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# Stranger Things

- Investigating Hyperon Structure at the Femtometer Scale

25<sup>th</sup> European Conference on Few-body Problems in Physics  
Mainz, Germany, 2023-08-04

Prof. Dr. Karin Schönning, Uppsala University



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# Outline

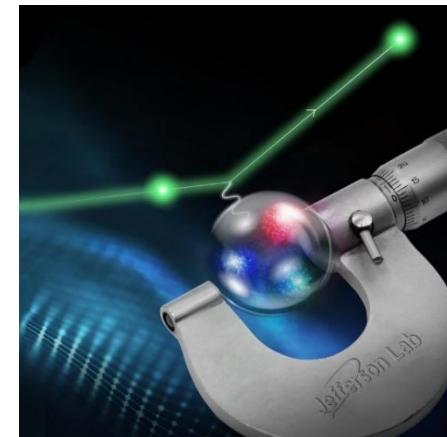
- Prologue
- Electromagnetic Form Factors
- Recent results from BESIII
- Summary

# Prologue

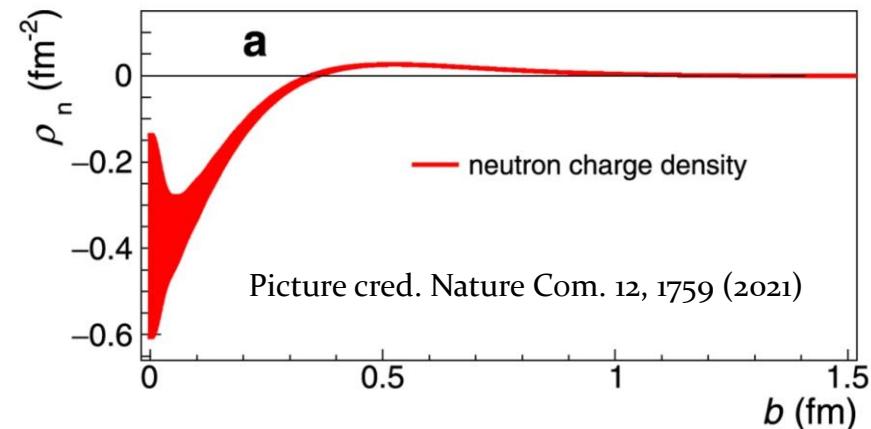
Strong interactions manifest in e.g. hadron **structure** and **size**  
→ quantities at the femtometer scale!

**Protons:** rapid progress the last  $\sim 5$  years!\*

**Neutrons:** asymmetric distribution  
of  $d$  quarks and  $u$  quark results in a  
negative squared charge  
radius  $\langle r_E^2 \rangle$ .\*\*



Picture cred. Y-H Lin, U. Bonn

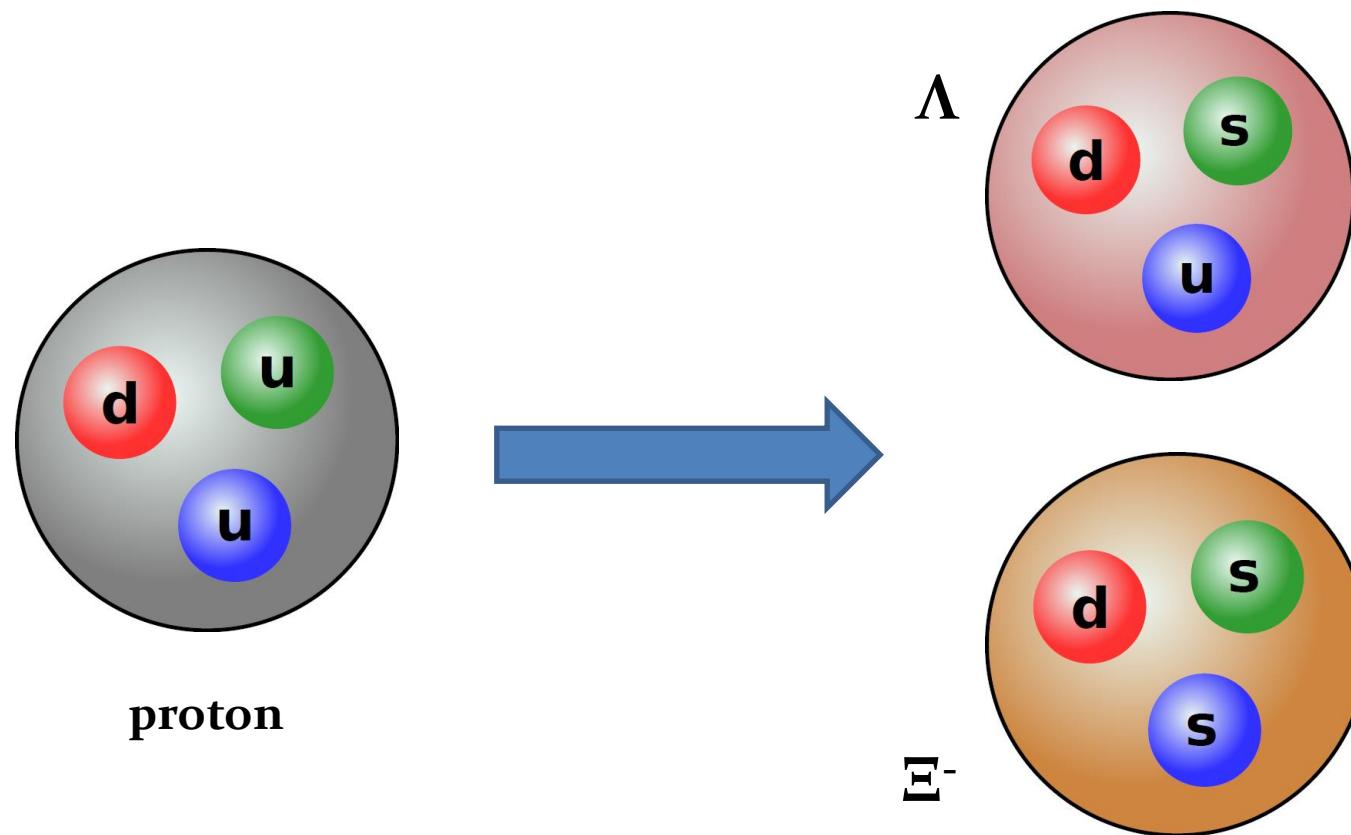


\*Talk by U.G. Meissner (Monday)

\*\*Atac *et al.*, Nature Com. 12, 1759 (2021)

# Prologue

**FAQ1:** How does the presence of heavy strange and charm quarks affect the strong interaction dynamics?



# Prologue

To find out, we first need to answer FAQ2:

*How can we study the structure of unstable hadrons?*

**Proton:**  $\tau > 10^{34}$  y

**Neutron:**  $\tau \sim 15$  min

**Strange hyperons:**  $\tau \sim 10^{-10}$  s

**Charm hyperons:**  $\tau \sim 10^{-13}$  s

# Prologue

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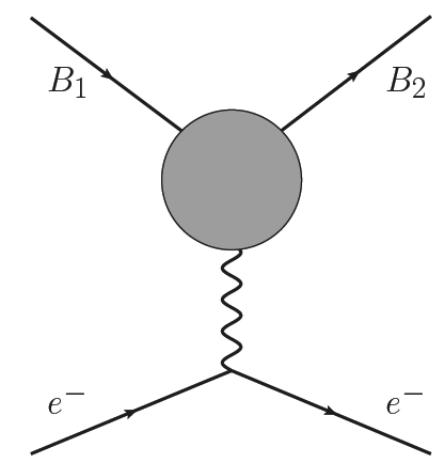
**Charm hyperons:**  $\tau \sim 10^{-13}$  s

Answer: By time-like  
electromagnetic form factors!

# Space-like vs. time-like EMFF's

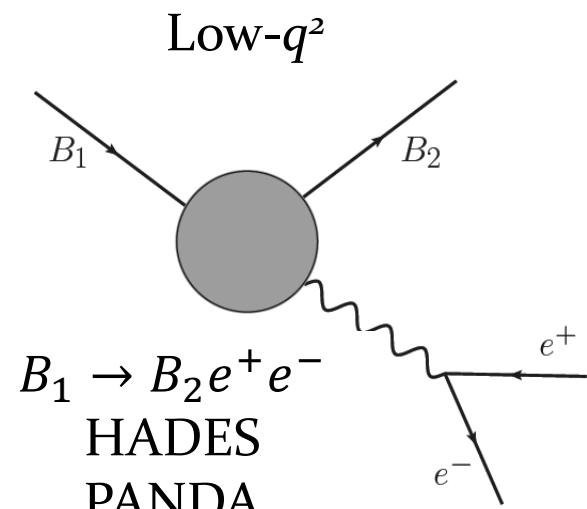
Space-like

$$q^2 < 0$$



Time-like

$$q^2 > 0$$

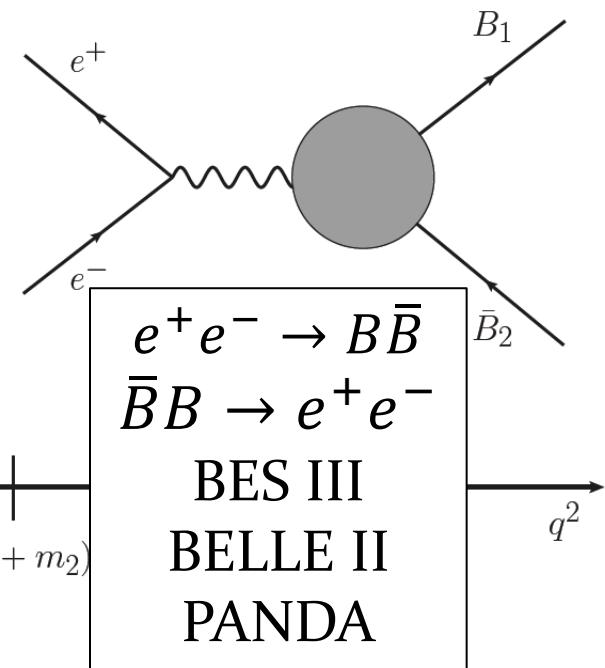


$e^-B \rightarrow e^-B$   
e.g. JLAB

$$0 \quad 4m_e^2$$

$$0 \quad 4m_e^2 \quad (m_1 - m_2)^2 \quad (m_1 + m_2)$$

High- $q^2$

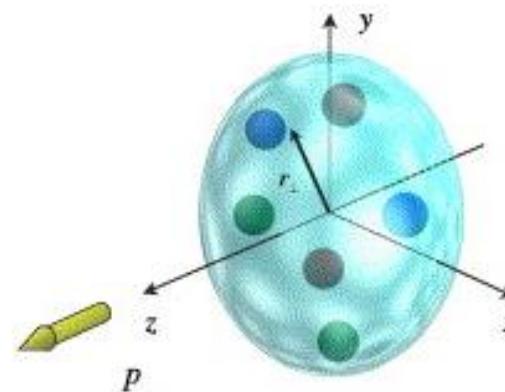


# Space-like form factors

- Number of EMFFs =  $2J+1 \rightarrow$  spin  $\frac{1}{2}$  baryons have 2.
- Sachs FFs: the electric  $G_E$  and magnetic  $G_M$

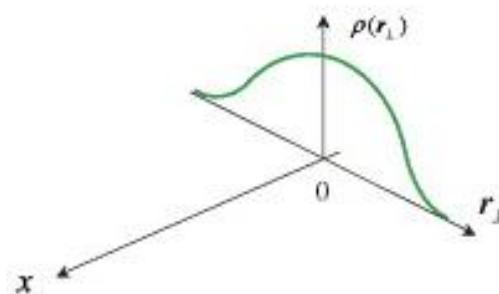
– Charge radius:

$$\langle r_E^2 \rangle = 6 \frac{dG_E(q^2)}{dq^2} \Big|_{q^2=0}$$



– Magnetic radius:

$$\langle r_M^2 \rangle = \frac{6}{G_M(0)} \frac{dG_M(q^2)}{dq^2} \Big|_{q^2=0}$$



# Space-like vs. time-like FF's

Space-like

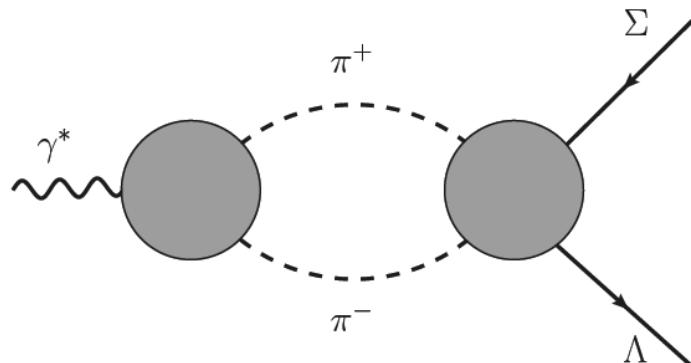


Time-like



# Time-like form factors

- Related to space-like EMFFs *via* dispersion relations.
  - Are complex:
    - $G_E(q^2) = |G_E(q^2)| \cdot e^{i\Phi_E}$  ,  $G_M(q^2) = |G_M(q^2)| \cdot e^{i\Phi_M}$
    - Ratio  $R = \frac{|G_E(q^2)|}{|G_M(q^2)|}$  accessible from baryon scattering angle.
    - $\Delta\Phi(q^2) = \Phi_M(q^2) - \Phi_E(q^2)$  = phase between  $G_E$  and  $G_M$
    - Phase a reflection of intermediate fluctuations of the  $\gamma^*$  into e.g.  $\pi\pi$ .
- Polarizes final state!



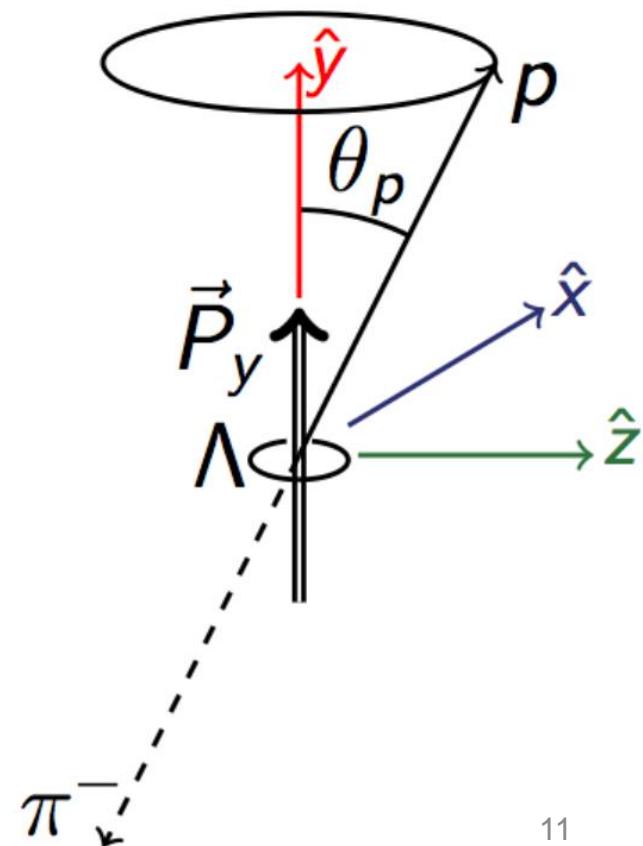
Picture credit:  
Elisabetta Perotti, PhD Thesis,  
UU (2020)

# Advantage of hyperons

Polarization experimentally accessible  
by the weak, parity violating decay:

Example:

$$I(\cos\theta_p) = N(1 + \alpha_\Lambda P_\Lambda \cos\theta_p)$$



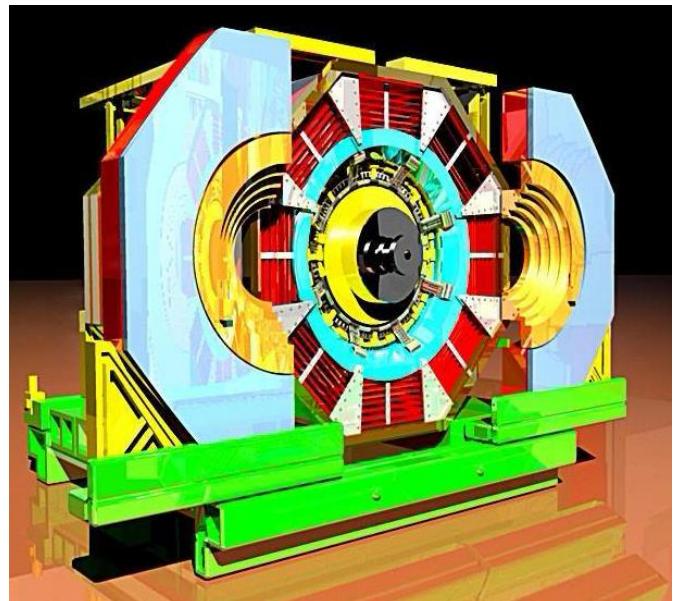
# Space-like vs. Time-like EMFFs

- **Onset of asymptotic scale**  $q_{asy}^2$  where SL = TL
  - Nucleons: SL and TL accessible.
  - Hyperons: Only TL accessible, but also phase!  
 $\Delta\Phi(q^2) \rightarrow 0 \leftrightarrow SL = TL$
- **Zero crossings\***: Existence and location in the SL region from the TL behaviour!

# The BESIII experiment

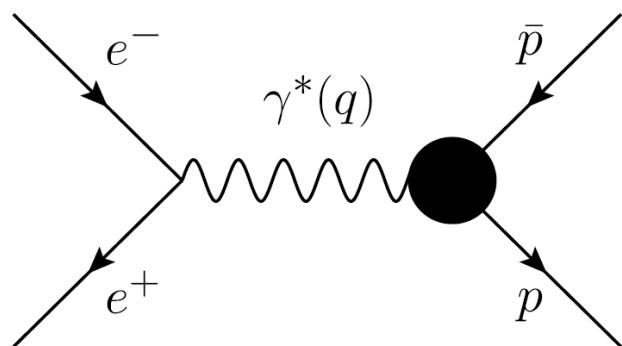
- Study  $e^+e^- \rightarrow B\bar{B}$ , where  $B = p, n, \Lambda, \Sigma, \Xi, \Lambda_c^+$
- Beijing Electron Positron Collider (BEPC II):
  - $e^+e^-$  collider within CMS range 2.0 – 4.95 GeV.
- Beijing Spectrometer (BES III):
  - Near  $4\pi$  coverage
  - Tracking, PID, Calorimetry
  - Broad physics scope

**BESIII**



# $B\bar{B}$ production in BESIII

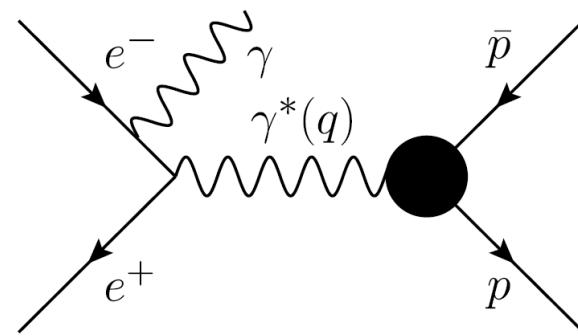
## Energy Scan



$$e^+e^- \rightarrow B\bar{B}$$

- Simple final state
- "Simple" formalism → Straight-forward to analyze
- Requires dedicated data campaigns

## Initial State Radiation (ISR)



$$e^+e^- \rightarrow e^+e^-\gamma_{ISR} \rightarrow \gamma_{ISR}B\bar{B}$$

- ISR photon tagged or untagged
- Effective cross section much smaller than in direct  $e^+e^- \rightarrow B\bar{B}$
- Possible to benefit from large data samples collected at *e.g.*  $J/\Psi$

# Production cross sections

- Energy dependence give information about the quark dynamics through
  - The *effective form factor*:  $G_{eff} \propto \sqrt{\sigma}$
  - Di-quark correlations
  - Coupling to vector mesons and/or  $B\bar{B}$  bound states
- Convenient for studies of
  - protons and (semi-) stable neutrons
  - small hyperon data samples

# Proton and neutron EMFFs

Picture credit SND: Eur. Phys. J. C (2022) 82: 761

Energy dependence of  $G_{eff}$ :

$$G_{eff} = G_0 + G_{osc}$$

$G_0$ : Dipole-like

$G_{osc}$ : Oscillations

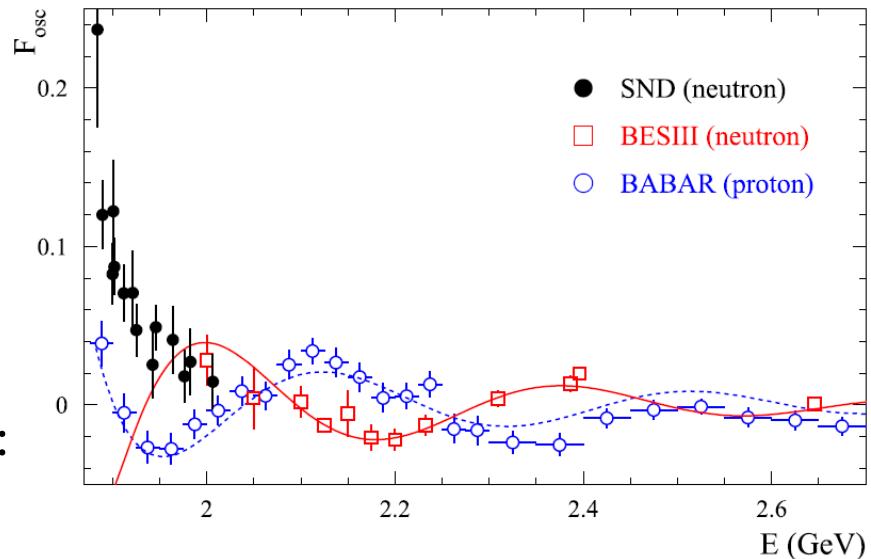
BESIII:  $G_{osc}(p)^*$  and  $G_{osc}(n)^*$  \*\*

have same frequency but different phase:

$$\Delta D = D_p - D_n = 125^\circ \pm 12^\circ$$

SND: Smaller frequency for neutron oscillations\*\*\*.

See also talk by U.G. Meissner



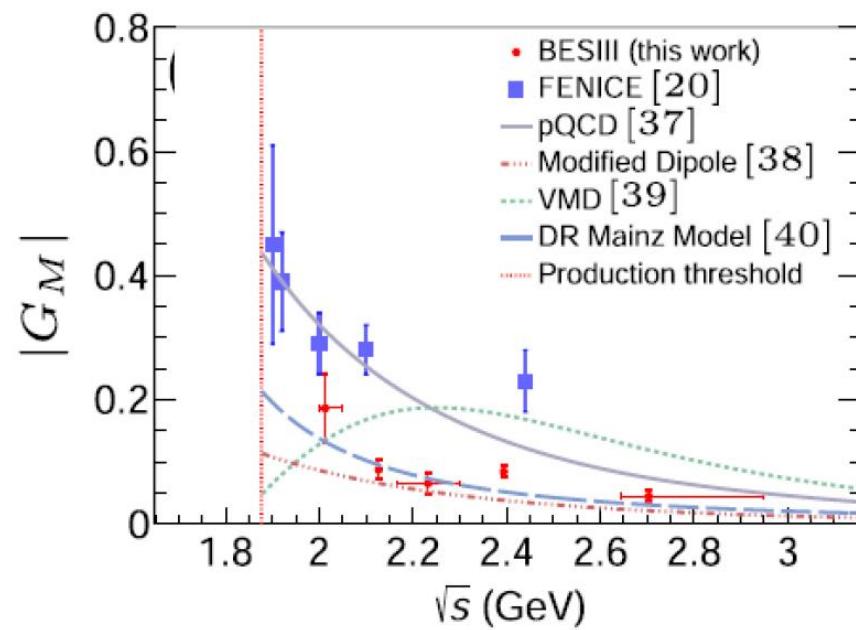
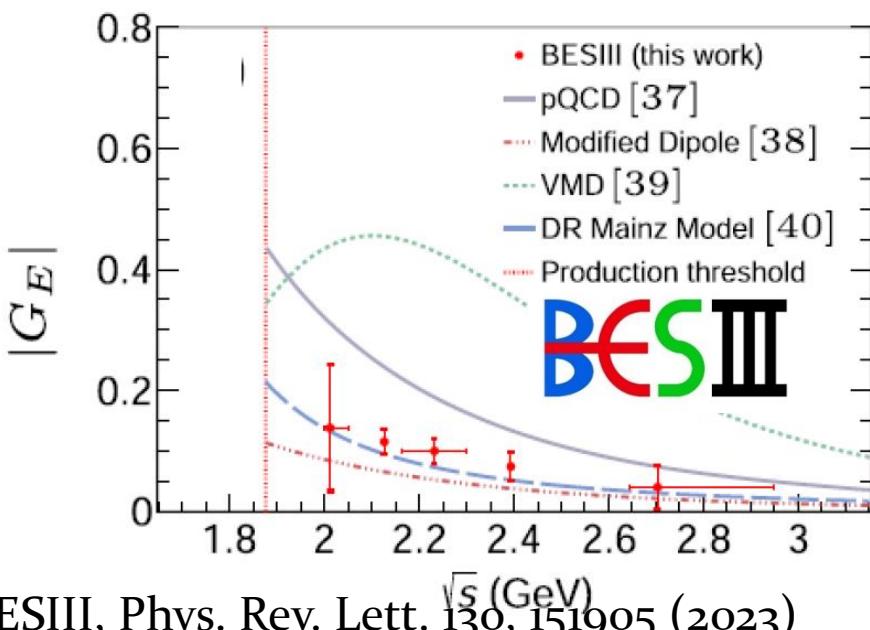
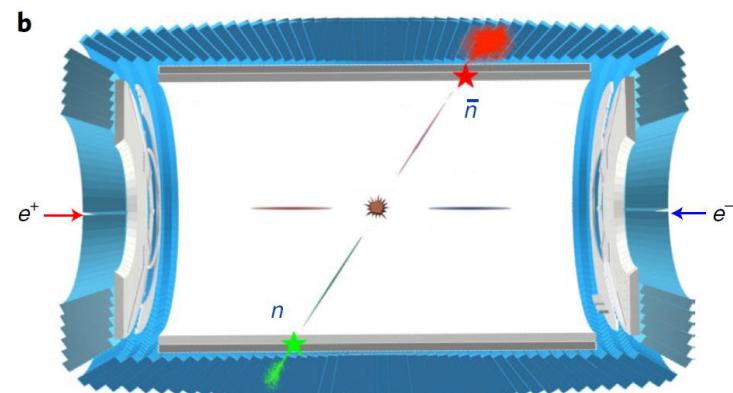
**BESIII proton EMFFs:**  
 Phys. Rev. D 91, 112004 (2015)  
 Phys. Rev. D 99, 092002 (2019)

Phys. Rev. Lett. 124, 042001 (2020)  
 Phys. Lett. B 817, 136328 (2021)

**BESIII neutron EMFFs:**  
 BESIII, Nature Phys. 17, p 1200–1204 (2021)  
 BESIII, Phys. Rev. Lett. 130, 151905 (2023)  
**SND:** Eur. Phys. J. C (2022) 82, 761

# Neutron EMFFs

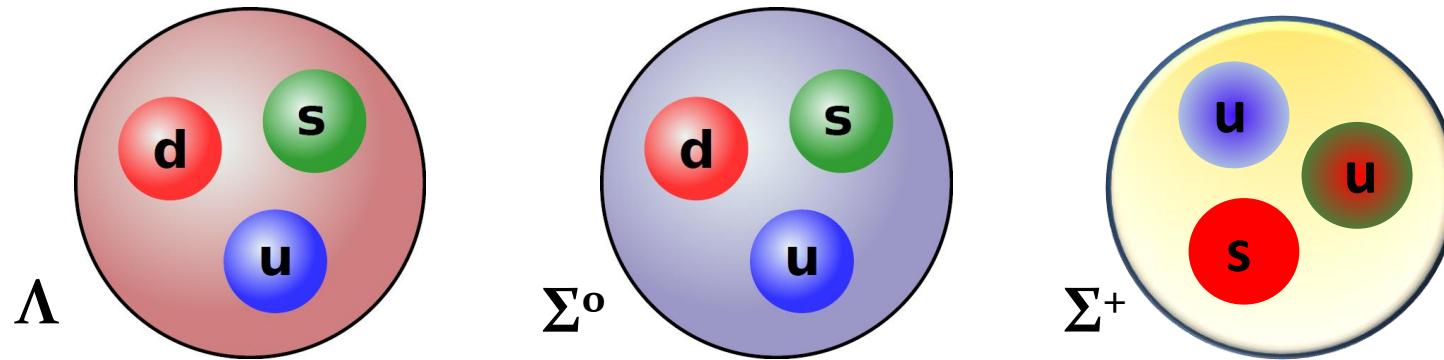
- New BESIII study\*: Production angle distribution enables separation of electric  $G_E$  and magnetic  $G_M$ 
  - First measured neutron time-like  $G_E$  !
  - Agreement with dispersive calculations, but not FENICE data.



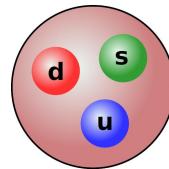
# Single-strange hyperons

Diquark correlations in baryons?

- The  $\Sigma^0$  has isospin 1 whereas  $\Lambda$  has isospin 0
  - Strange quark has no isospin → difference is in the  $ud$  diquark
  - different spin structure
  - different cross sections expected.\*
- In  $\Sigma^+$ , the  $uu$  should have same spin structure as the  $ud$  in  $\Lambda$ .
  - Similar cross sections expected.\*

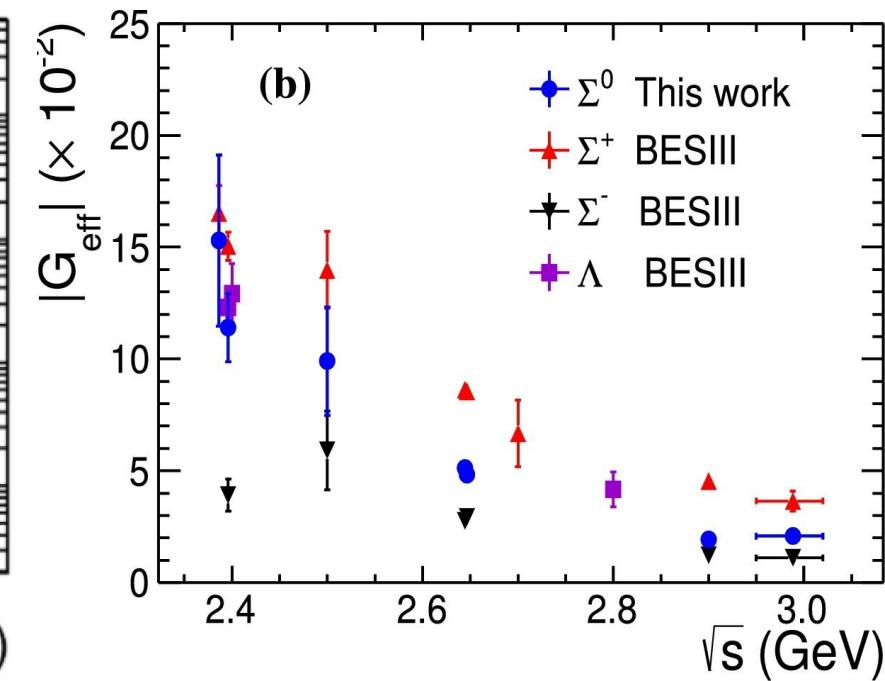
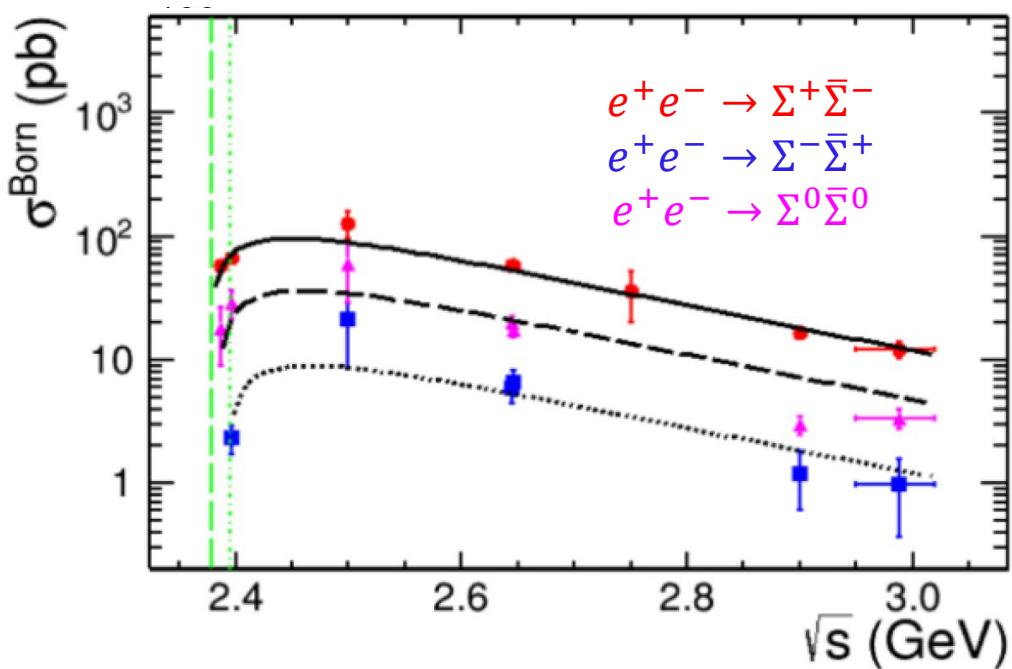


\*Dobbs et al.,: Phys. Lett. B 739, 90 (2014)



# $\Lambda$ and $\Sigma$ hyperons

- Scan data between 2.386 GeV and 2.98 GeV.
- $\Lambda/\Sigma^+$   $G_{eff}$  similar as expected from diquark correlations.<sup>\*, \*\*, \*\*\*</sup>
- $\Sigma^+/\Sigma^-$  cross section ratio  $\sim 9^{**}$

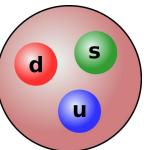


\* BESIII: Phys. Lett. B 831, 137187 (2022)

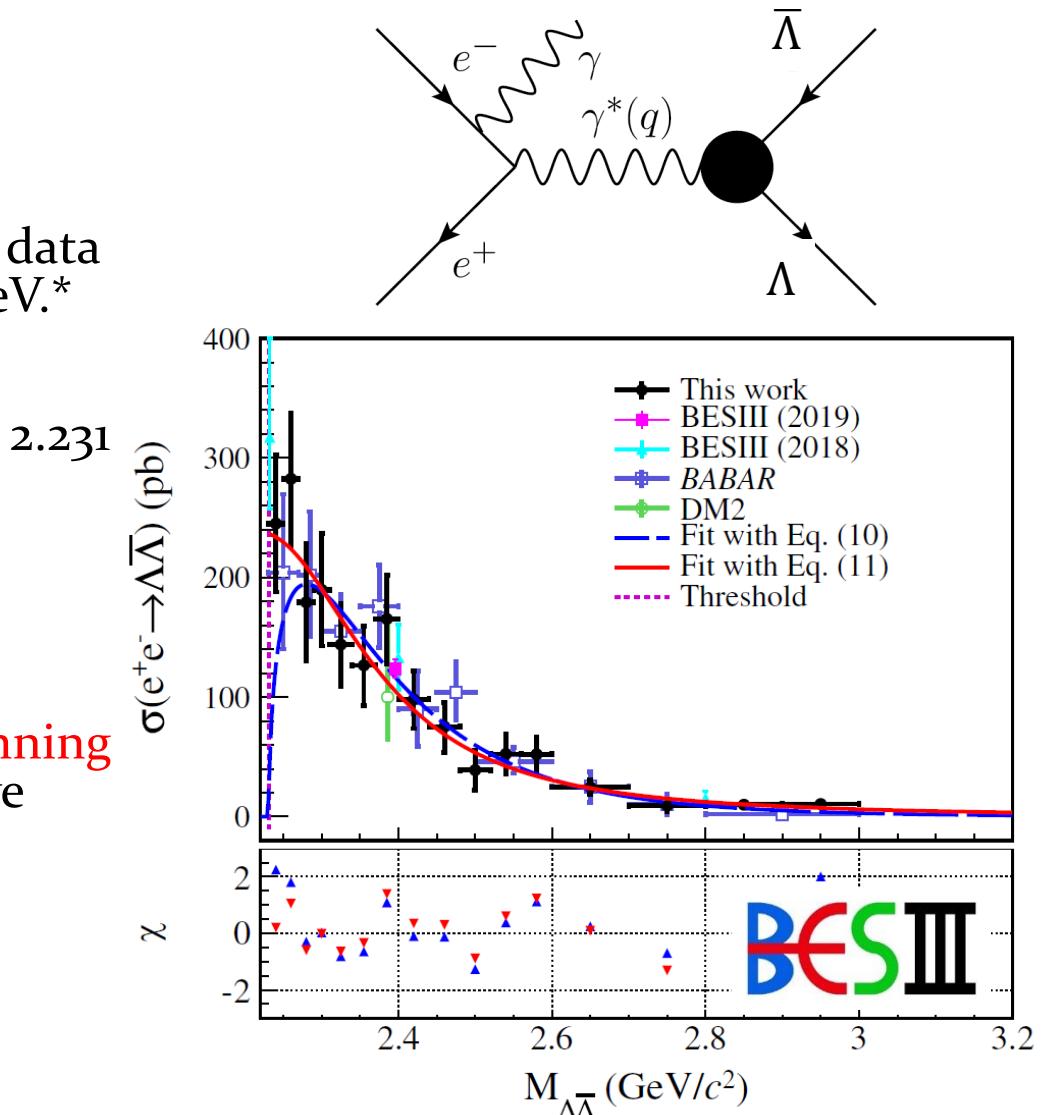
\*\* BESIII: Phys. Lett. B 814, 136110 (2021)

\*\*\* BESIII: Phys. Rev. D 97, 032013 (2018)

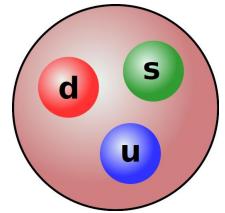
# New: $\Lambda$ production with ISR



- ISR method applied on  $12 \text{ fb}^{-1}$  of data between  $3.773 \text{ GeV}$  and  $4.258 \text{ GeV}$ .\*
- The  $e^+e^- \rightarrow \Lambda\bar{\Lambda}$  cross section measured at 16 energies  $3.0 \text{ GeV}$ .
- Cross section enhancement at threshold confirmed.
- Fit accounting for the **strong running coupling** near threshold into give better agreement than a pQCD approach.

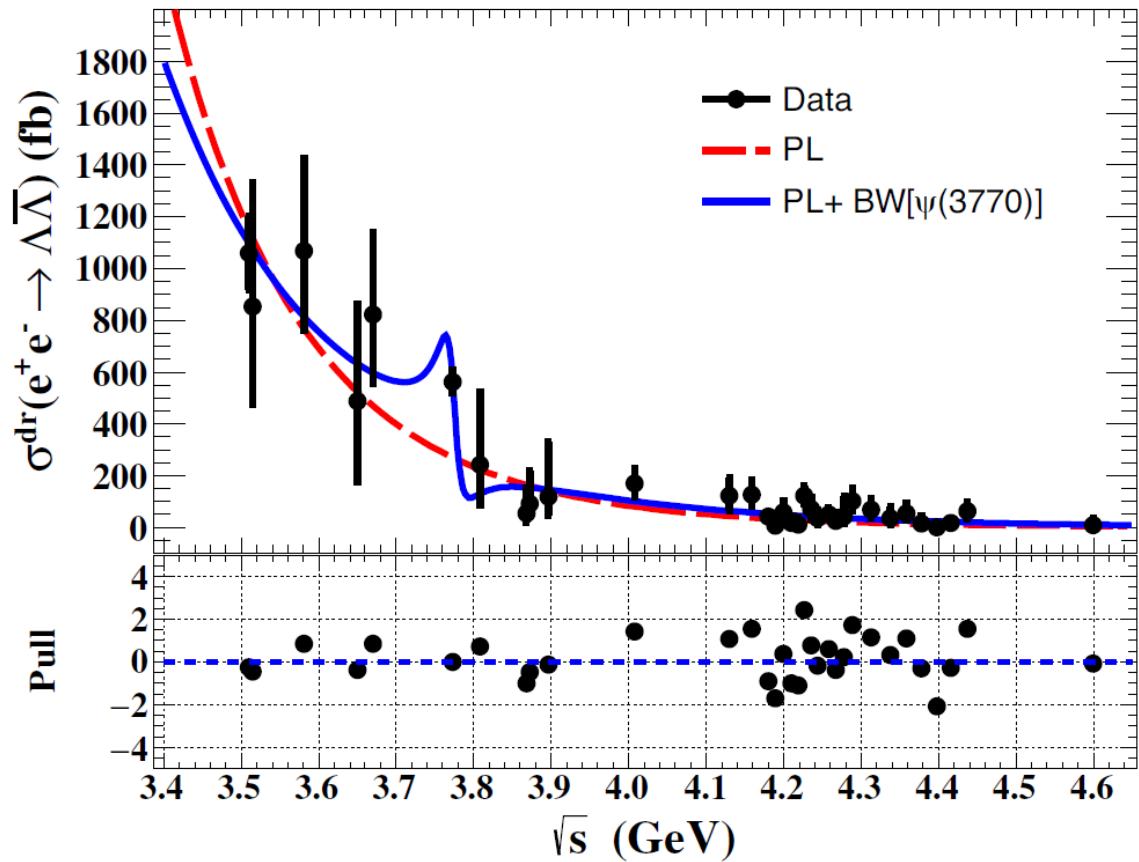


# Production of $\Lambda$ at high $q^2$



- $\Lambda\bar{\Lambda}$  production near vector charmonia\*, \*\*
- $BR(\Psi \rightarrow \Lambda\bar{\Lambda}) > 10$  times larger than assumed in previous studies by CLEO-c\*\*\*.

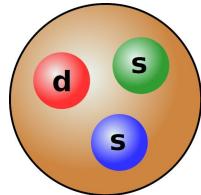
**BESIII**



\* BESIII: Phys. Rev. D 104, L091104 (2021)

\*\* BESIII: Phys. Rev. D 105, L011101 (2022)

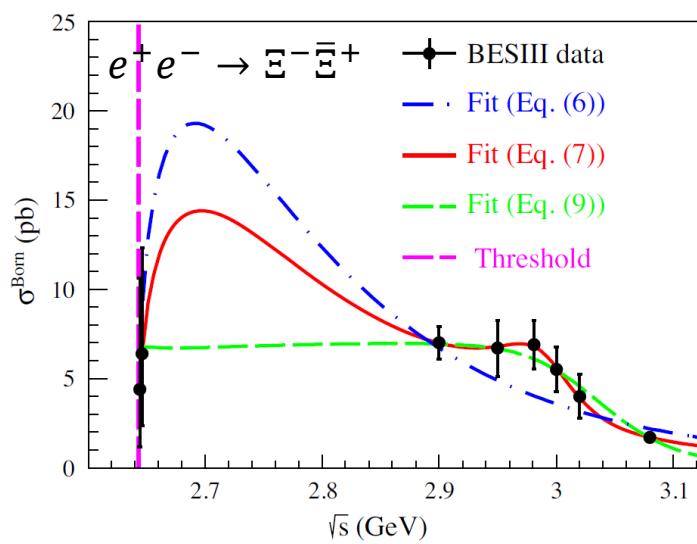
\*\*\* Dobbs *et al.*: Phys. Rev. D 96, 092004 (2017); Phys. Lett. B 739, 90 (2014)



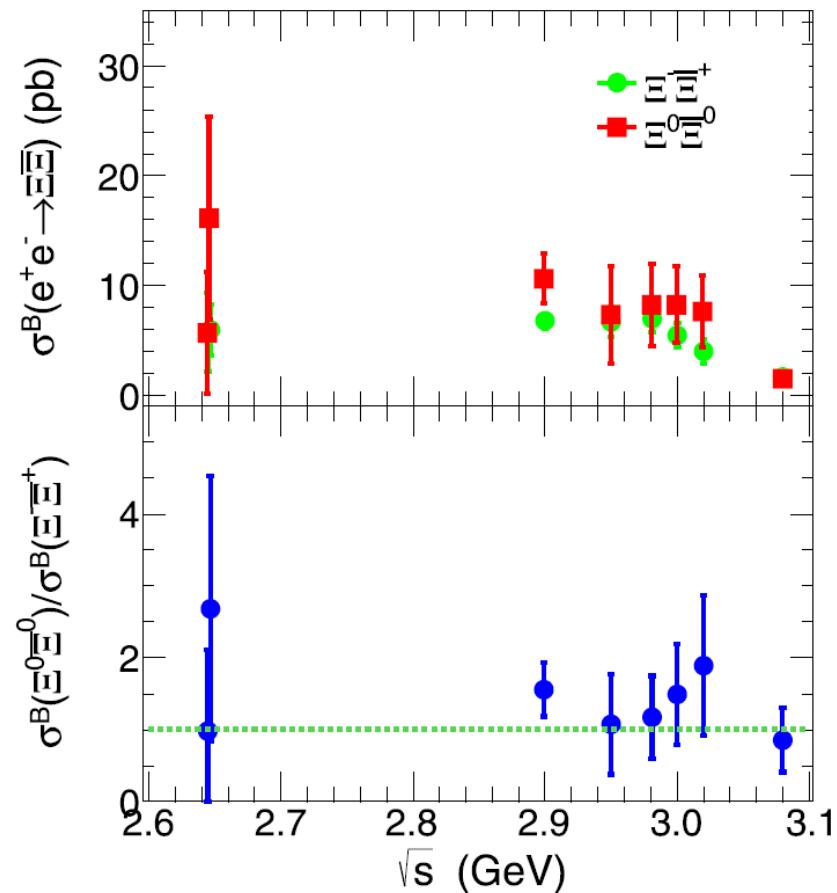
# Double-strange $\Xi$ hyperons

- $e^+e^- \rightarrow \Xi^-\bar{\Xi}^+$  and  $e^+e^- \rightarrow \Xi^0\bar{\Xi}^0$  studied for the first time.
- Possible resonance around 3 GeV.

**BESIII**



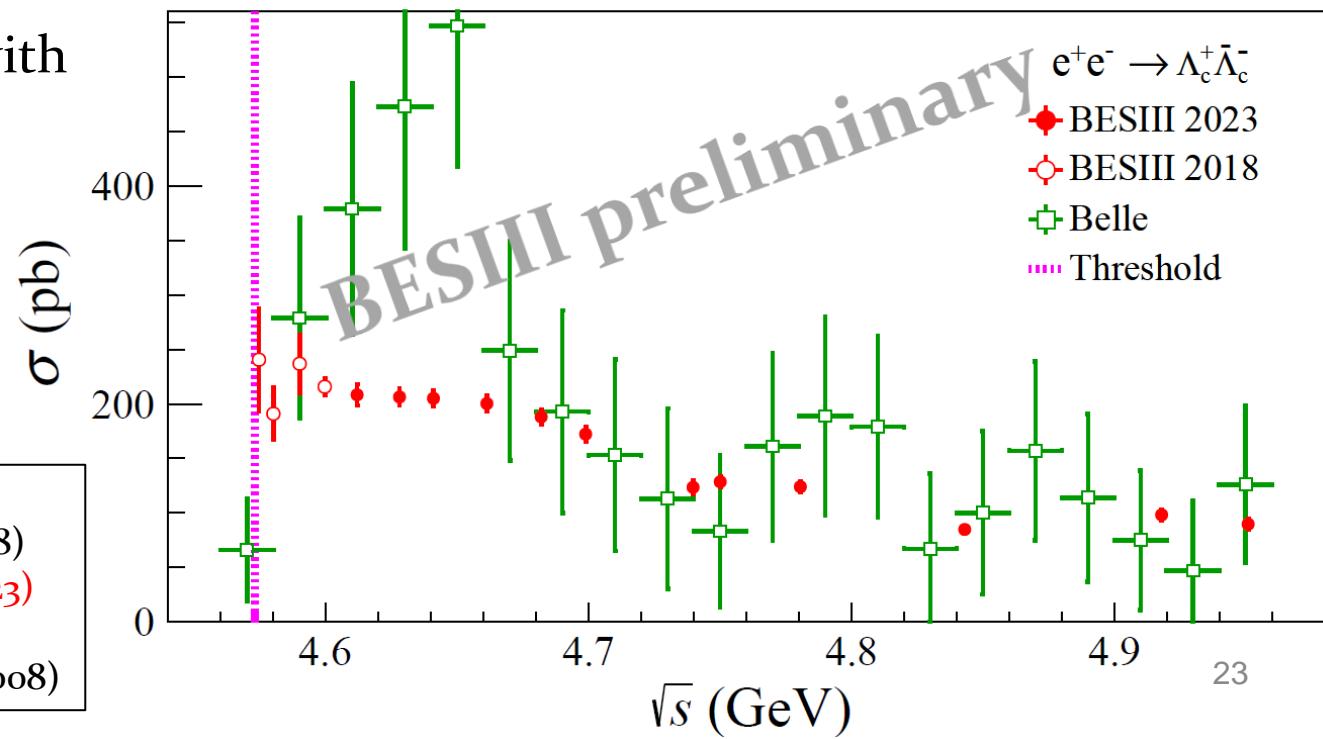
$\Xi^-$  BESIII: Phys. Rev. D 103, 012005 (2021)  
 $\Xi^0$  BESIII: Phys. Lett. B 820, 136557 (2021).



# New: Single-charm $\Lambda_c^+$ baryons

BESIII energy scans published in 2018\* and 2023\*\*

- Very precise cross section measurements
- First direct measurement of  $\Lambda_c^+$  form factors
- Sharp rise in cross section near threshold
- Disagreement with Belle data\*\*\* near 4.6 GeV
- No discernible  $G_{\text{eff}}$  oscillations



BESIII:

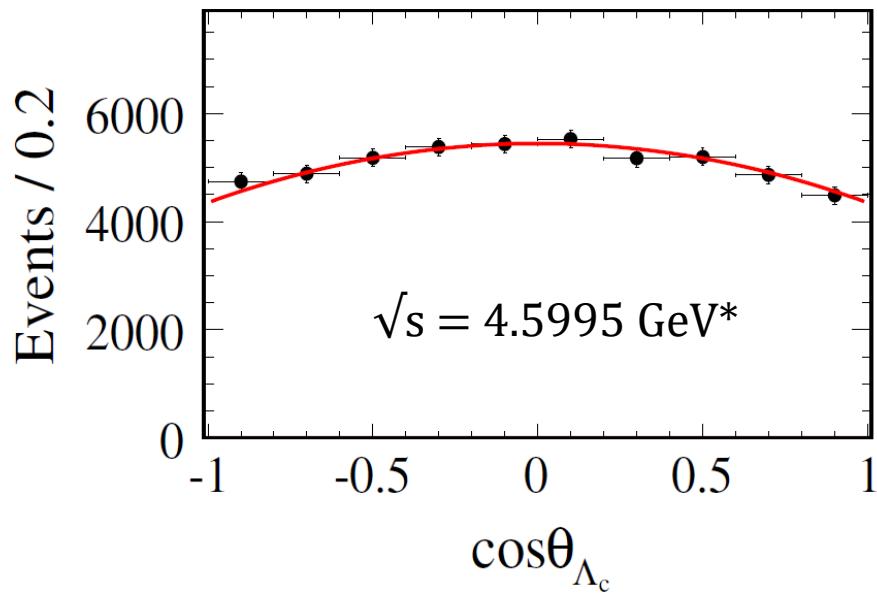
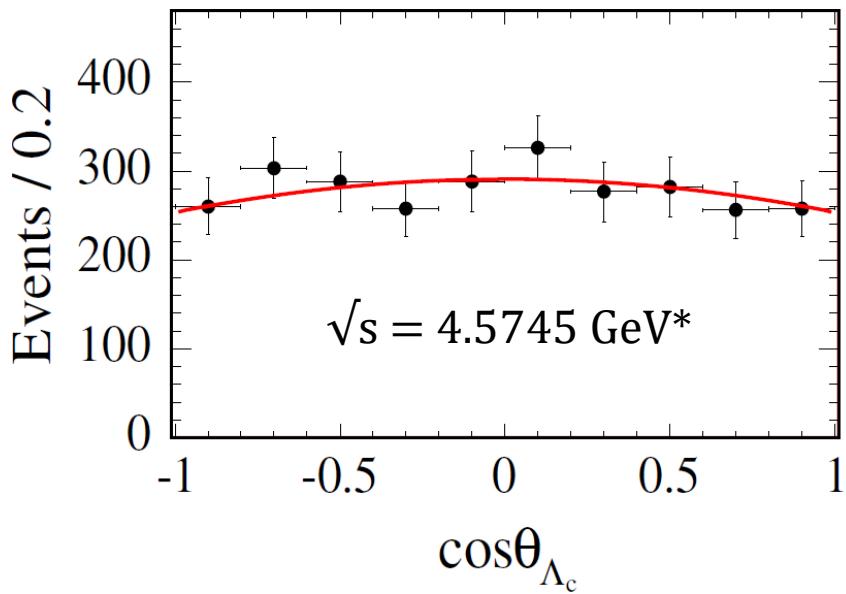
\*Phys. Rev. Lett. 120, 132001 (2018)

\*\*arXiv[hep-ex]: 2307.07316 (2023)

Belle:

\*\*\*Phys. Rev. Lett. 101, 172001 (2008)

# Single-charm $\Lambda_c^+$ baryons



Angular distributions enable extraction of ratio  $R = |G_E/G_M|$  of  $\Lambda_c^+$  near threshold\* and away from threshold\*\*.



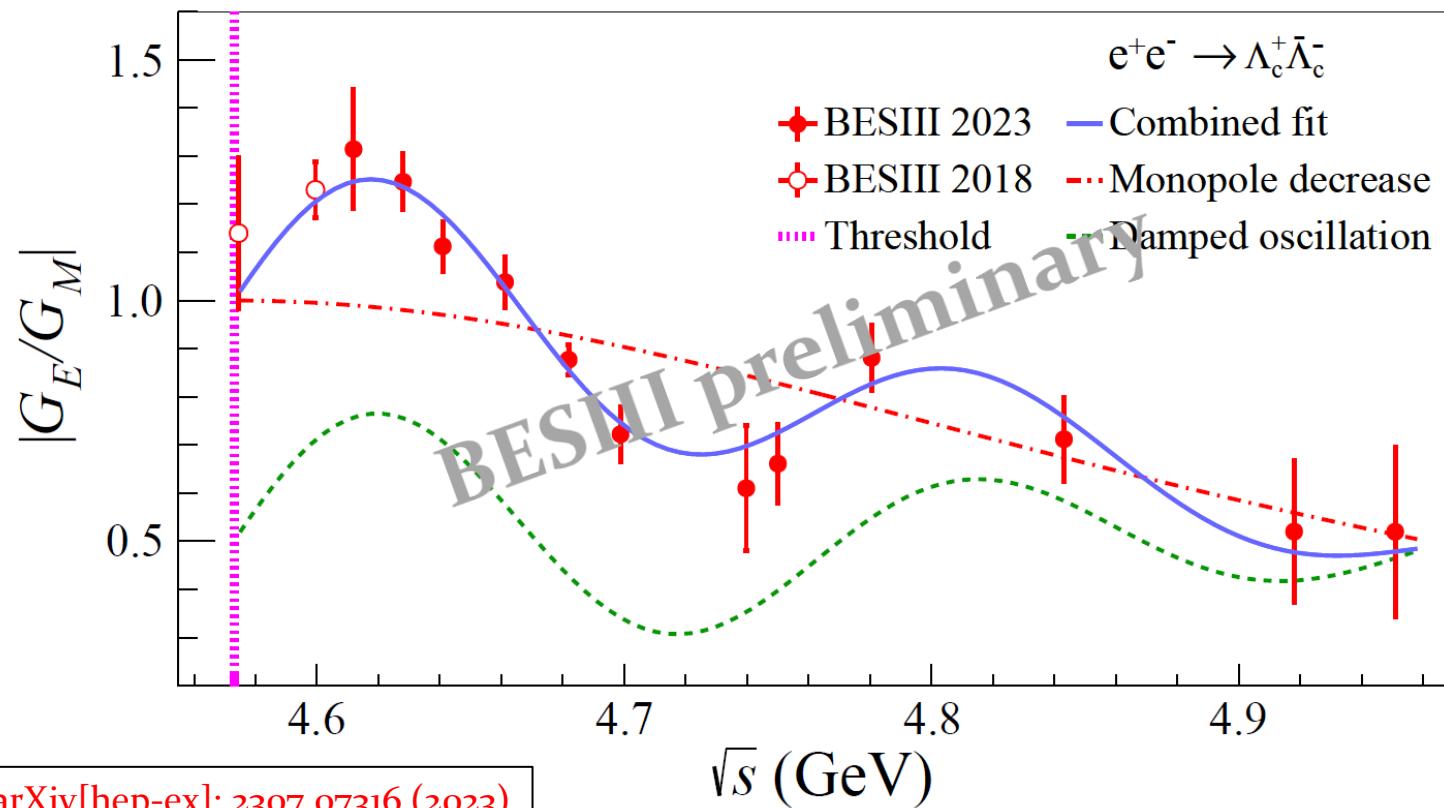
BESIII:

\*Phys. Rev. Lett. 120, 132001 (2018)  
 \*\*arXiv[hep-ex]: 2307.07316 (2023)

# New: Single-charm $\Lambda_c^+$ baryons

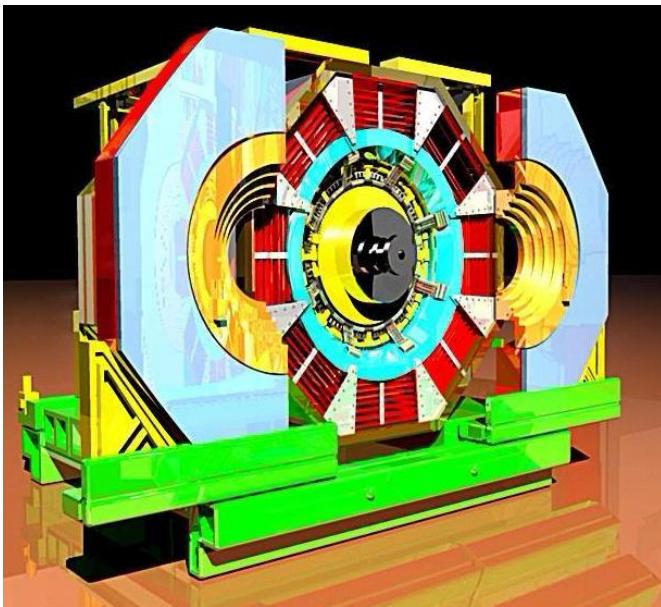
Energy dependence of  $R = |G_E/G_M|^*$ :

- Described by monopole model + damped oscillations  
 $\rightarrow$  Oscillation frequency  $\sim 3.5$  times larger than for the proton

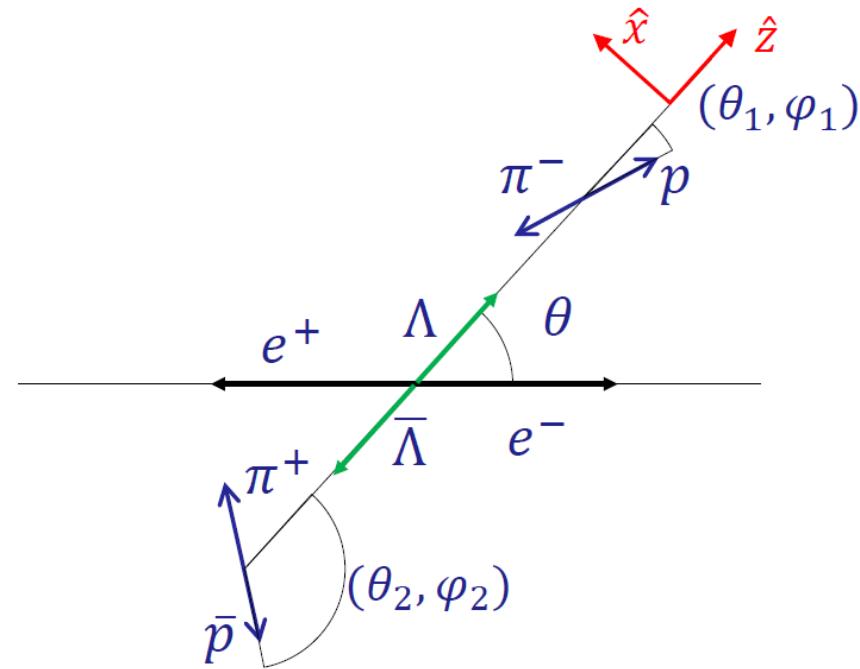


# Spin Analysis

BESIII



Consider  $e^+e^- \rightarrow \bar{Y}Y, Y \rightarrow BM + c.c$



# Spin Analysis

Production parameters of spin  $\frac{1}{2}$  baryons:

- Angular distribution parameter  $\eta = \frac{\tau - R^2}{\tau + R^2}$  where  $\tau = q^2/4M_B^2$
- Phase  $\Delta\Phi$

Decay parameters for 2-body decays:  $\alpha_1$  and  $\alpha_2$ . If CP symmetry,  $\alpha_1 = -\alpha_2 = \alpha$

**Unpolarized part**    **Polarized part**    **Spin correlated part**

$$W(\xi) = F_0(\xi) + \eta F_5(\xi) + \alpha^2 (F_1(\xi) + \sqrt{1 - \eta^2} \cos(\Delta\Phi) F_2(\xi) + \eta F_6(\xi)) \\ + \alpha \sqrt{1 - \eta^2} \sin(\Delta\Phi) (F_3(\xi) + F_4(\xi))$$

$$\mathcal{T}_0(\xi) = 1$$

$$\mathcal{T}_1(\xi) = \sin^2 \theta \sin \theta_1 \sin \theta_2 \cos \phi_1 \cos \phi_2 + \cos^2 \theta \cos \theta_1 \cos \theta_2$$

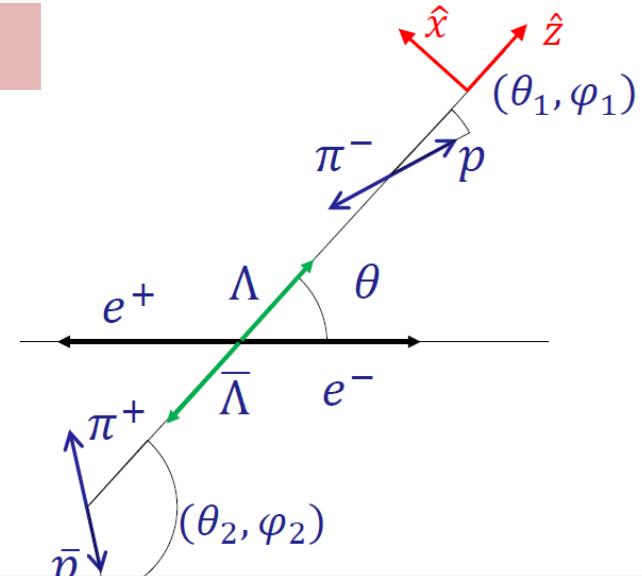
$$\mathcal{T}_2(\xi) = \sin \theta \cos \theta (\sin \theta_1 \cos \theta_2 \cos \phi_1 + \cos \theta_1 \sin \theta_2 \cos \phi_2)$$

$$\mathcal{T}_3(\xi) = \sin \theta \cos \theta \sin \theta_1 \sin \phi_1$$

$$\mathcal{T}_4(\xi) = \sin \theta \cos \theta \sin \theta_2 \sin \phi_2$$

$$\mathcal{T}_5(\xi) = \cos^2 \theta$$

$$\mathcal{T}_6(\xi) = \cos \theta_1 \cos \theta_2 - \sin^2 \theta \sin \theta_1 \sin \theta_2 \sin \phi_1 \sin \phi_2$$



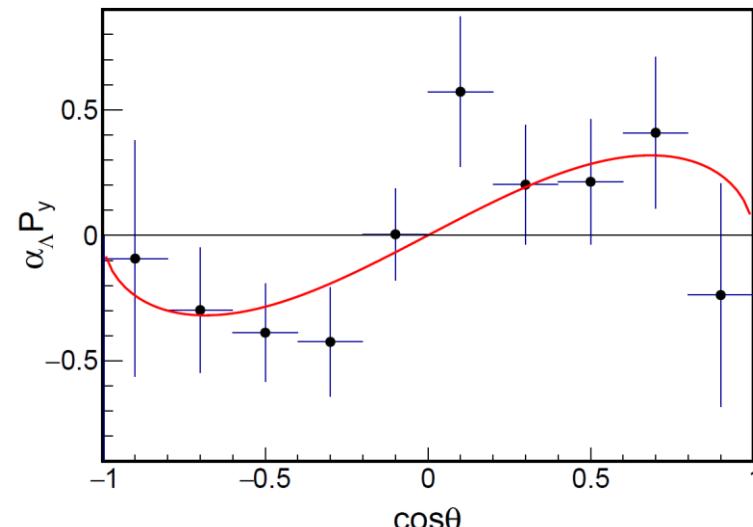
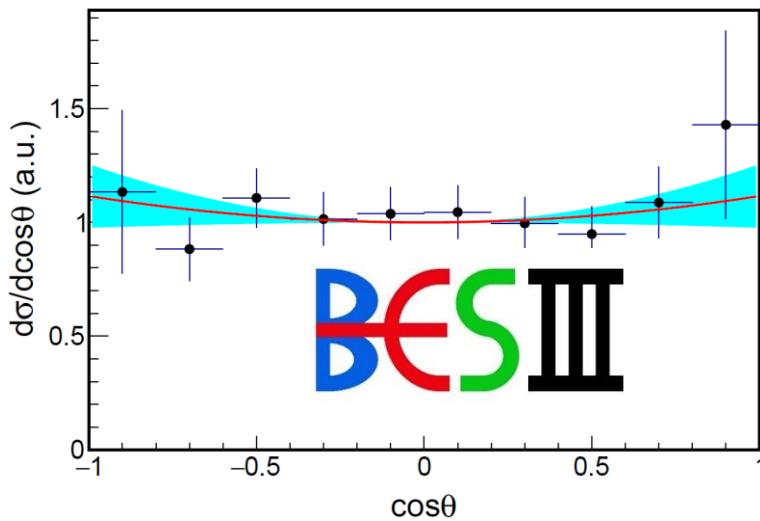
# First complete measurement of $\Lambda$ EMFF

- BESIII data at 2.396 GeV with 555 exclusive  $\bar{\Lambda}\Lambda$  events in sample.

- $R = |G_E/G_M| = 0.96 \pm 0.14 \pm 0.02$
- $\Delta\Phi = 37^\circ \pm 12^\circ \pm 6^\circ$
- $\sigma = 118.7 \pm 5.3 \pm 5.1 \text{ pb}$

BESIII:  
 Phys. Rev. Lett. 123, 122003 (2019)

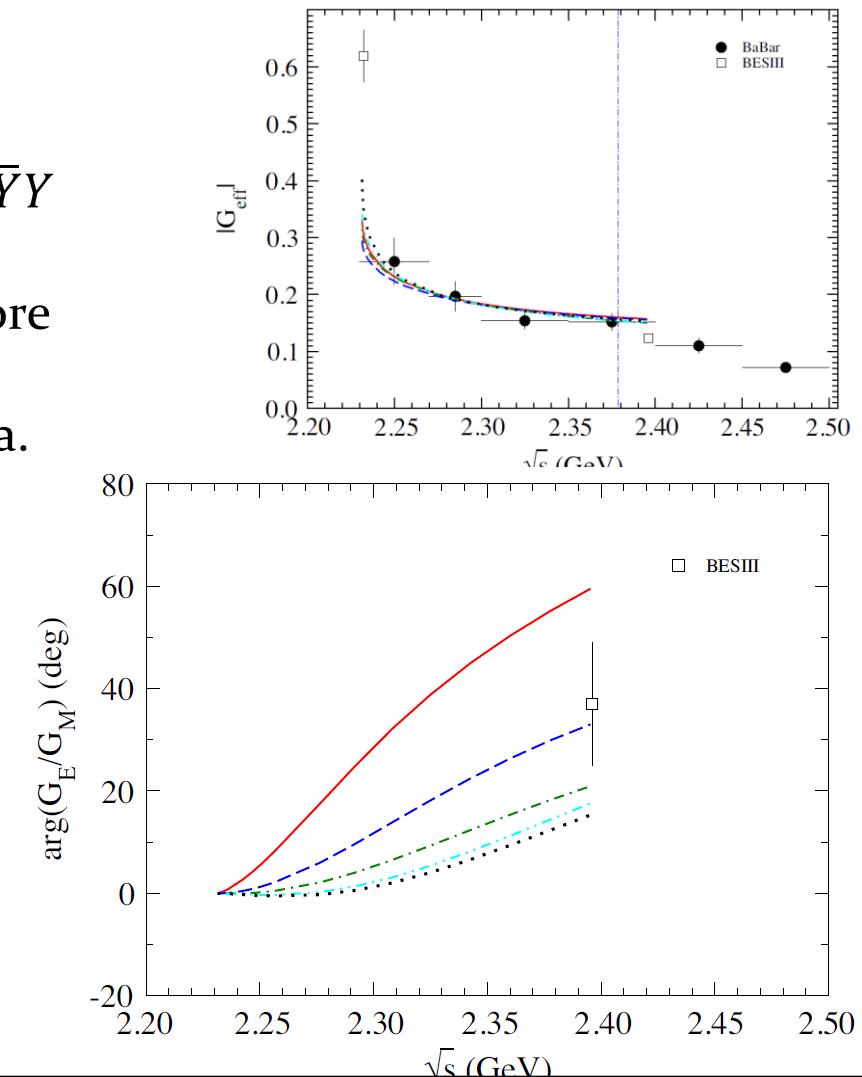
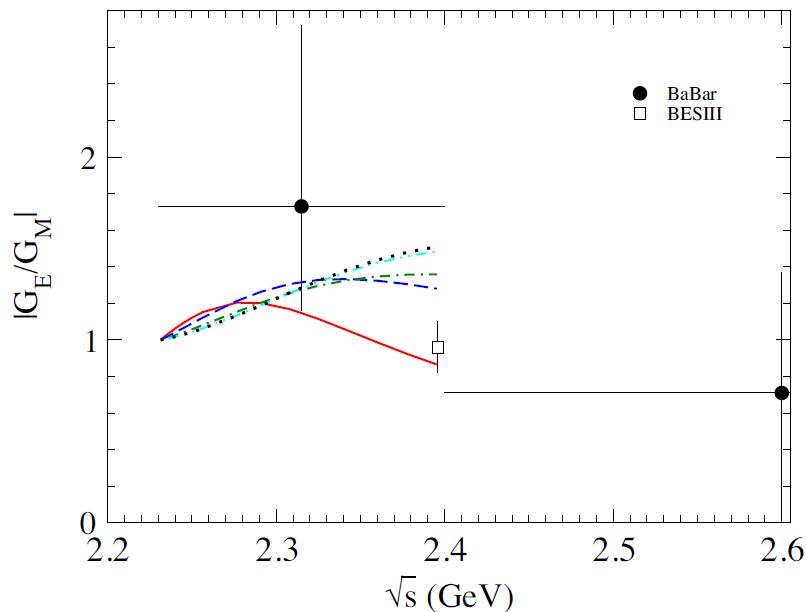
- Most **precise** result on  $R$  and  $\sigma$
- First conclusive result on  $\Delta\Phi$



# Theory Interpretation

Theoretical study of the  $e^+e^- \rightarrow Y\bar{Y}$  by Haidenbauer, Meissner and Dai\*

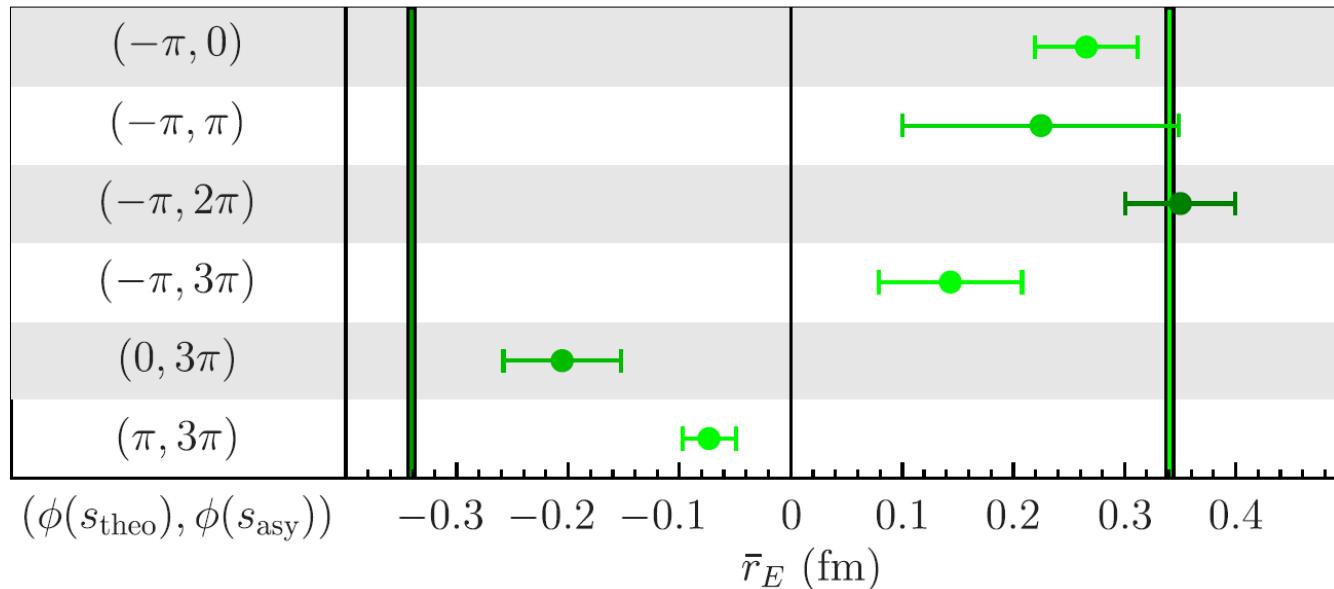
- $Y\bar{Y}$  potentials constructed from  $\bar{p}p \rightarrow Y\bar{Y}$  data from PS185.
- Spin-dependent observables much more sensitive to the  $Y\bar{Y}$  potential.
- Fairly good agreement with BESIII data.



# Theory interpretation

Dispersive calculations by Mangoni, Pacetti & Tomasi-Gustafsson\*:

- Study of the phase  $\Delta\Phi$  – must be integer multiple of  $\pi$  at threshold ( $N_{th}$ ) and at the asymptotic scale  $q_{asy}$  ( $N_{asy}$ ).
- Fit of different data from \*\* and \*\*\* to different scenarios of  $N_{th}$  and  $N_{asy}$   
 $\rightarrow$  calculations of charge radius!



\*Mangoni *et al.*, Phys. Rev. D 104, 116016 (2021)

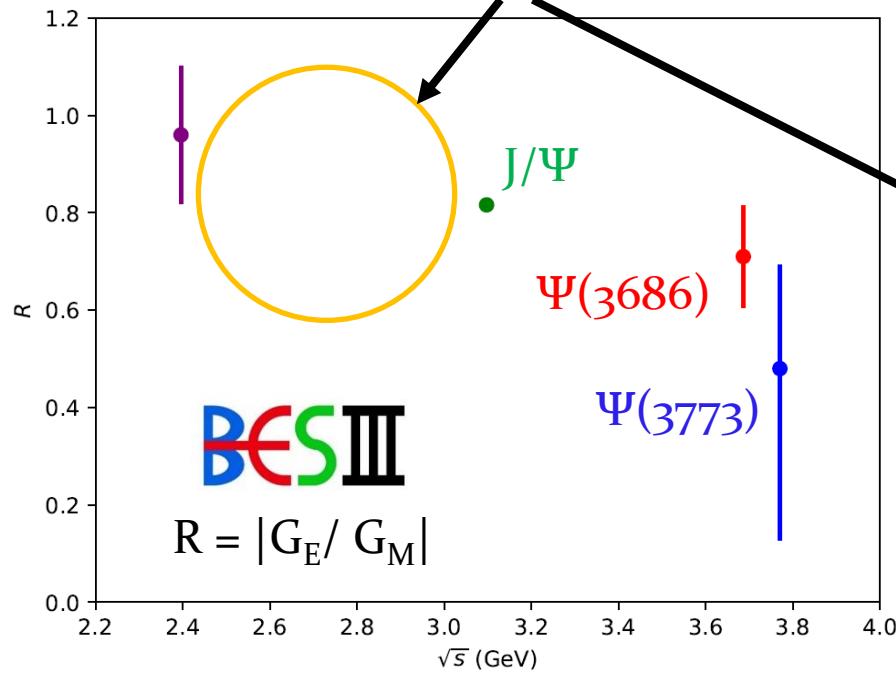
\*\*BESIII: Phys. Rev. Lett. 123, 122003 (2019)

\*\*\*BaBar: Phys. Rev. D 76, 092006 (2007)

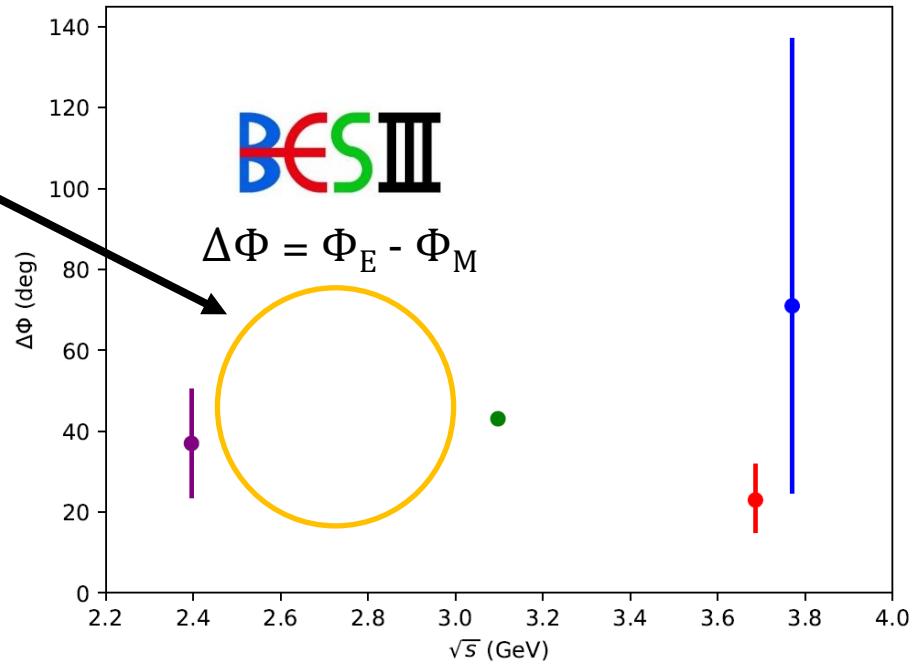
# $\Lambda$ Spin Analyses

Similar analyses performed at  
 $J/\Psi^{**}$ ,  $\Psi(3686)^{***}$  and  $\Psi(3773)^{****}$

- $R$  and  $\Delta\Phi$  interpreted as *psionic* structure functions
- New off-resonance data underway



- \*Phys. Rev. Lett. 123, 122003 (2019)  
 \*\*Nature Phys. 15, p. 631-634 (2019)  
 \*\*\*arXiv[hep-ex]: 2303.00271 (2023)  
 \*\*\*\*Phys. Rev. D 105, L011101 (2020)



# New: $\Sigma^+$ Spin Analysis

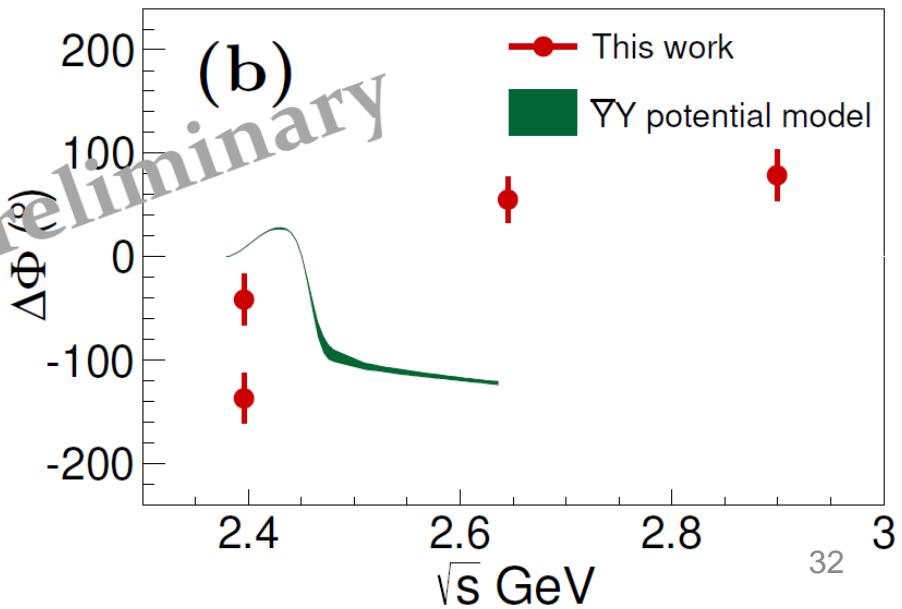
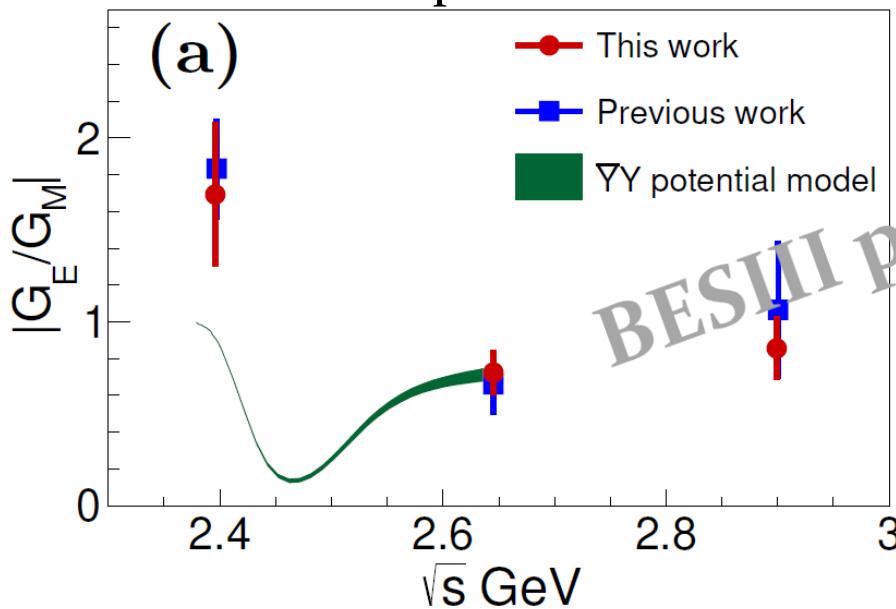
- Energy dependence of  $R$  and  $\Delta\Phi$  in three different points\*
  - Double-tag  $e^+e^- \rightarrow \Sigma^+\bar{\Sigma}^- \rightarrow p\pi^0\bar{p}\pi^0$  at 2.64 GeV and 2.9 GeV
  - Single-tag  $e^+e^- \rightarrow \Sigma^+\bar{\Sigma}^- \rightarrow p\pi^0X + c.c.$  at 2.396 GeV  
 $\rightarrow \Delta\Phi / 180^\circ - \Delta\Phi$  ambiguity
- Better precision than in previous work\*\*.
- Worse agreement with  $Y\bar{Y}$  potential model \*\*\* compared to  $\Lambda$ .

\*BESIII, arXiv[hep-ex]:2307.15894 (2023)

\*\* BESIII, Phys. Lett. B 814, 136110 (2021)

\*\*\* Haidenbauer *et al.*,

Phys. Rev. D 103, 014028 (2021)



# Summary

- Time-like form factors a viable tool to study structure and femtometer sizes.
- Many new results from the BESIII experiment
  - single- and double strange hyperons
  - charm baryons
- Hyperon polarisation provide information about space-like structure *e.g.* charge radius.
- More data collected → STAY TUNED !!!





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# Thanks for your attention!

*Knut and Alice  
Wallenberg  
Foundation*



Swedish  
Research  
Council



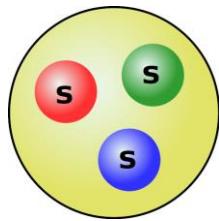
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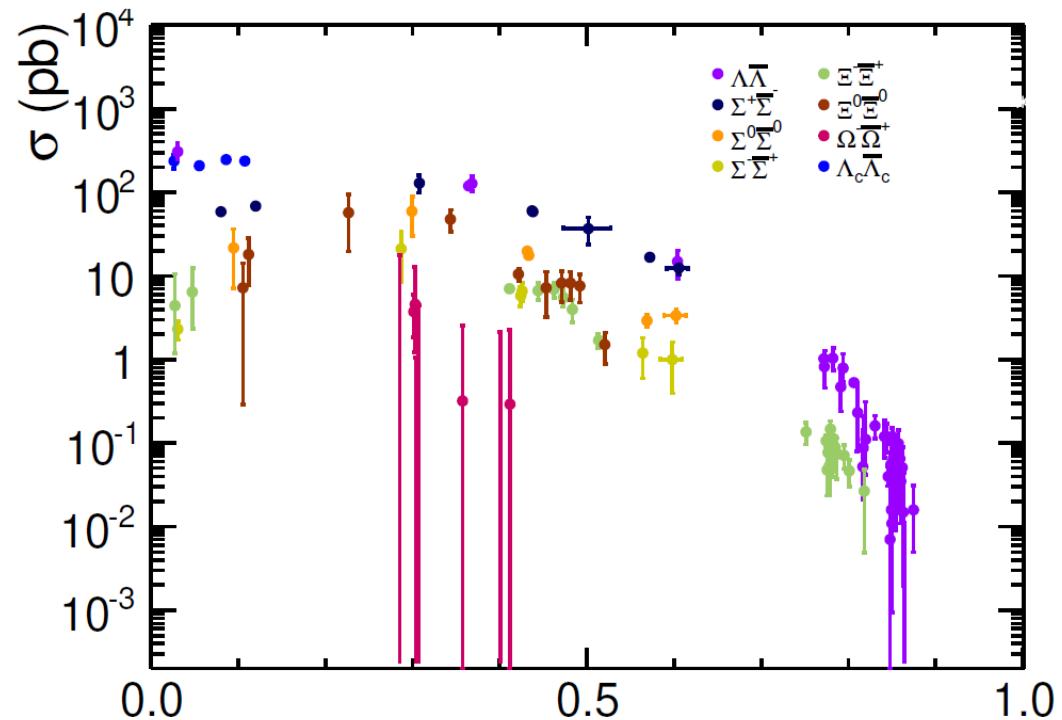
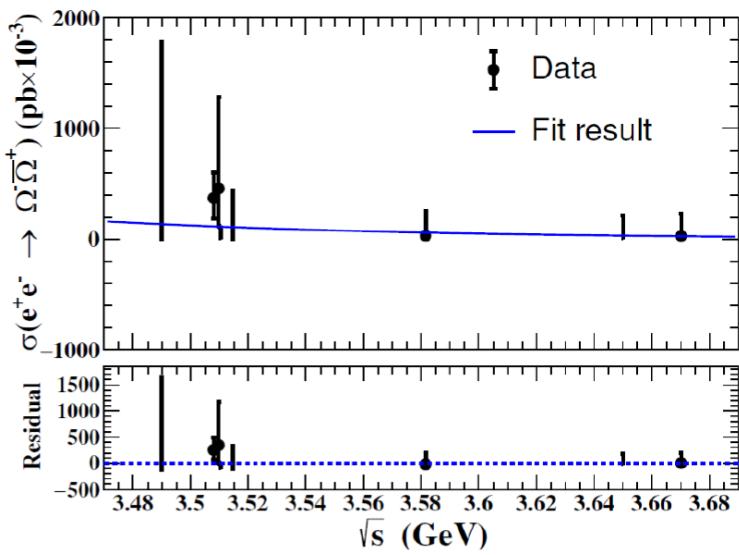
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# Backup



# Triple-strange $\Omega$ hyperons

- New BESIII study: Search for  $e^+e^- \rightarrow \Omega^-\bar{\Omega}^{+*}$ 
  - No signals seen → only upper limits determined.
  - Will need much larger luminosities to match other hyperon studies\*\*



\* BESIII: Phys. Rev. D 107, 052003, 2023

\*\* Schönning et al., Chin. Phys. C 47, 5, 052002 (2023)

$$\beta = \sqrt{1 - 4M_B^2/s}$$

# Single-strange hyperons

$\Sigma^+$  Form Factor Ratio:

$$R = \frac{|G_E(q^2)|}{|G_M(q^2)|} \text{ measured at } 2.396 \text{ GeV to be } 1.83 \pm 0.26$$

BESIII

