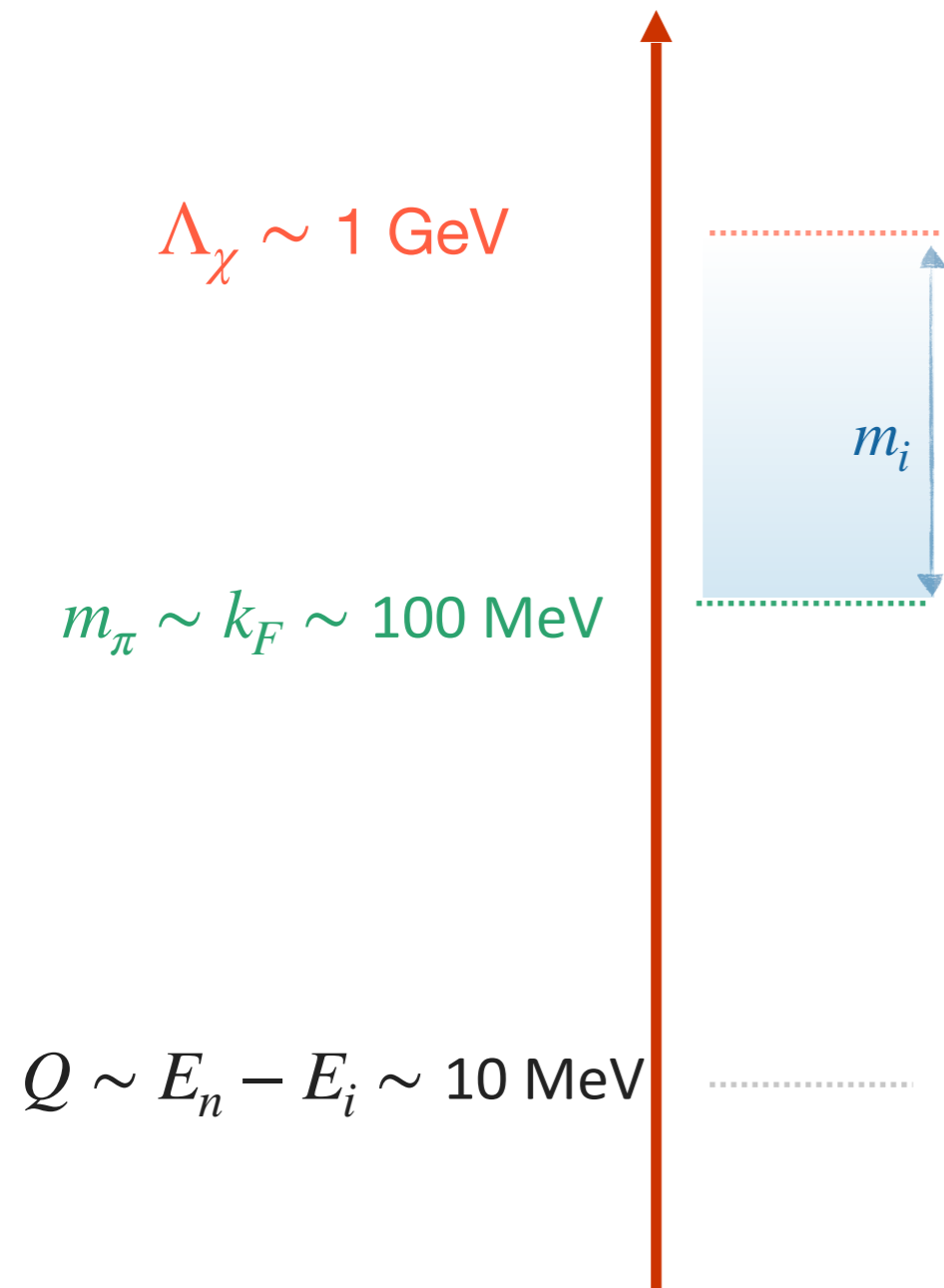
EFT approach

One momentum scale at a time

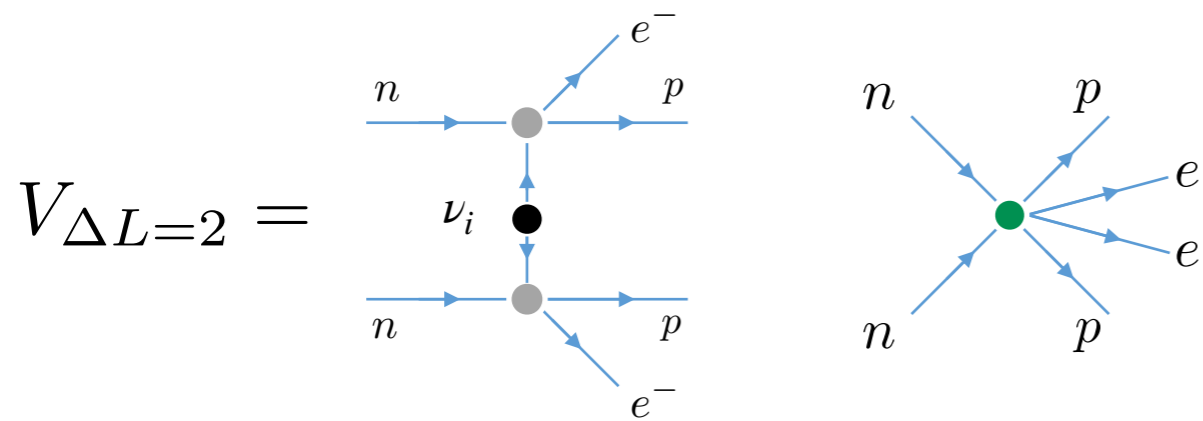


EFT approach

One momentum scale at a time

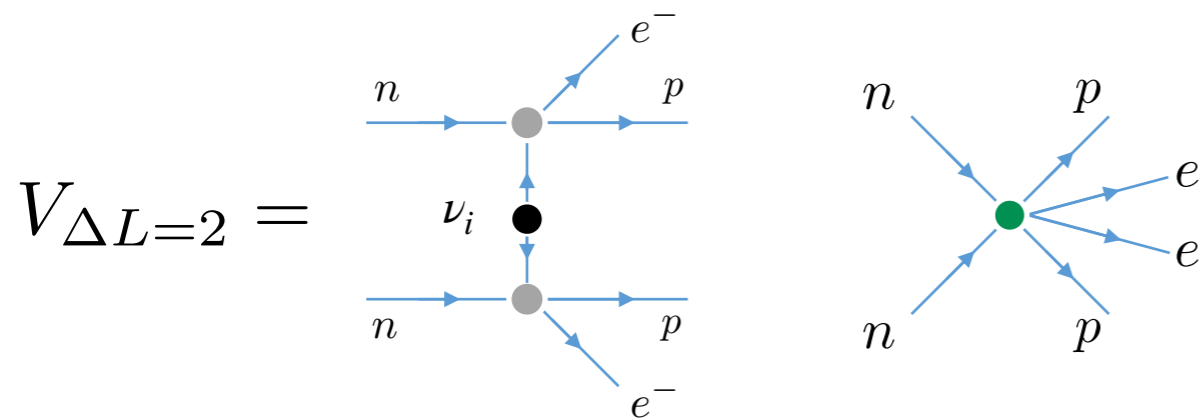


$$\Lambda_\chi \gtrsim m_i \gtrsim k_F$$

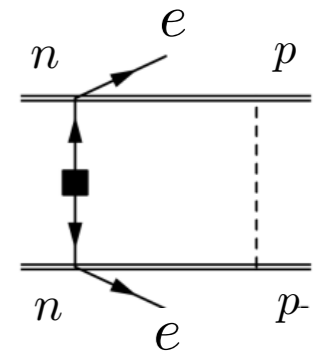


- Have to keep ν_i in the chiral theory
- Again have 'potential' + 'hard' contributions
- m_i dependence in NMEs and g_ν^{NN}

$$\Lambda_\chi \gtrsim m_i \gtrsim k_F$$



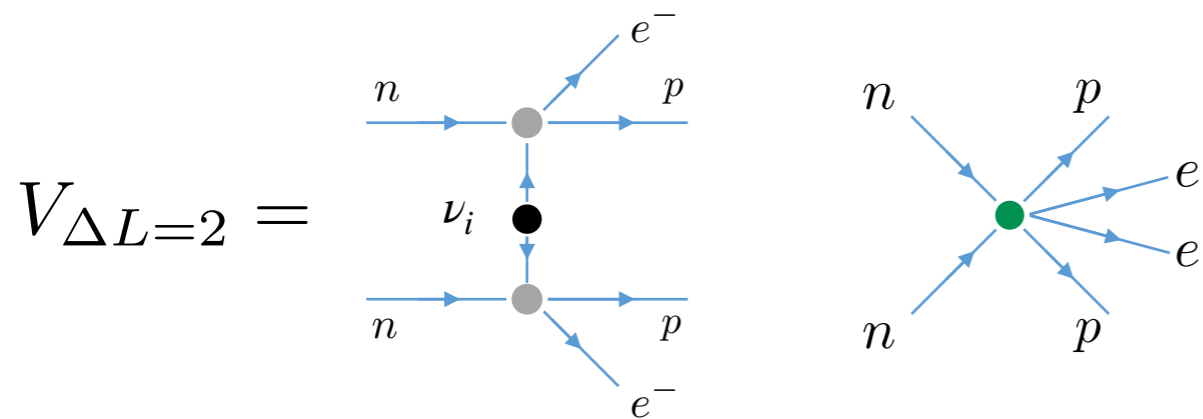
Soft contributions $\mathcal{O}\left(\frac{m_i^2}{\Lambda_\chi^2}\right)$



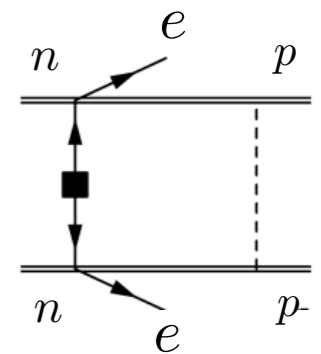
- Have to keep ν_i in the chiral theory
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Soft contributions $\mathcal{O}\left(\frac{m_i^2}{\Lambda_\chi^2}\right)$

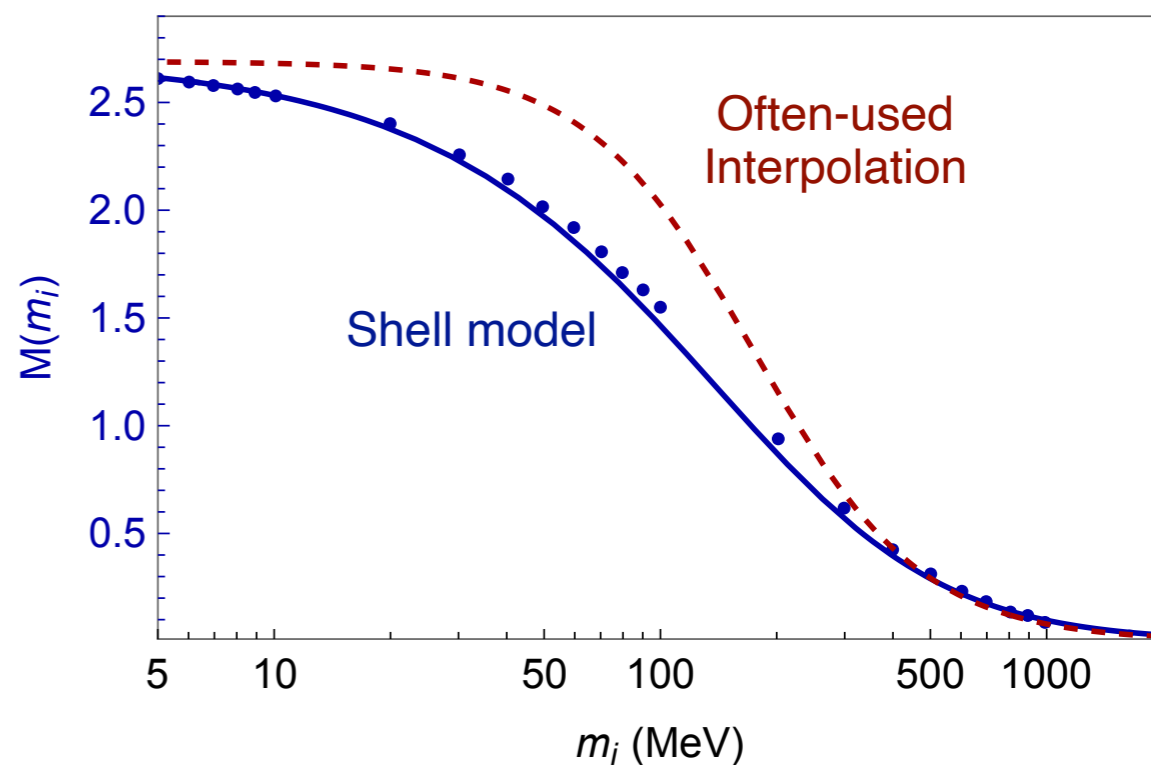


- Have to keep ν_i in the chiral theory
- Again have 'potential' + 'hard' contributions
- m_i dependence in NMEs and g_ν^{NN}

- 'soft' contributions can be significant

Present in usual approach

$$A_\nu(m_i) = A_\nu(0) \frac{\langle p^2 \rangle}{\langle p^2 \rangle + m_i^2}$$



Required NMEs/LECs



Overview

Required input

$$m_i \ll \Delta E$$

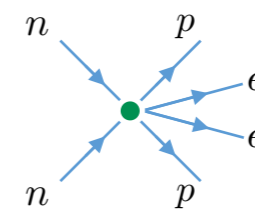
$$\Delta E \ll m_i \ll k_F$$

$$k_F \ll m_i \ll \Lambda_\chi$$

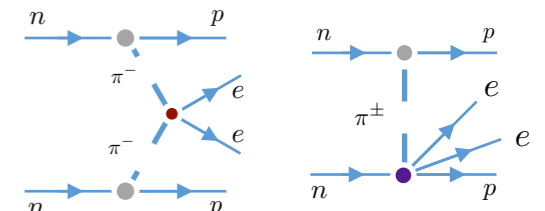
$$\Lambda_\chi \ll m_i$$

Low-energy constants

$$g_\nu^{NN}(m_i)$$



$$g_1^{\pi\pi}, g_1^{\pi N}, g_1^{NN}$$



Nuclear matrix elements

$$M_\nu(m_i) = \langle f | V | i \rangle$$

$$\langle f | \tau^+ \sigma | n \rangle$$

$$\Delta E \sim E_n - E_i$$

$M_\nu^{\text{short-distance}}$

- Known from LQCD
- Use NDA for $g_1^{\pi N}, g_1^{NN}$
- Interpolate g_ν^{NN} between $m_i = 0$ and $m_i \gg \Lambda_\chi$ regions

- Shell model calculations for the NMEs

Phenomenology with sterile neutrinos



Phenomenology

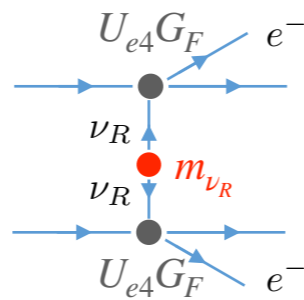
From heavy new physics + light ν_R

Example with ν_R

- Toy Model

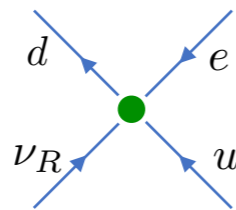
- SM + 1 light ν_R

$$\Gamma_{0\nu\beta\beta} \sim$$



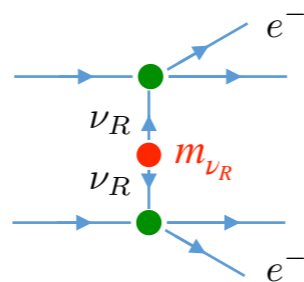
- Add dimension-six interaction

- SM + 1 light ν_R +

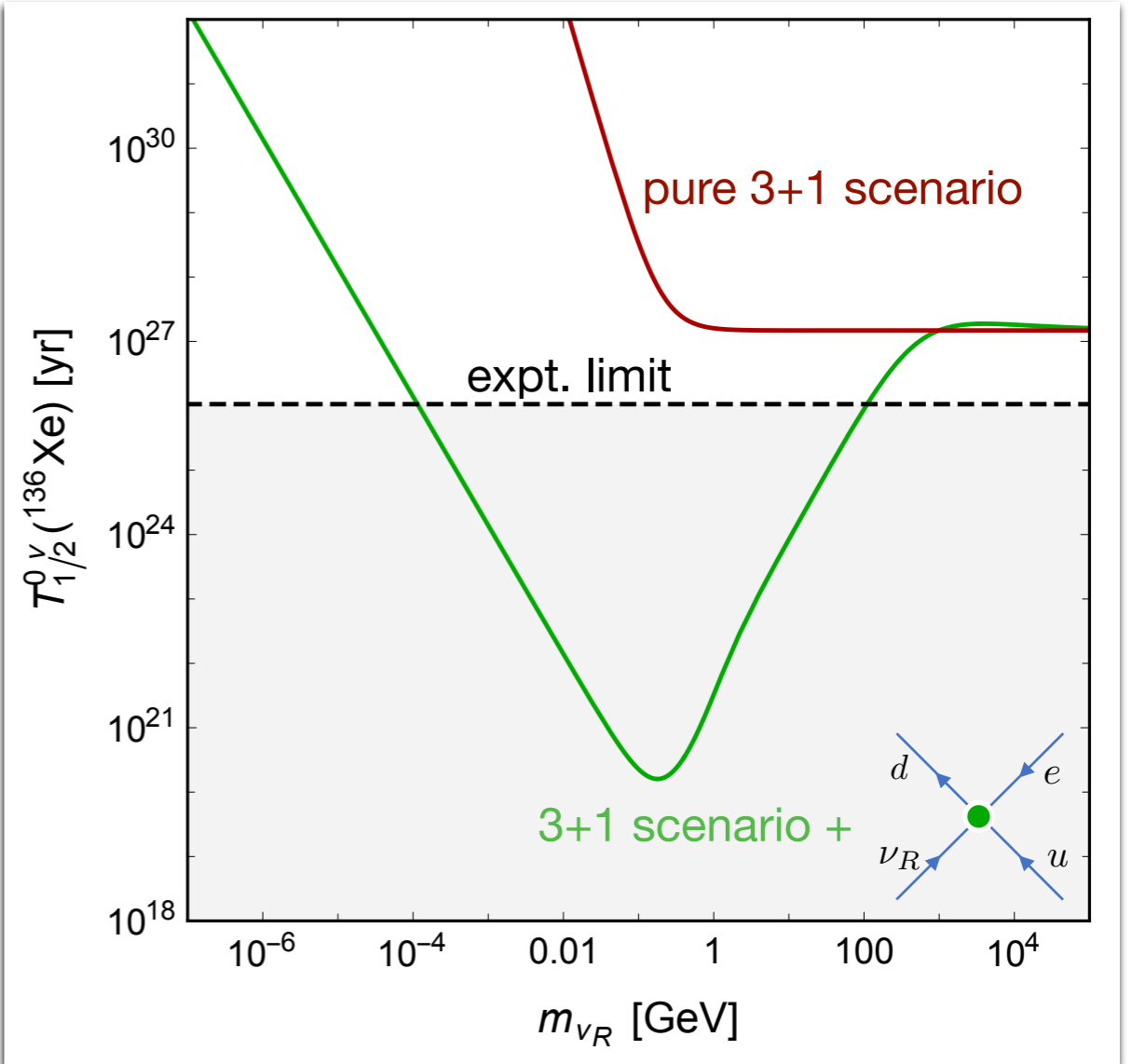


$$\Lambda = 10 \text{ TeV}$$

$$\Gamma_{0\nu\beta\beta} \sim$$



O(100%) uncertainties not shown



- Higher dimensional ν_R terms can have a large impact!