

Experiment of Few-Nucleon Scattering to Explore Three-Nucleon Forces

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August 3rd, 2023

Three-Nucleon Force (3NF)

- nuclear forces acting in systems more than $A = 2$ nucleons -

Key to fully understand properties of nucleus

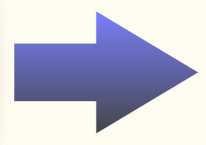
Existence of 3NF was predicted in 1930's (after Yukawa's meson theory).

1957 **Fujita-Miyazawa 3NF**

'80's **First indication** of 3NF : Binding Energies of Triton

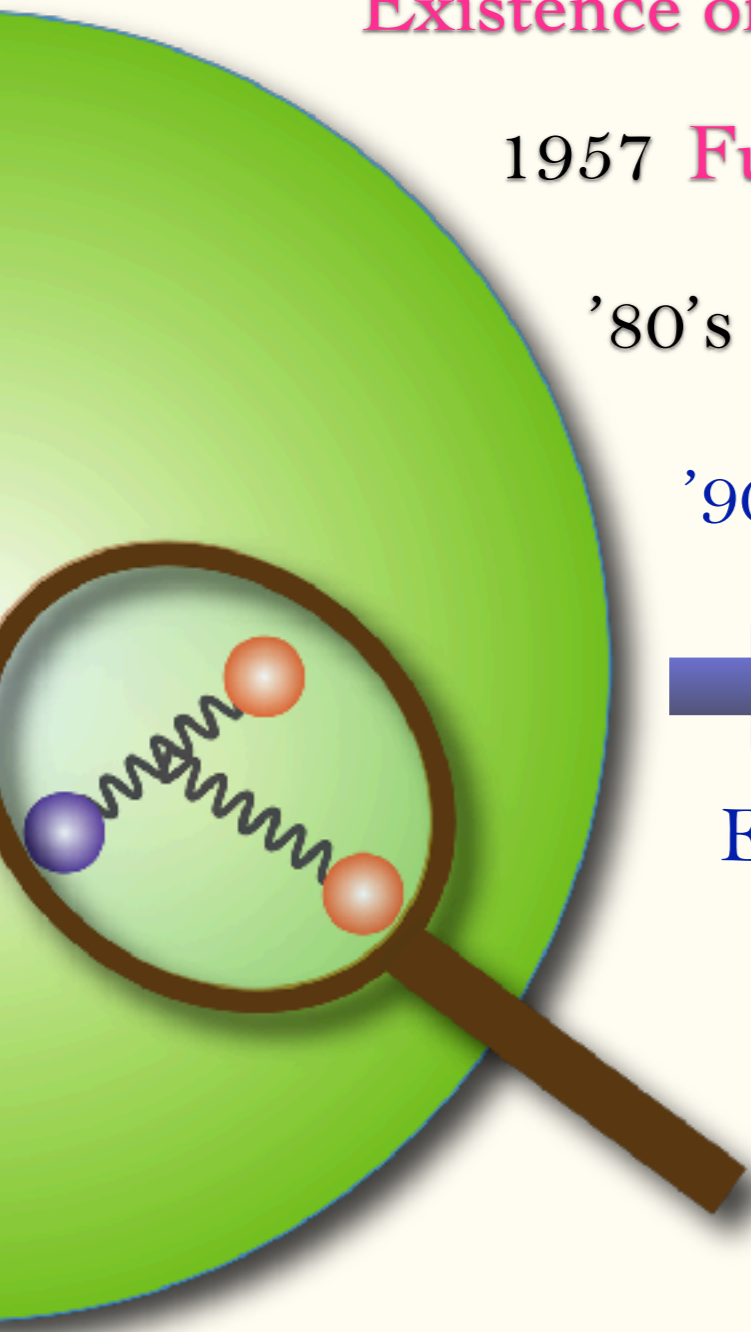
'90's Realistic Nucleon-Nucleon Potential

(CD Bonn, AV18, Nijmegen I, II)



Evidence / Candidates of 3NF Effects

- Nucleon-Deuteron Scattering at Intermediate Energies
- Binding Energies / Levels of Light Mass Nuclei
- Equation of State of Nuclear Matter
- etc ...

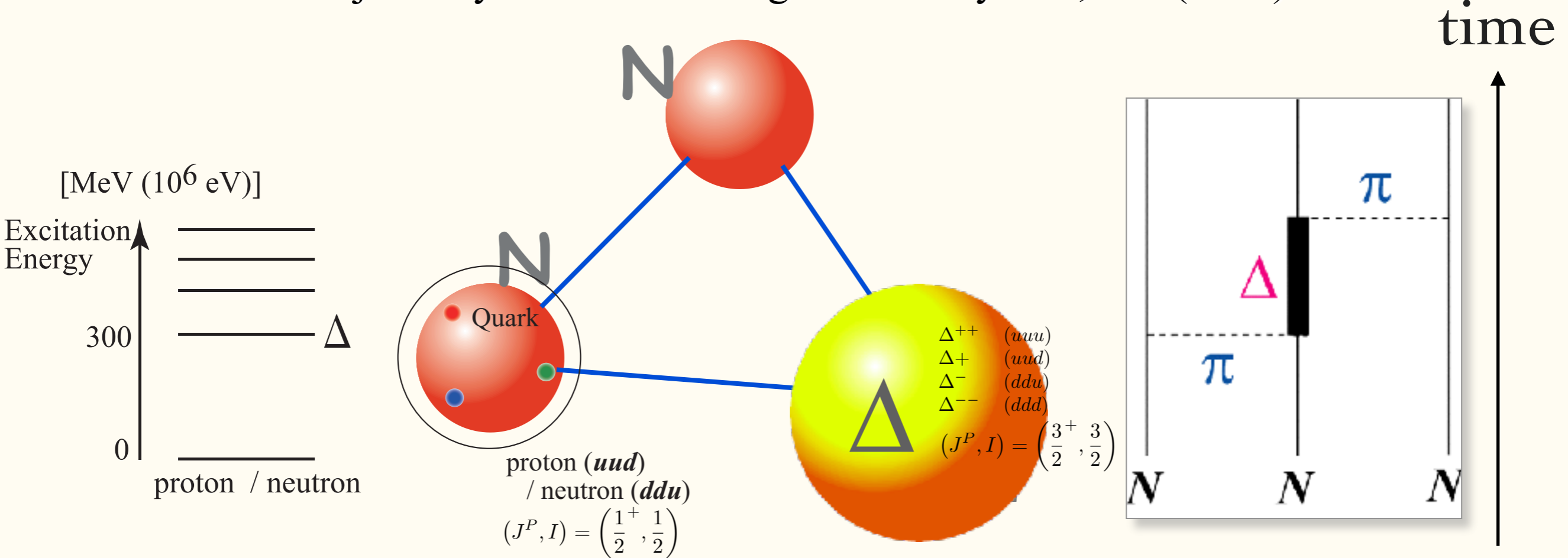


Three-Nucleon Force

• 2π -exchange 3NF :

- Main Ingredients : Δ -isobar excitations in the intermediate

1957 Fujita-Miyazawa 3NF Prog. Theor. Phys. 17, 360 (1957)

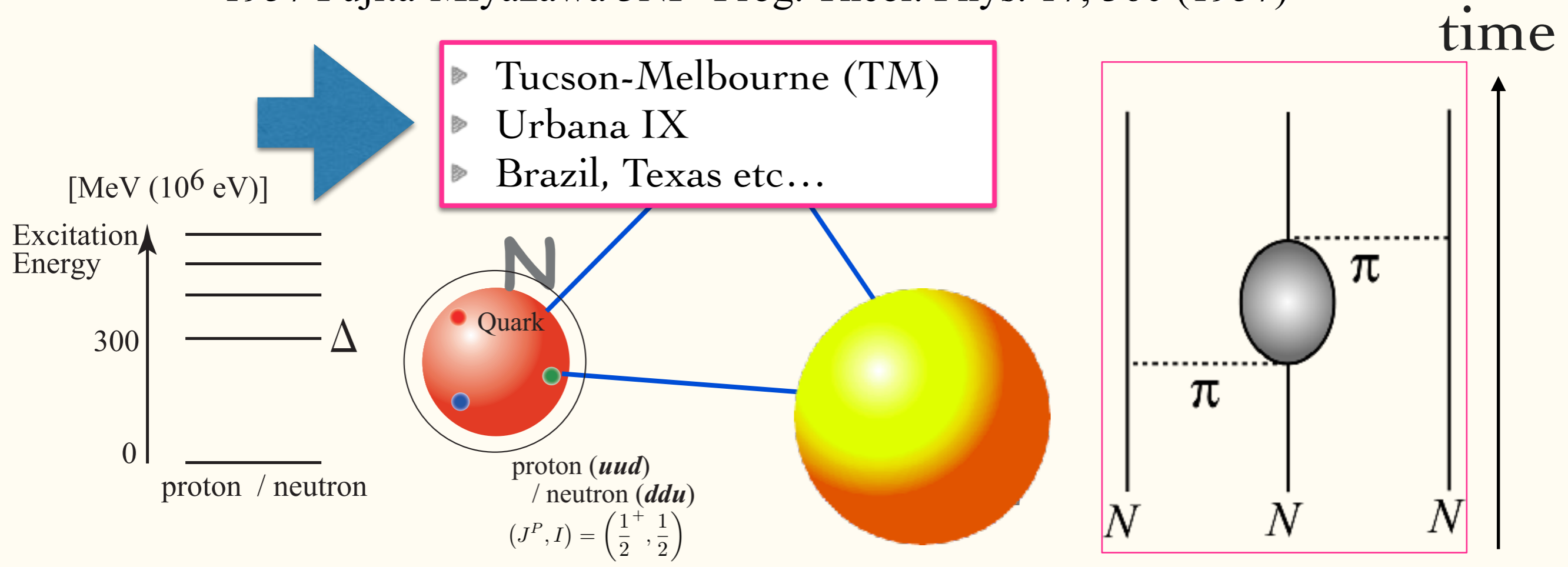


3NF naturally arises due to the inner structure of Nucleon.

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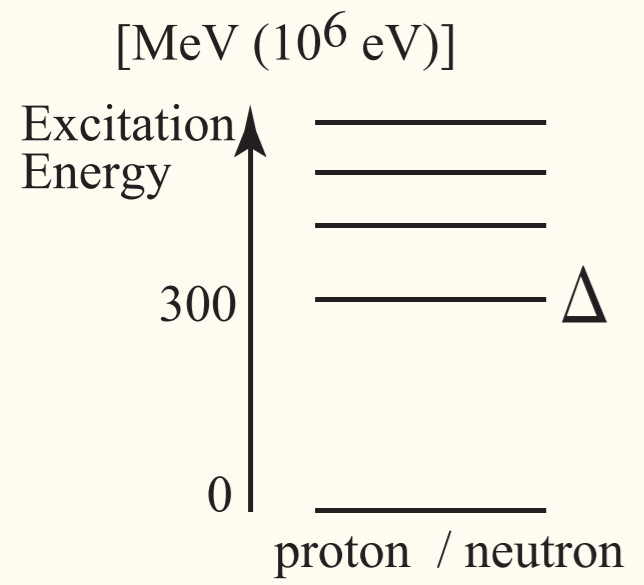


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Chiral EFT Nuclear Forces

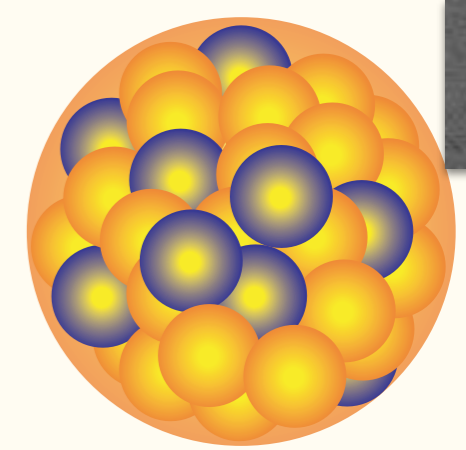
	2N Force	3N Force	4N Force
LO $(Q/\Lambda_\chi)^0$		—	—
NLO $(Q/\Lambda_\chi)^2$			
N2LO $(Q/\Lambda_\chi)^3$			—
N3LO $(Q/\Lambda_\chi)^4$			
N4LO $(Q/\Lambda_\chi)^5$			

3NFs appear at N2LO

3NF naturally arises

Where ?

3NFs in $A > 3$ - ① -



3NFs in Finite Nuclei

Ab Initio Calculations for Light Nuclei ($A \lesssim 12$): ${}^4\text{He}$ to ${}^{12}\text{C}$

- Green's Function Monte Carlo
- No-Core Shell Model etc..
- 2NF provide less binding energies
- 3NF : well reproduce the data

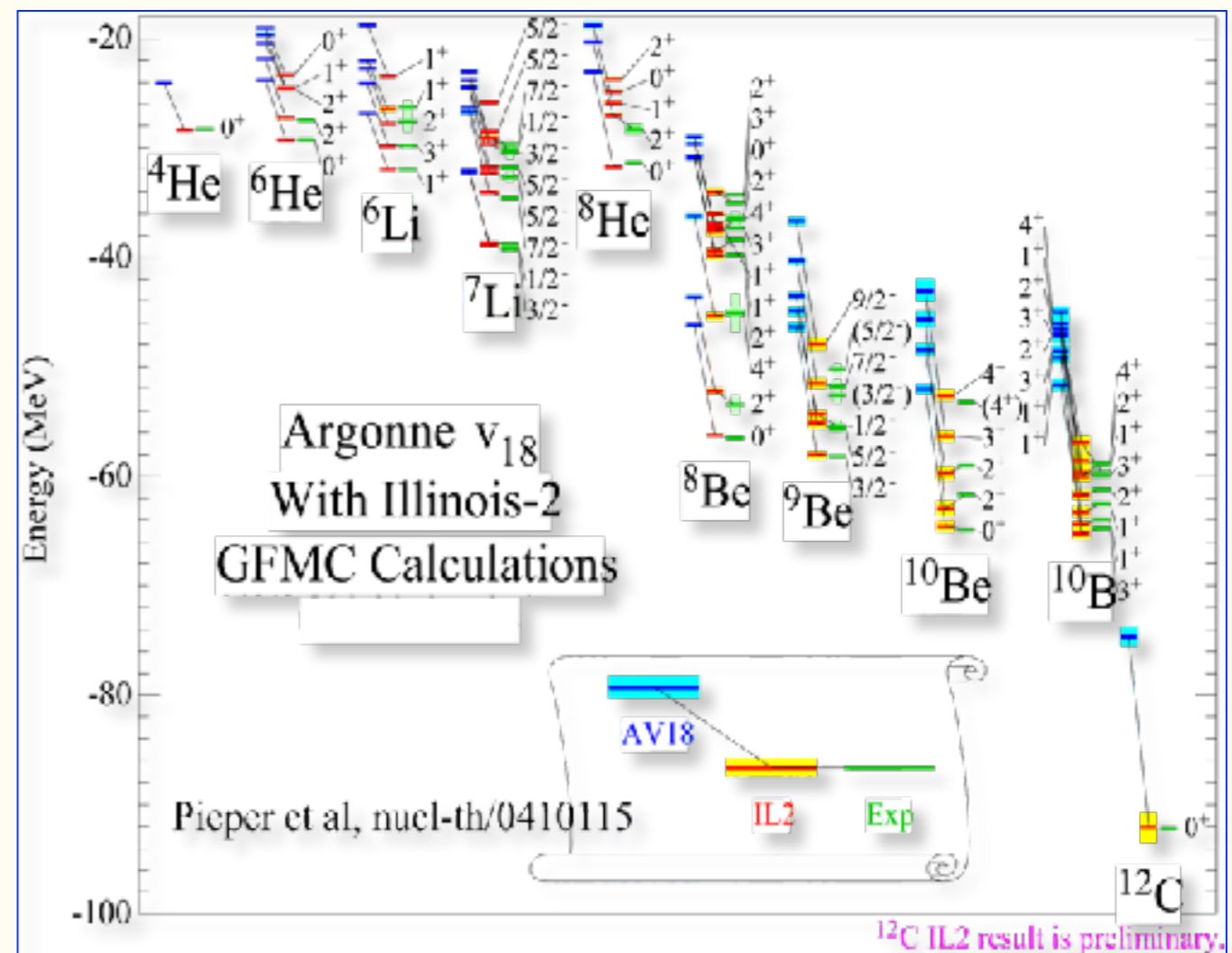
IL2 3NF (Illinois-II 3NF) :
 2π -exchange 3NF
+ 3π -ring with Δ -isobar

3NF effects in B.E.

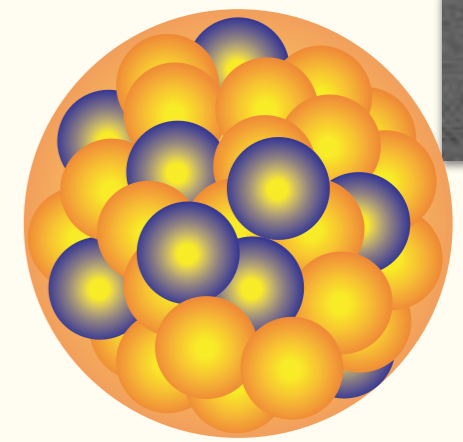
- 10-25%
- Attractive

Note :

T=3/2 3NFs (three-neutron force) play important roles to explain B.E. in neutron rich nuclei.



3NFs in $A > 3$ - ① -



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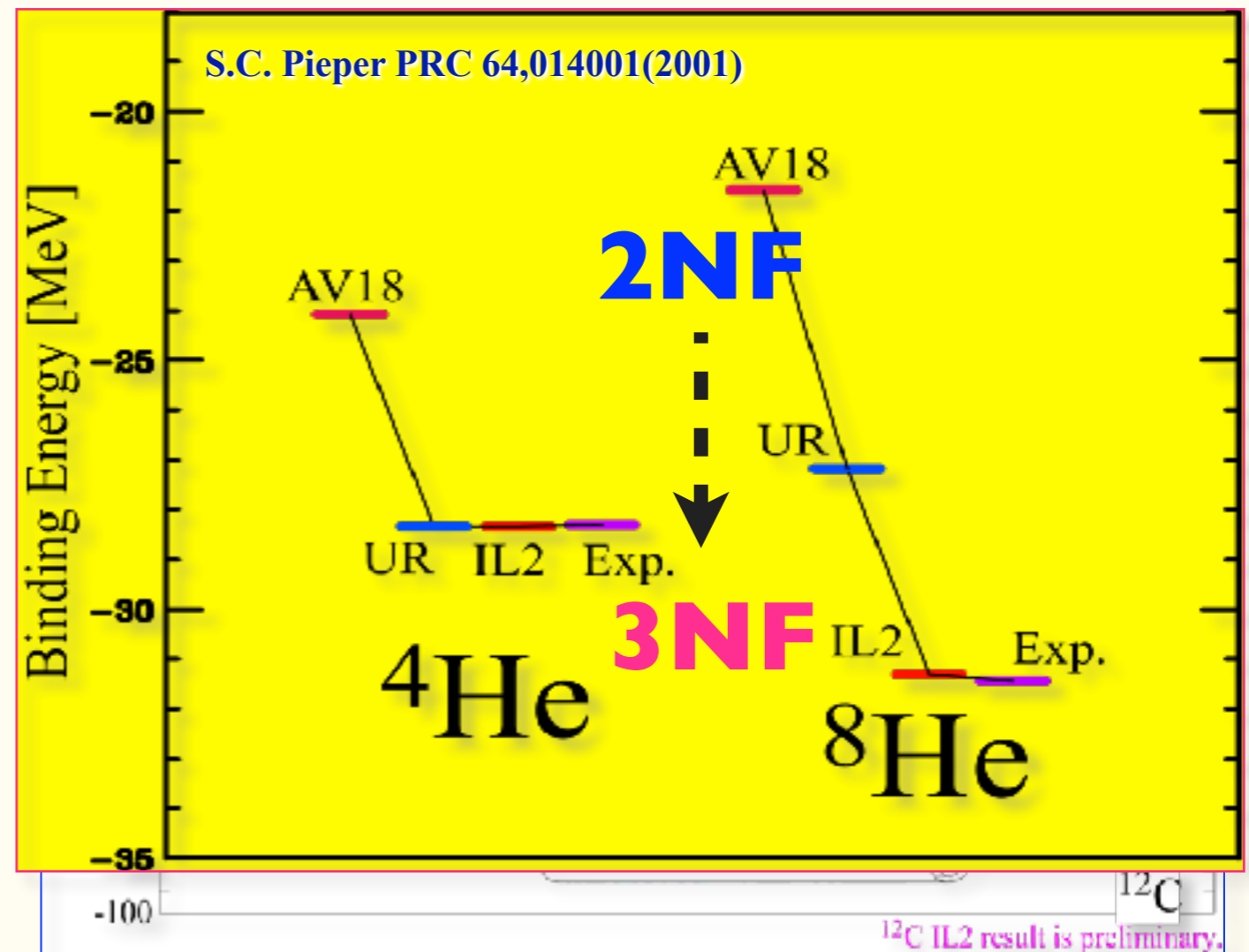
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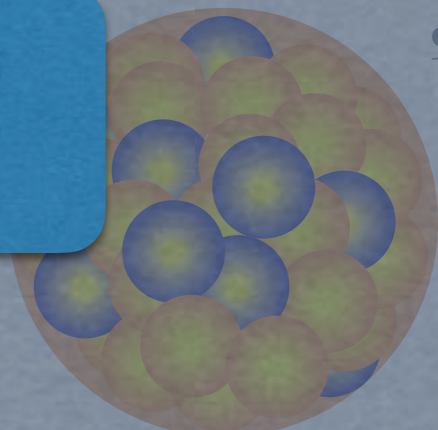
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3NFs in Finite Nuclei

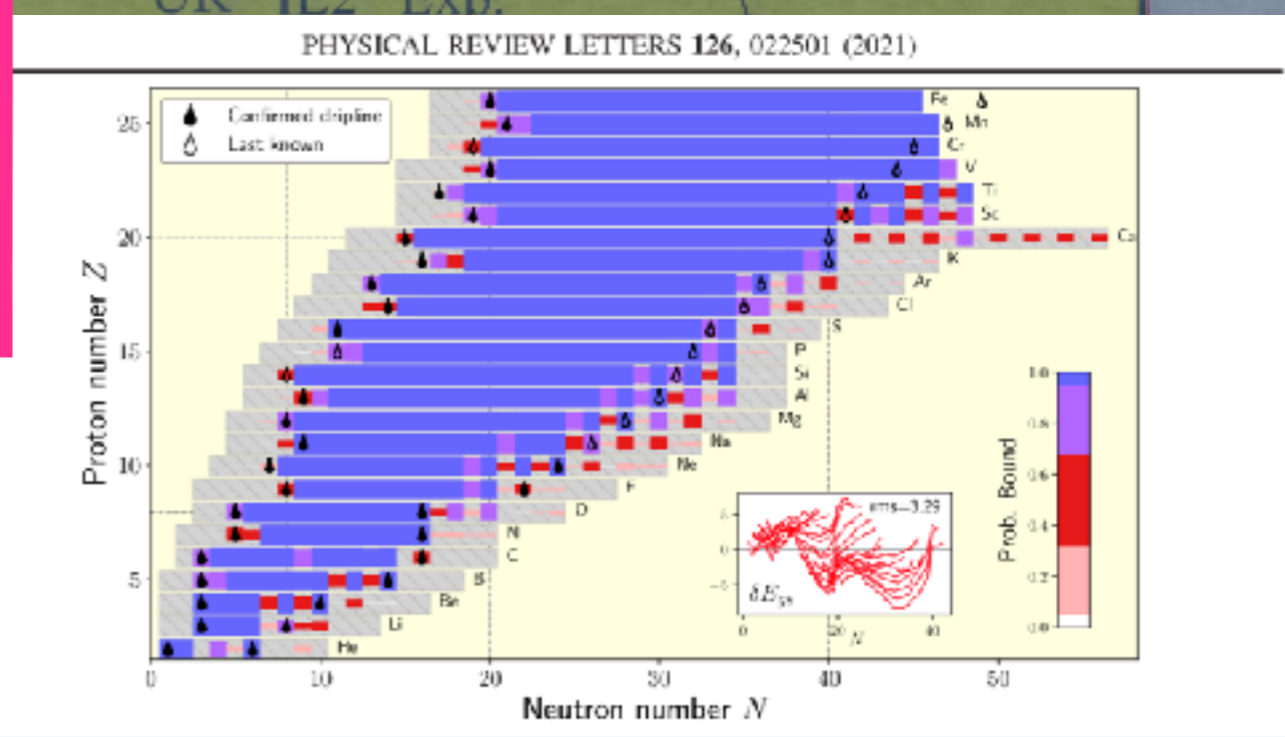
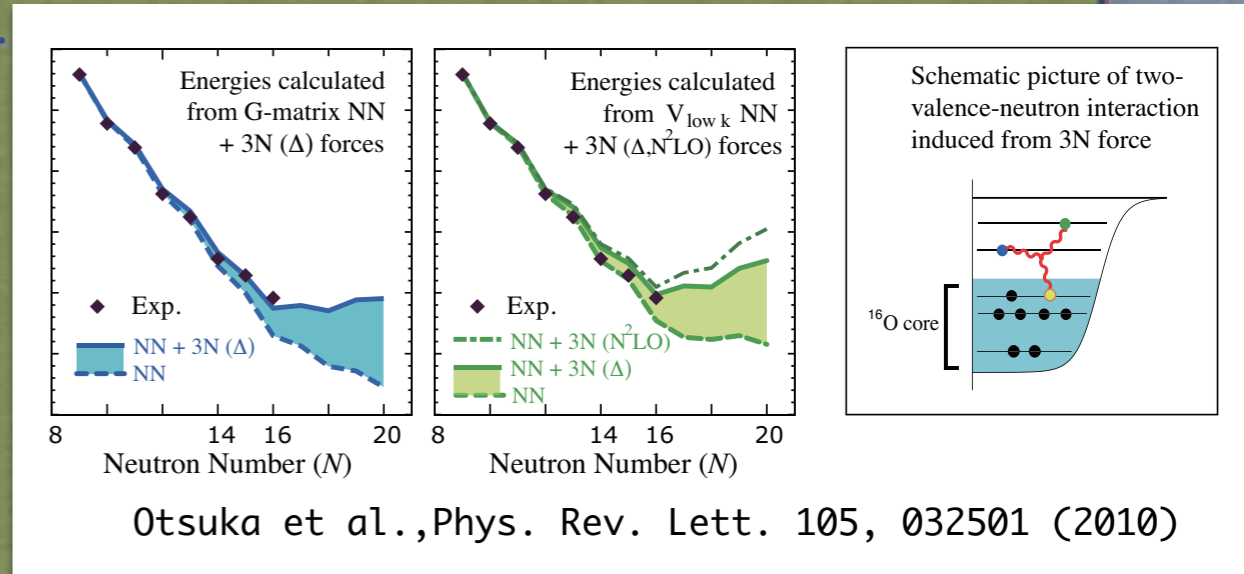
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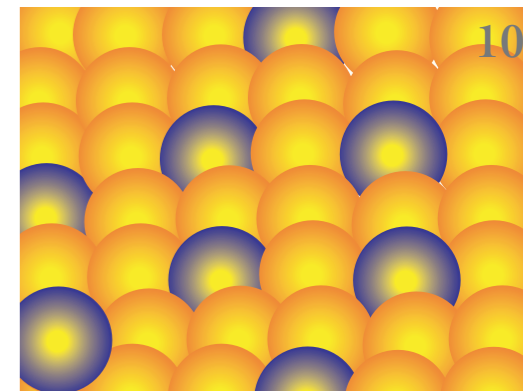


Medium Mass Nuclei
 3NFs provide key mechanisms,
 e.g. shell-evolution,
 boundaries of nuclear stability.

Note :
 $T=3/2$ 3NFs (three-neutron force) play important roles to explain B.E. in neutron rich nuclei.

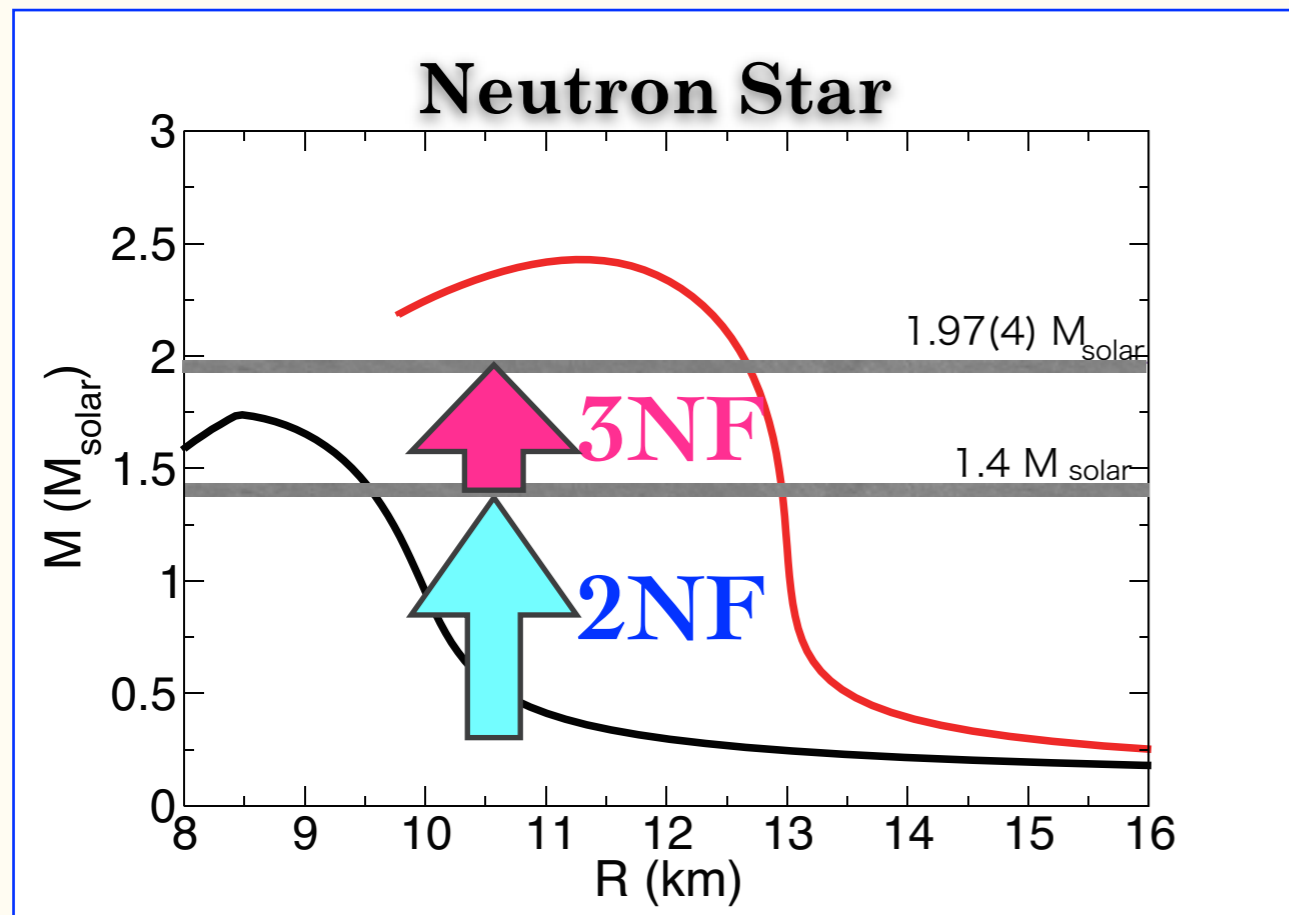


3NFs in $A > 3$ - ② -



10

3NFs in Infinite Nuclei - Neutron Star -



A. Akmal et al., PRC 58, 1804('98)

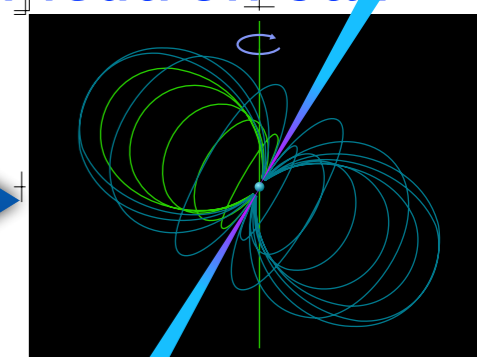
- 3NF in Nuclei is required...
 - Short & Repulsive
- Large effects at high density.

“Endpoint of stellar evolution”

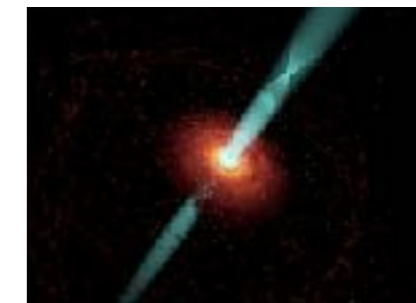
Supernovae
Explosion



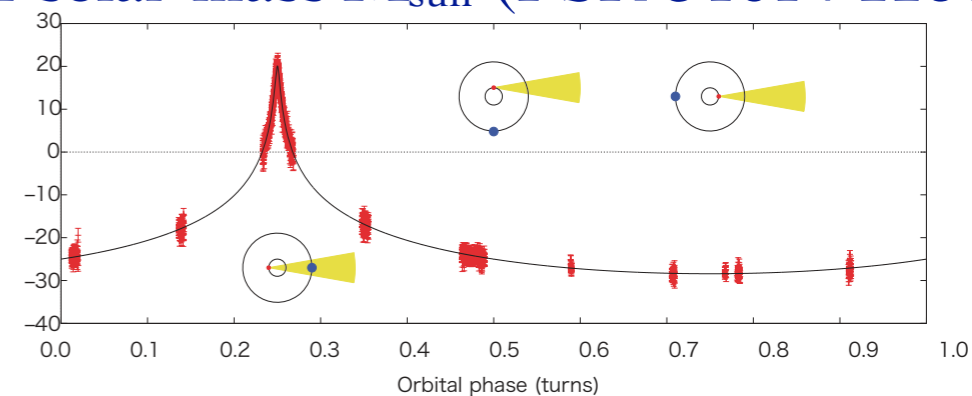
Neutron Star



Black Hole



Discovery of Heaviest Neutron Star
with 2 solar-mass M_{sun} (PSR J1614-2230)



Nature 467 1081 (2010)

How ?

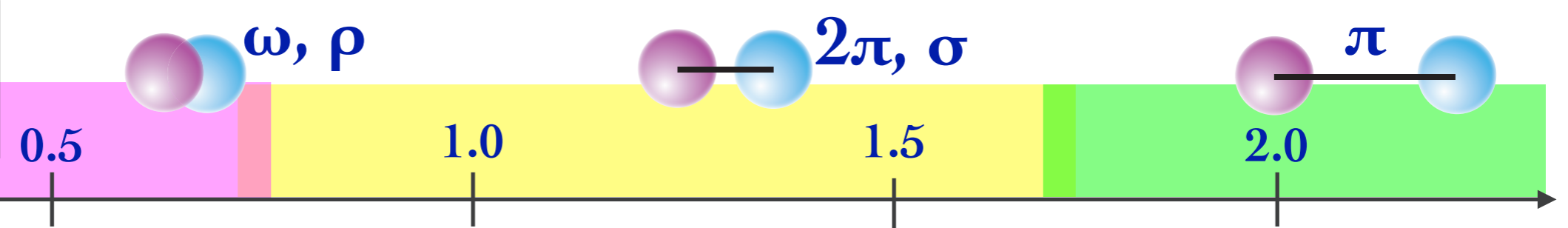
Two & Three-Nucleon Force

①. Repulsive
-Short Range-

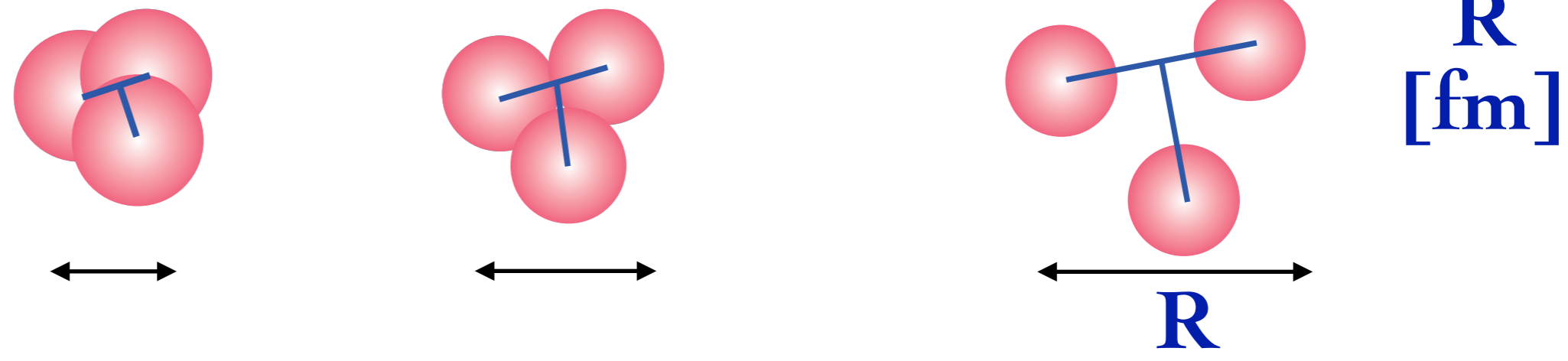
②. Attractive (strong)
-Intermediate Range-

③. Attractive (weak)
- Long Range -

Two-Nucleon Force



Three-Nucleon Force



3NFs are momentum, spin, and iso-spin dependent.

Nuclear Matter
Neutron Star

Nuclear Structure

Few-Nucleon Scattering

a good probe to study the dynamical aspects of 3NFs.

- ✓ Momentum dependence
- ✓ Spin & Iso-spin dependence

Direct Comparison between Theory and Experiment

• Theory : Faddeev / Faddeev-Yakubovsky Calculations

Rigorous Numerical Calculations of 3, 4N System

2NF Input

- CDBonn
- Argonne V18 (AV18)
- Nijmegen I, II, 93

3NF Input

- Tucson-Melbourne
- Urbana IX
- etc..

2NF & 3NF Input

- Chiral Effective Field Theory

• Experiment : Precise Data

- $d\sigma/d\Omega$, Spin Observables (A_p , K_{ij} , C_{ij})

Extract fundamental information of Nuclear Forces

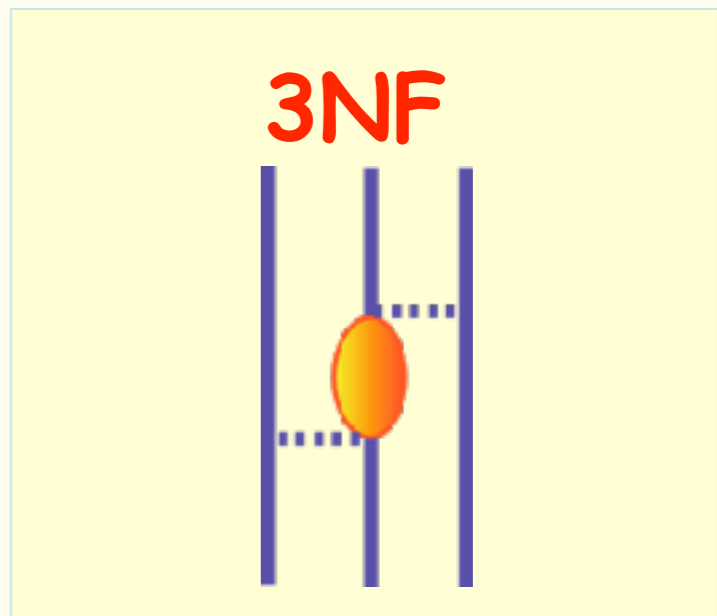
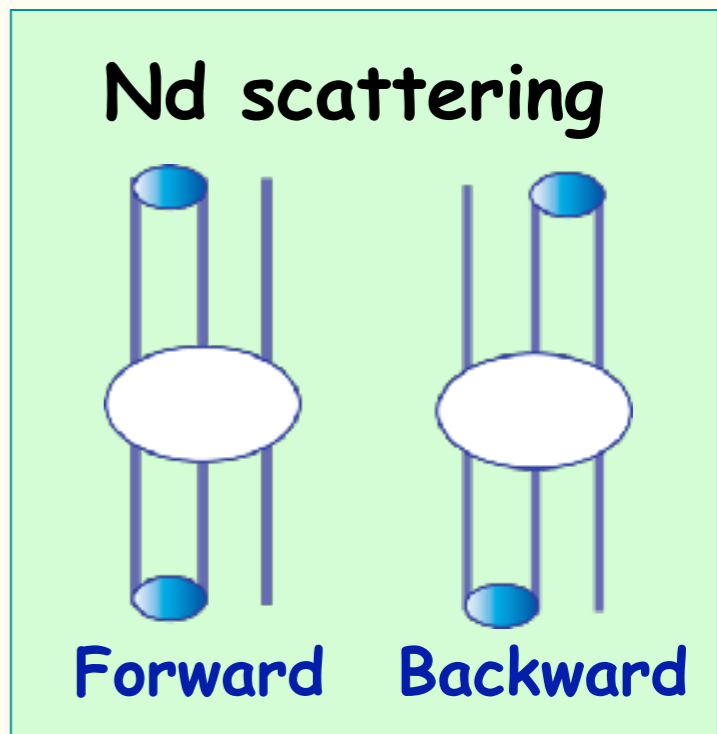
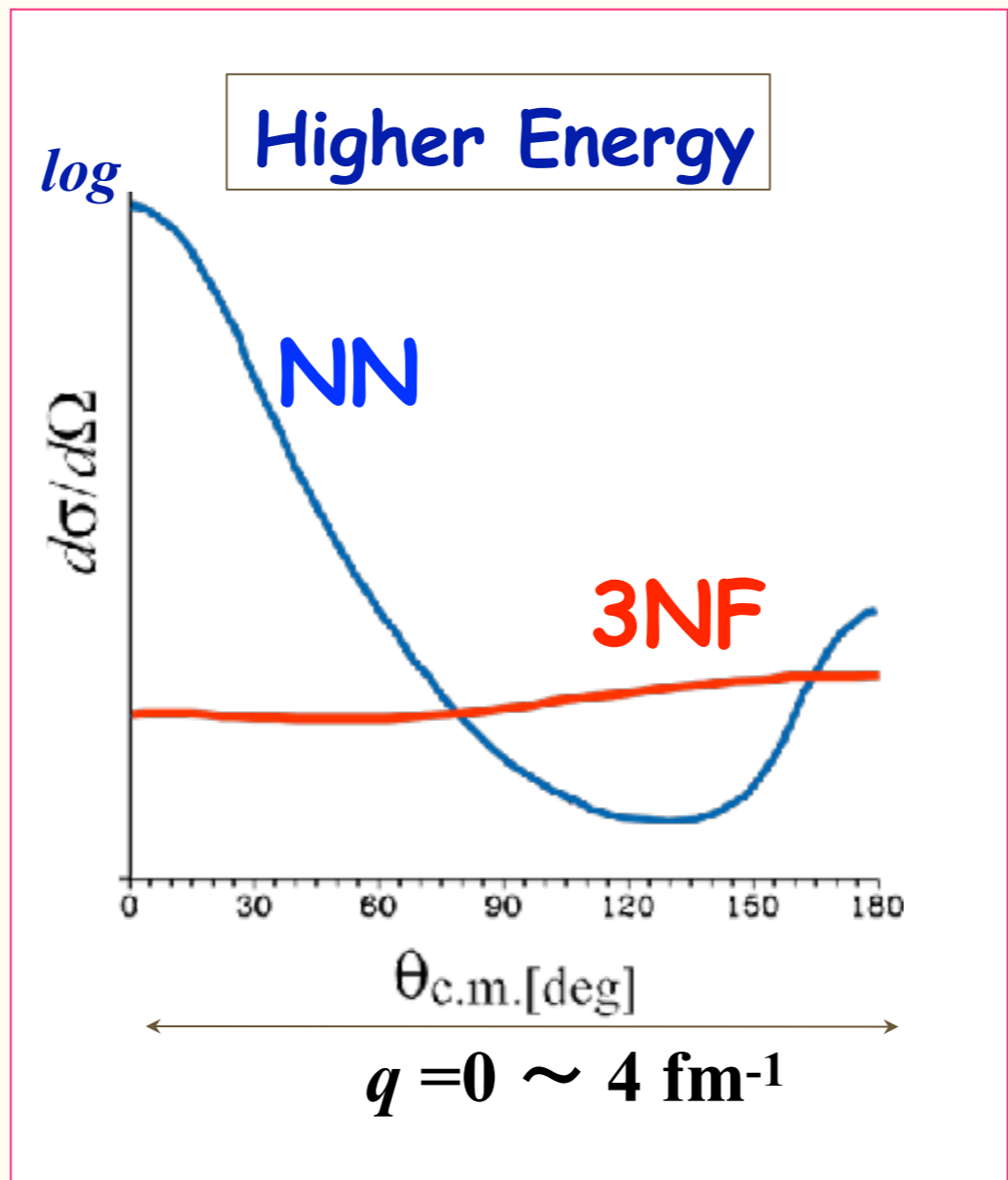
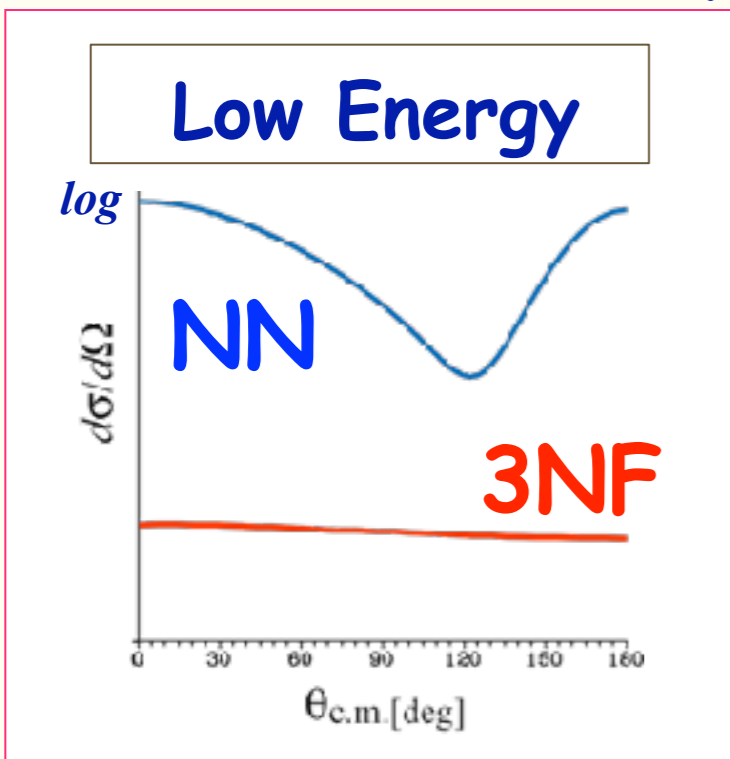
Where is the hot spot for study of 3NFs ?

Nucleon-Deuteron Scattering

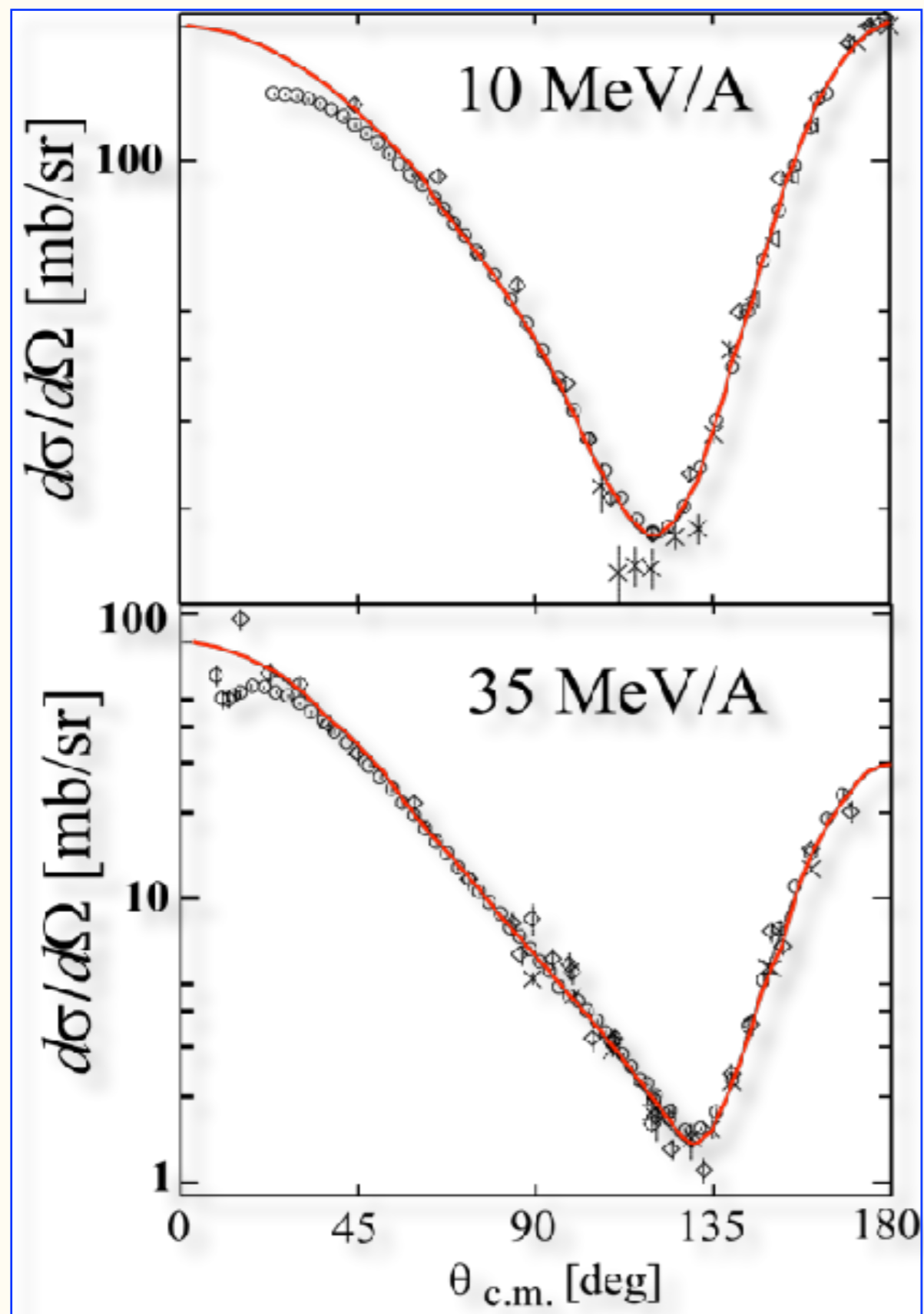
To study momentum & spin dependences
 Iso-spin dependence : T=1/2 only

Predictions by H. Witala et al. (1998)

Cross Section minimum for Nd Scattering at ~ 100 MeV/nucleon



Nd Scattering at Low Energies ($E \leq 30$ MeV/A)



⊙ High precision data are explained by Faddeev calculations based on 2NF. (Exception : A_y, iT_{11})

No signatures of 3NF

Exp. Data from
Kyushu, TUNL, Cologne etc..

Observables for Nd Scattering

• Differential Cross Section

• Overall Strength

➤ Absolute Quantity : normalization to pp or np data

$$\frac{d\sigma}{d\Omega} = \frac{\text{yields}}{(\text{target thickness}) \times (\text{beam charge}) \times (\text{solid angle}) \times (\text{efficiency})}$$

• Spin Observables :

– Analyzing Powers

• Vector Analyzing Power : iT_{11}

– $(L \cdot S)$ interaction

• Tensor Analyzing Power : T_{20}, T_{21}, T_{22}

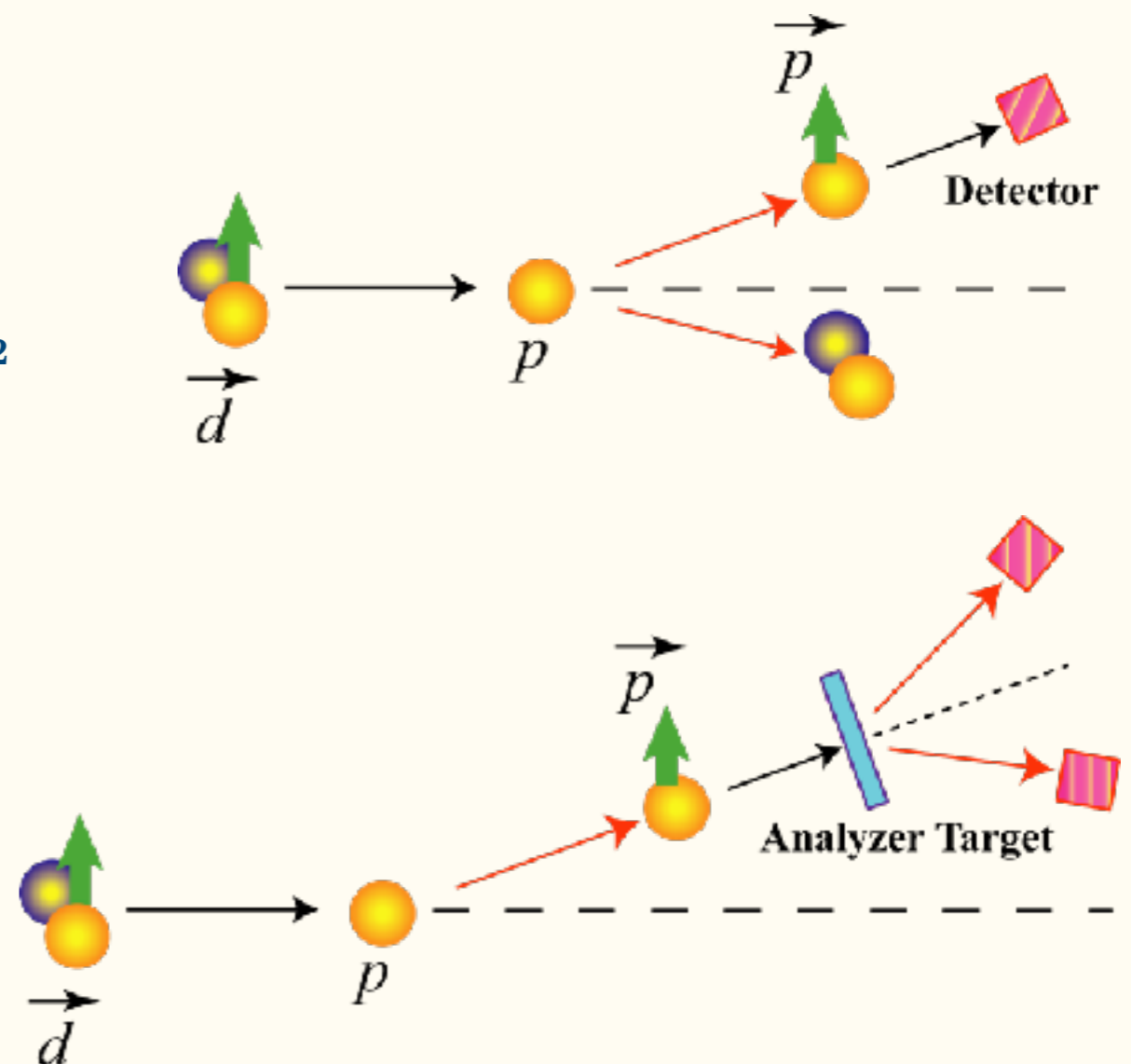
– Tensor interaction (D-state)

– Higher order $(L \cdot S)$ interaction

– Polarization Transfer Coefficient : K_{ij}^l

– Spin Correlation Coefficients : $C_{ij,k}$

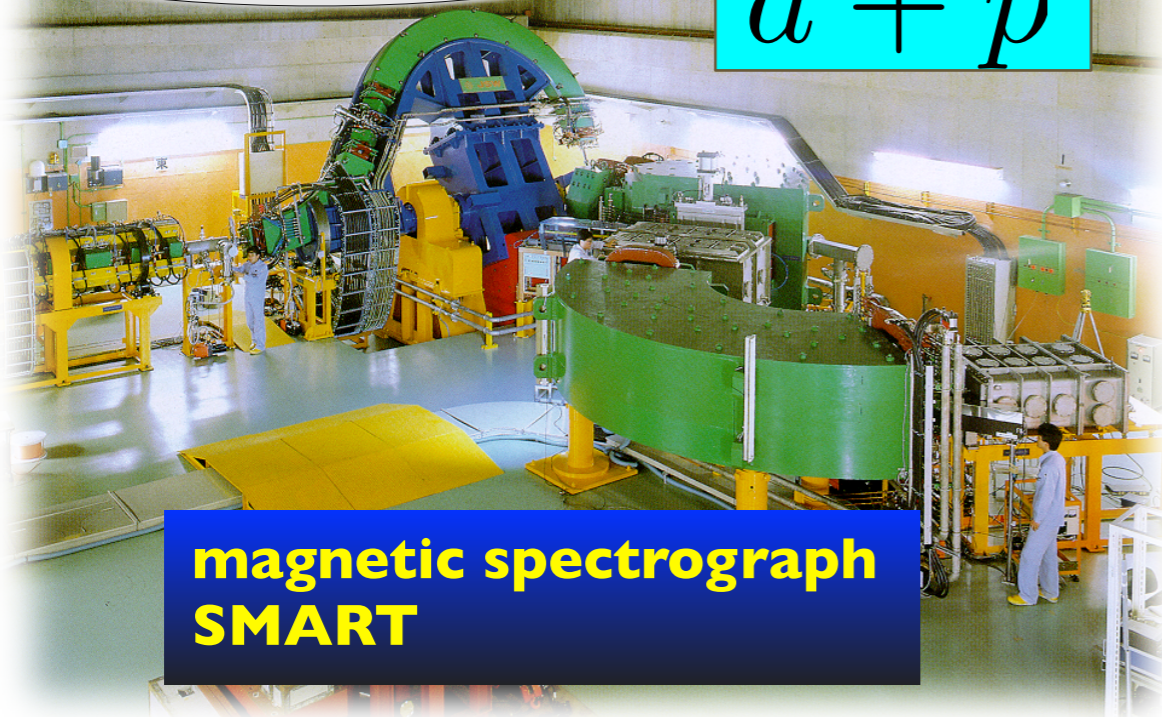
• Spin-Spin interaction



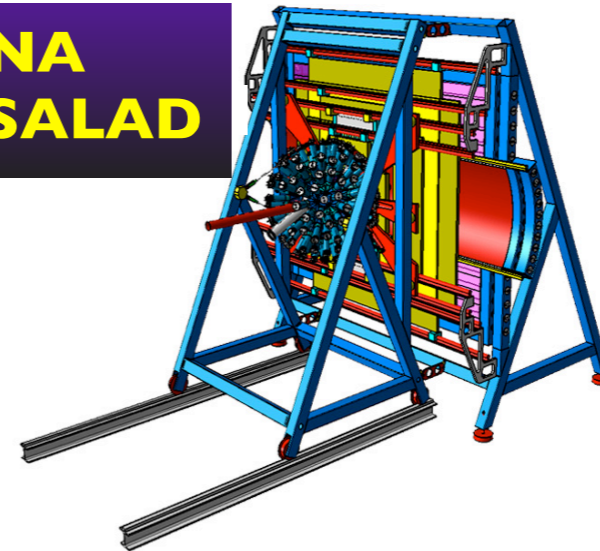
Facilities

RIKEN

$$\vec{d} + p$$

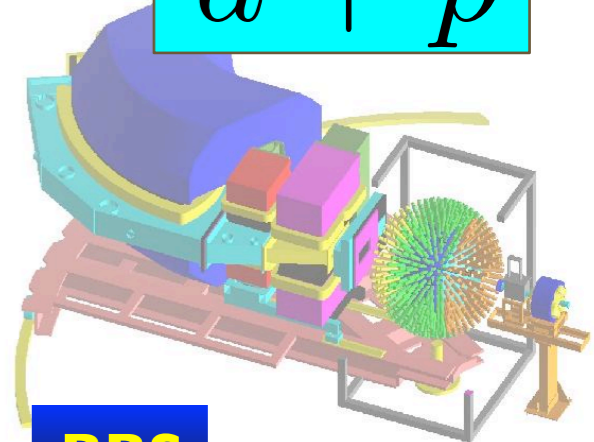


**BINA
& SALAD**



$$\vec{p} + d$$

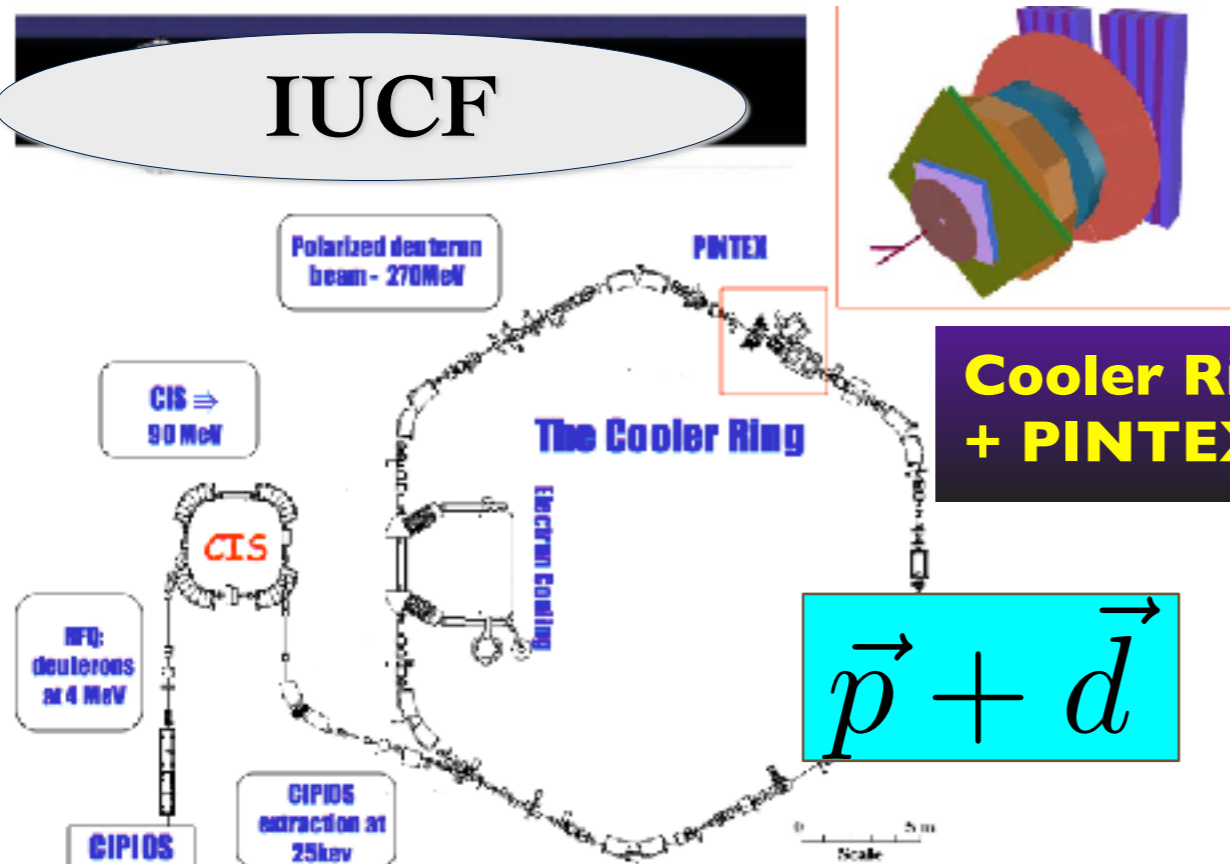
$$\vec{d} + p$$



BBS

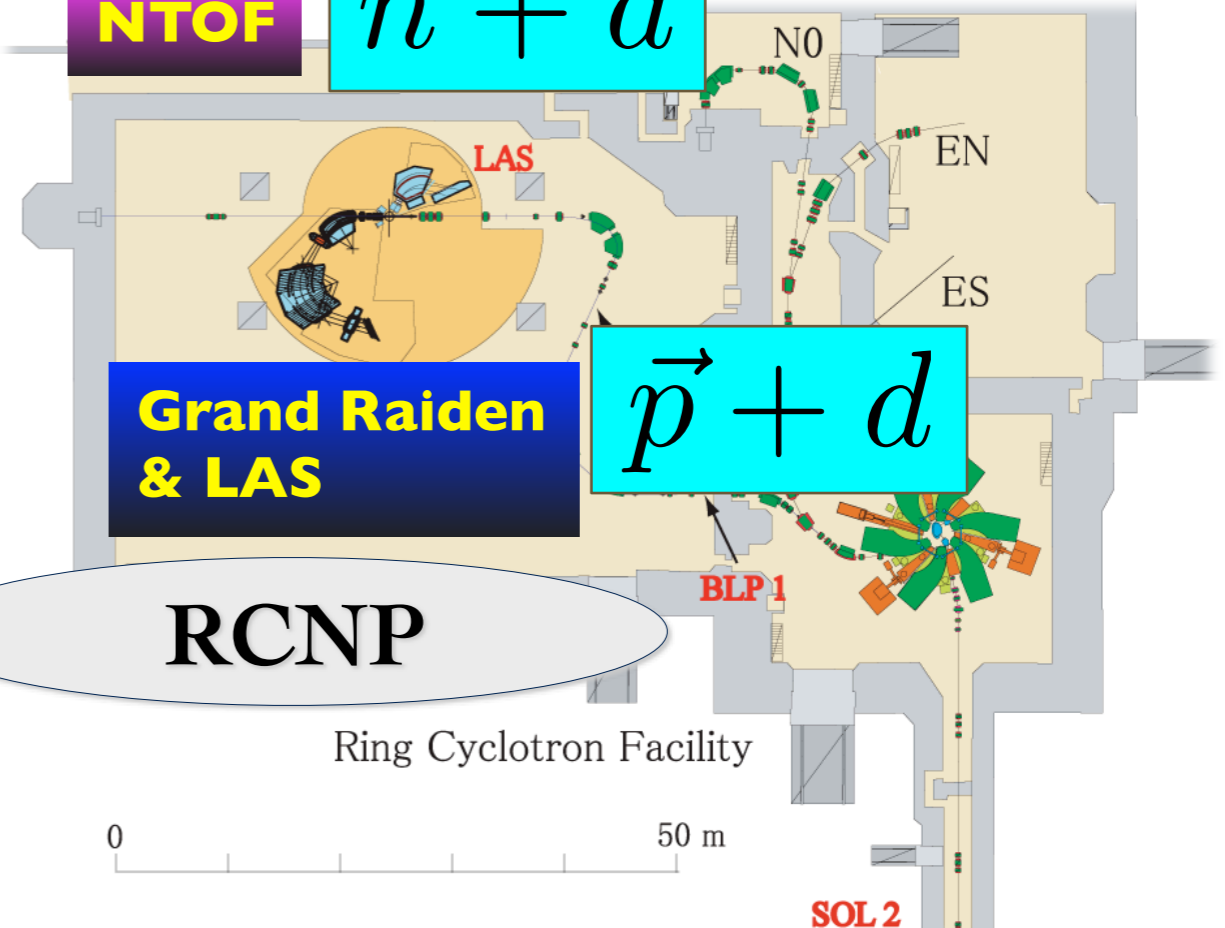
KVI to CCB

IUCF



NTOF

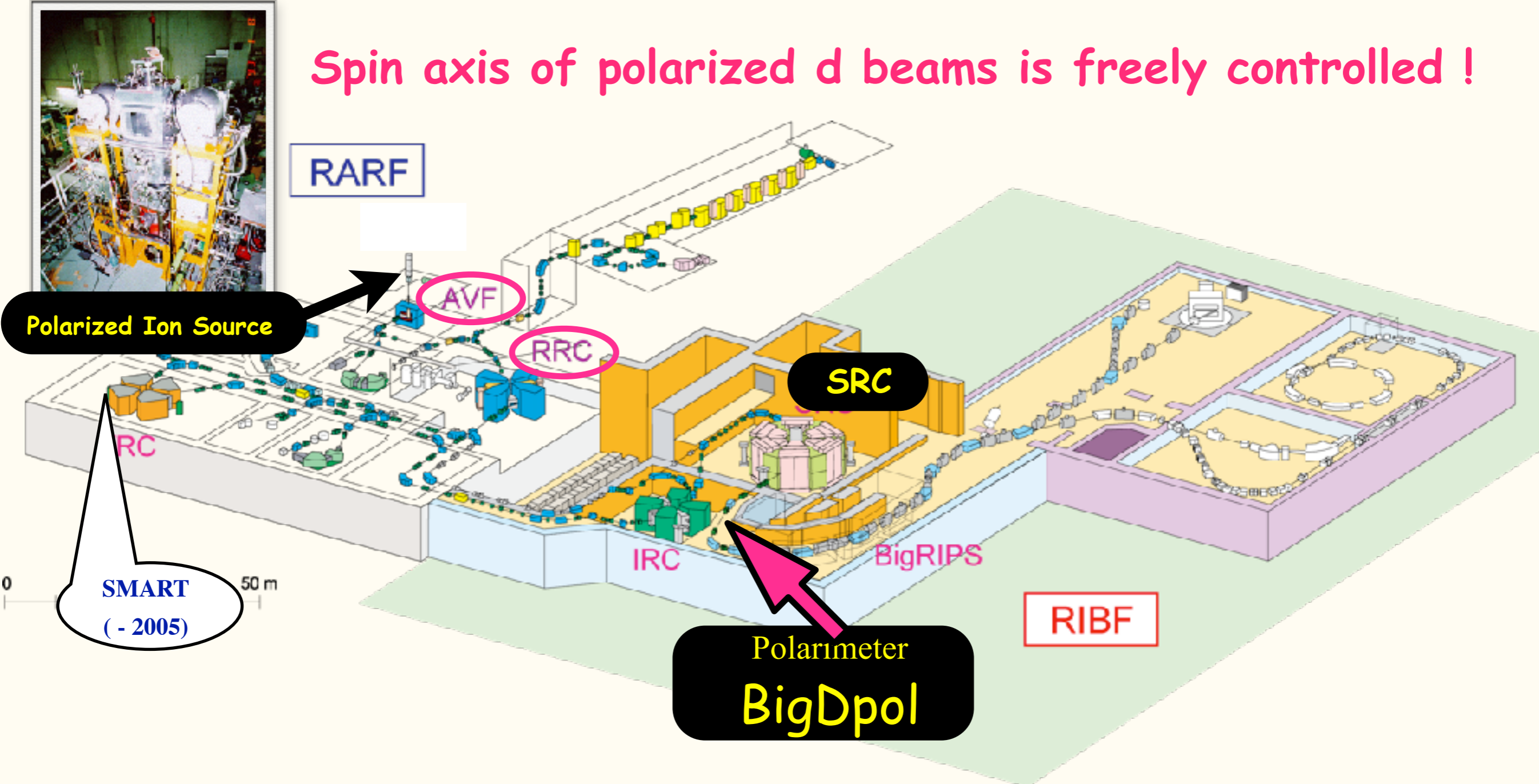
$$\vec{n} + d$$



RIKEN RI Beam Factory (RIBF)

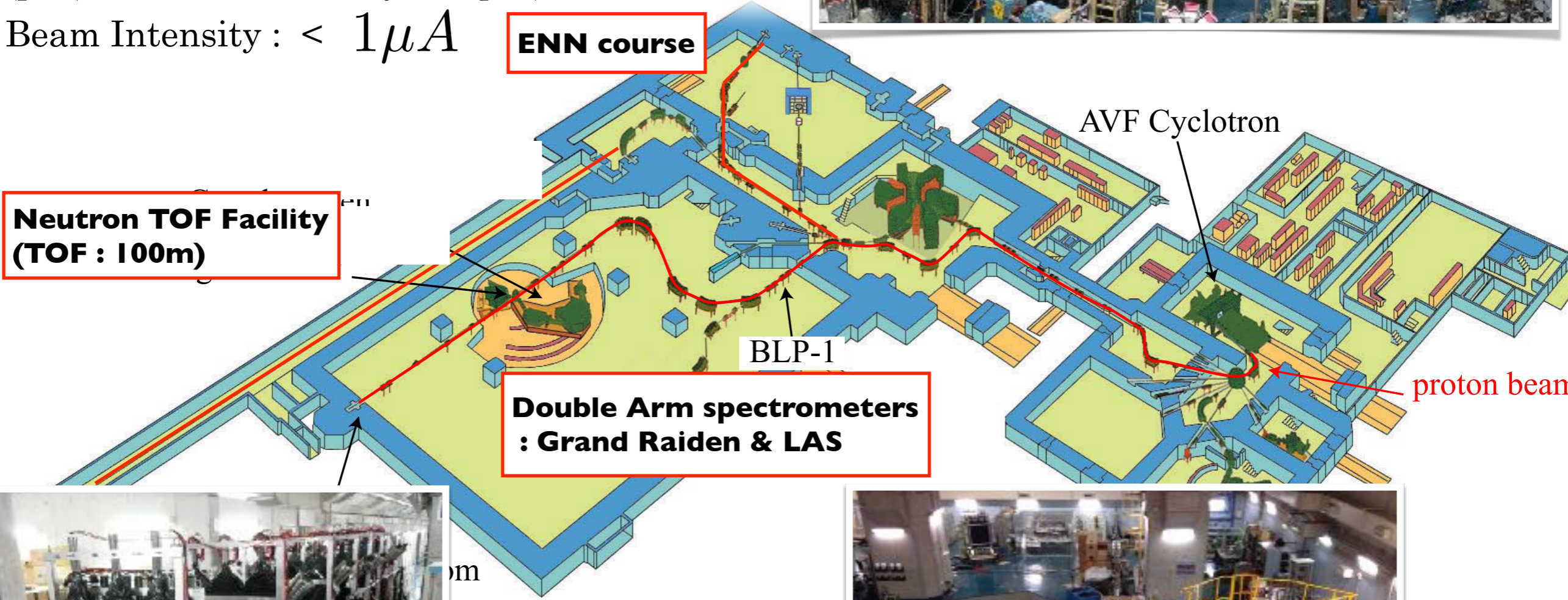
- Polarized *d* beam
 - acceleration by AVF+RRC : 65-135 MeV/nucleon
 - acceleration by AVF+RRC+SRC : 190-300 MeV/nucleon
 - polarization : 60-80% of theoretical maximum values
- Beam Intensity : < 100 nA

Spin axis of polarized d beams is freely controlled !



RCNP, Osaka University

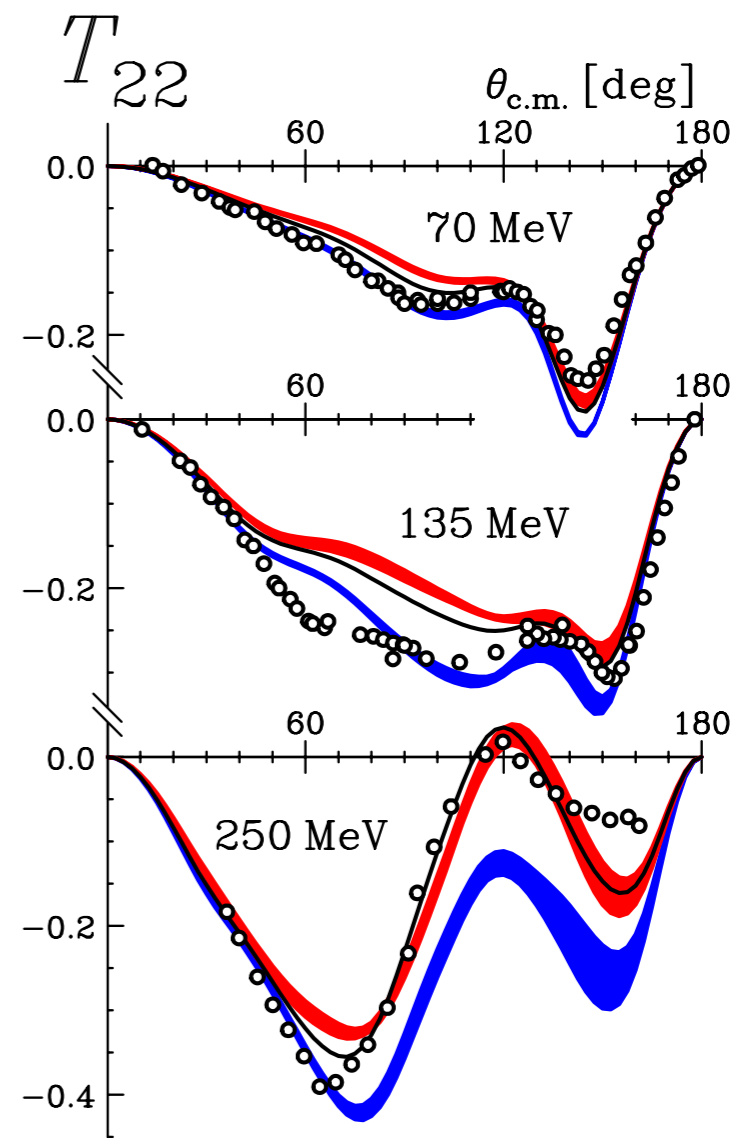
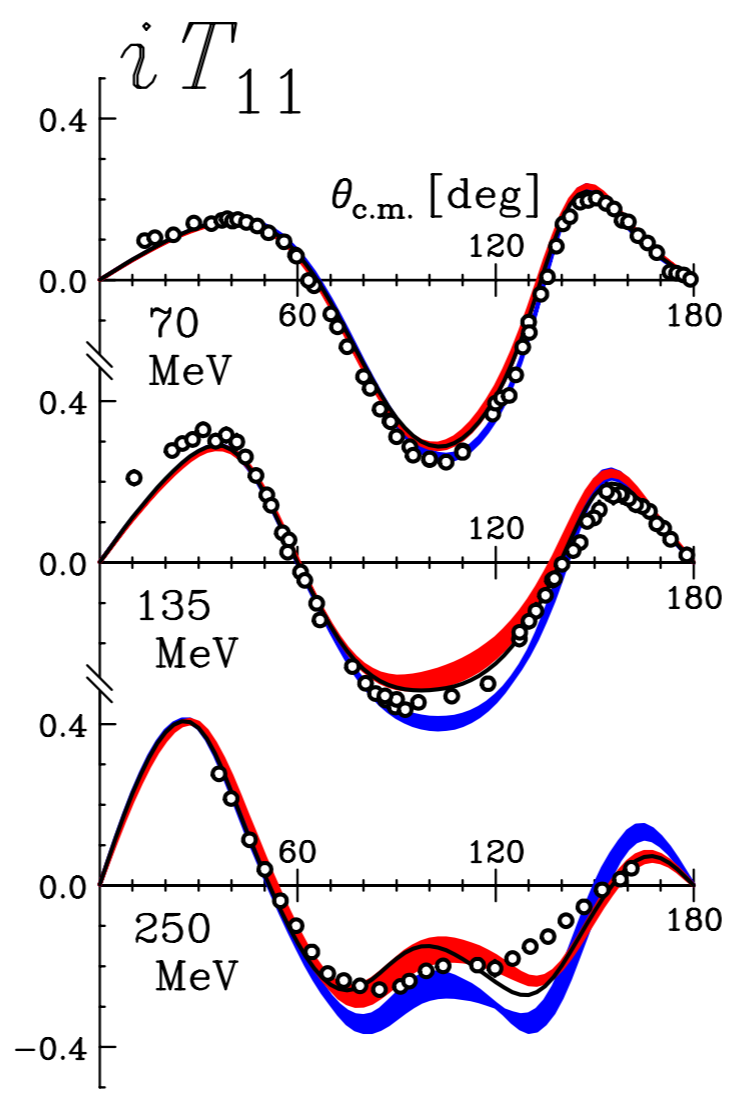
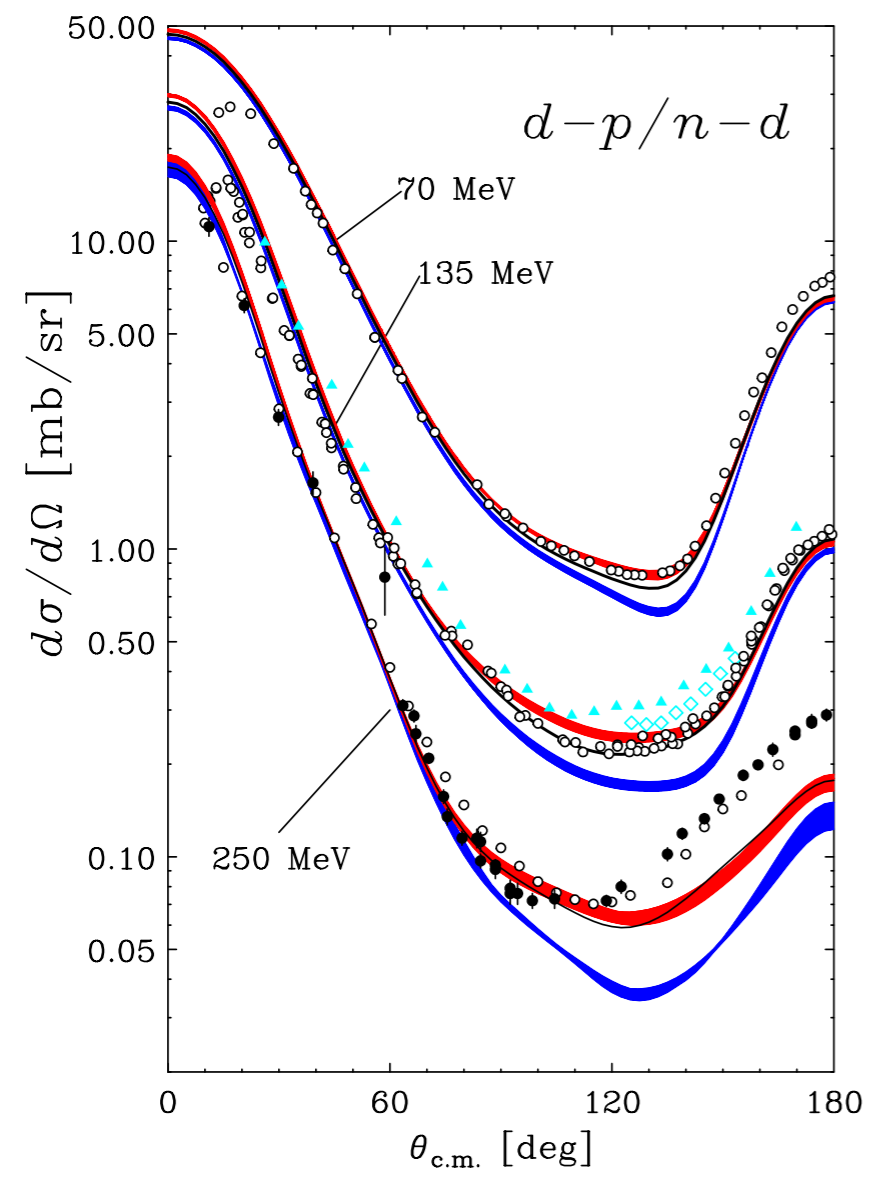
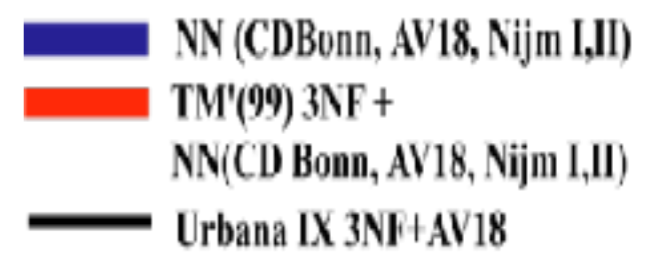
- Polarized p beam : 10 - 420 MeV/nucleon
- Polarized d beam : 5 - 100 MeV/nucleon
 - Polarizations : < 70 %
- (pol.) Neutron beams by ${}^7\text{Li}(p,n)$
- Beam Intensity : < $1\mu\text{A}$



3NF effects in proton-deuteron scattering at 70-250 MeV

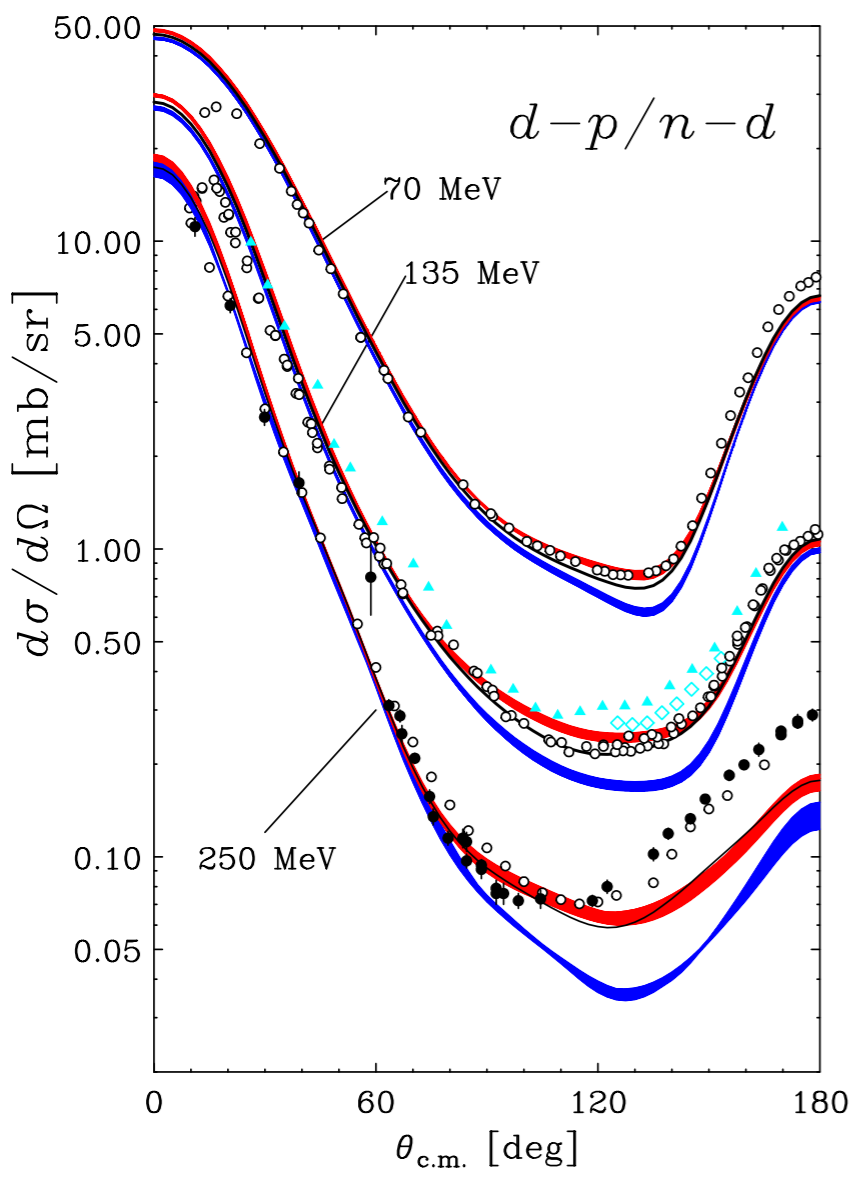
K. S. et al., Phys. Rev. C 65, 034003 (2002),
K. Hatanaka et al., Phys. Rev. C. 66, 044002 (2002),
Y. Maeda et al., Phys. Rev. C 76, 014004 (2007),
K. S. et al., Phys. Rev. C 89, 064007 (2014) etc...

- **Clear signatures** of 3NF Effects in the cross section minimum.
- 3NF effects become larger with increasing an incident energy.
- Spin dependent parts of 3NFs are deficient.
- **Serious discrepancy** at backward angles at higher energies

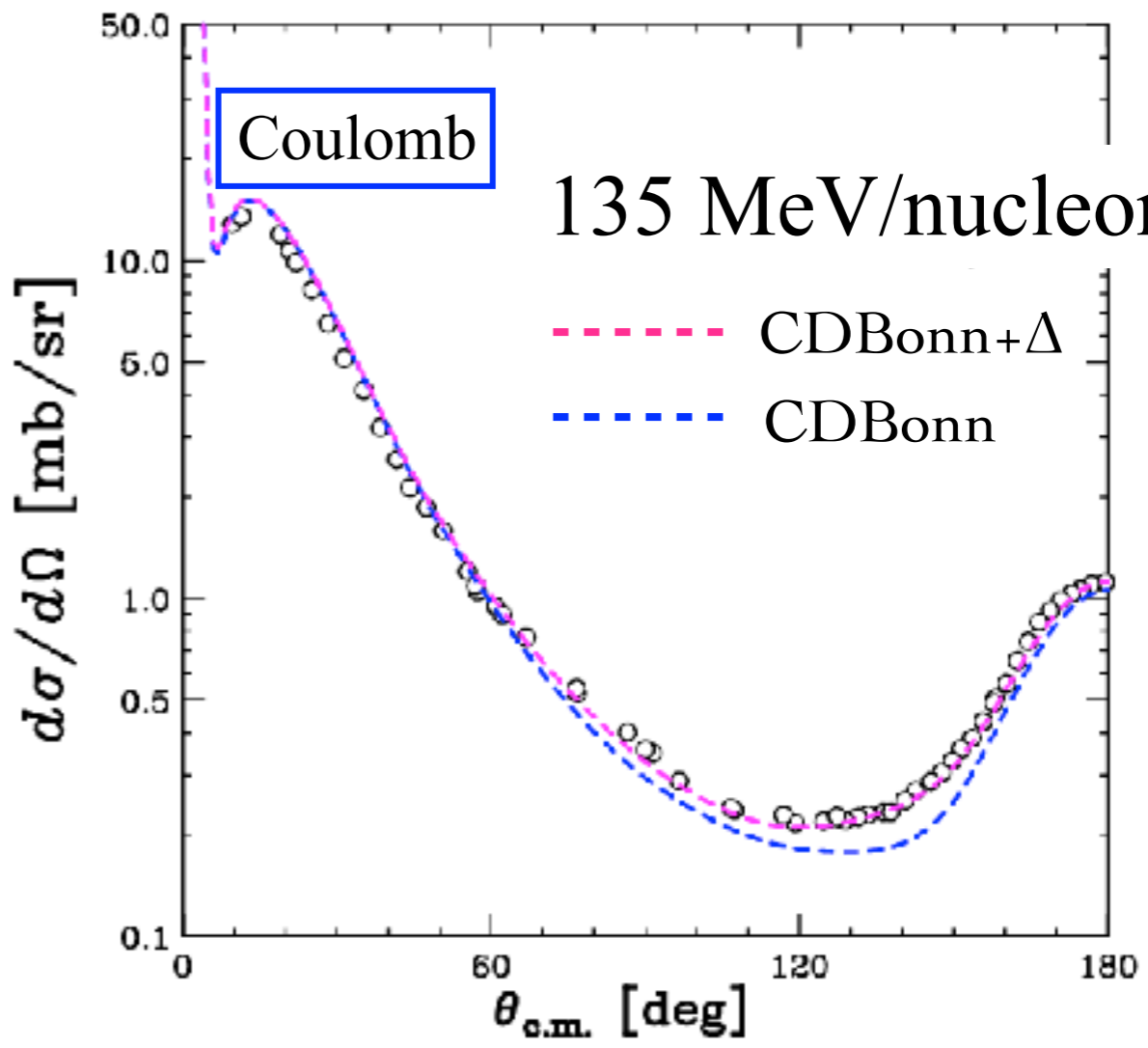


3NF effects in proton-deuteron scattering at 70-250 MeV

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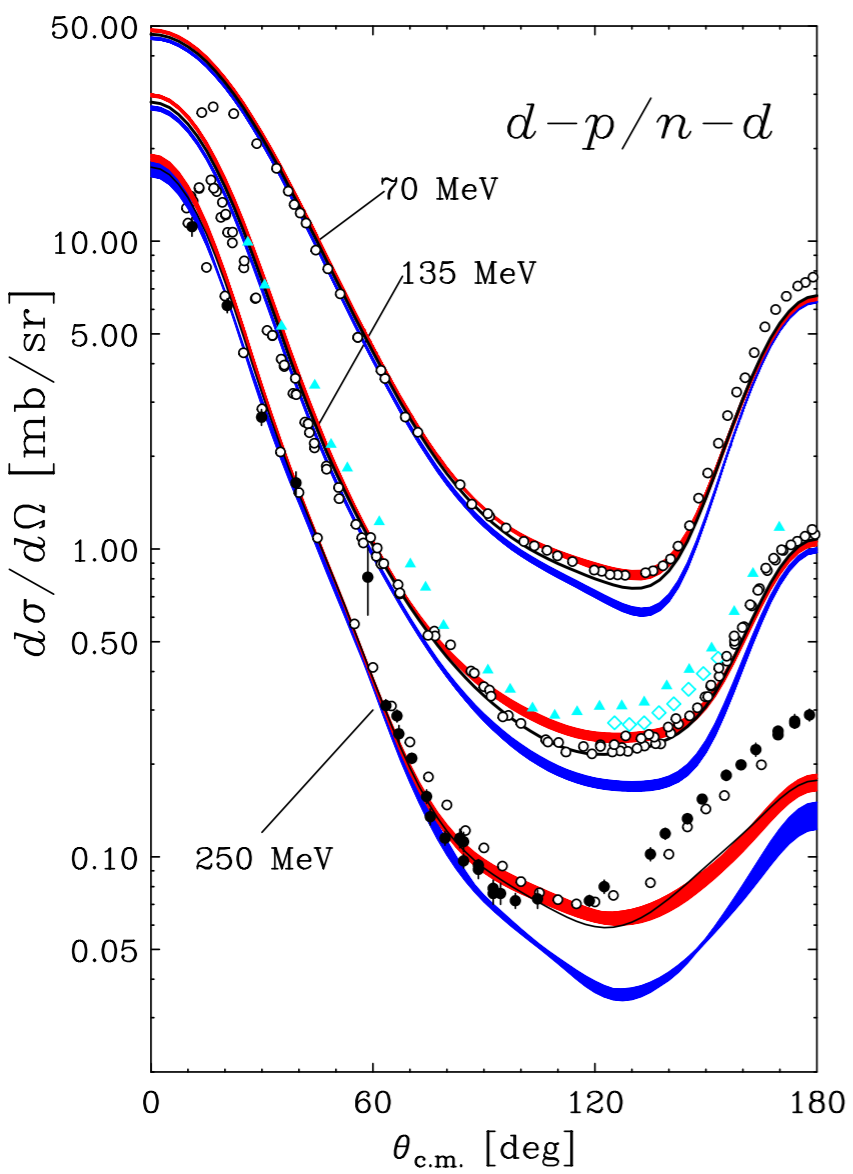
Coupled channel approach with Nucleon & Δ -isobar



A. Deltuva et al., PRC 68, 024005 (2003)
 A. Deltuva et al., PRC 71, 054005 (2005)

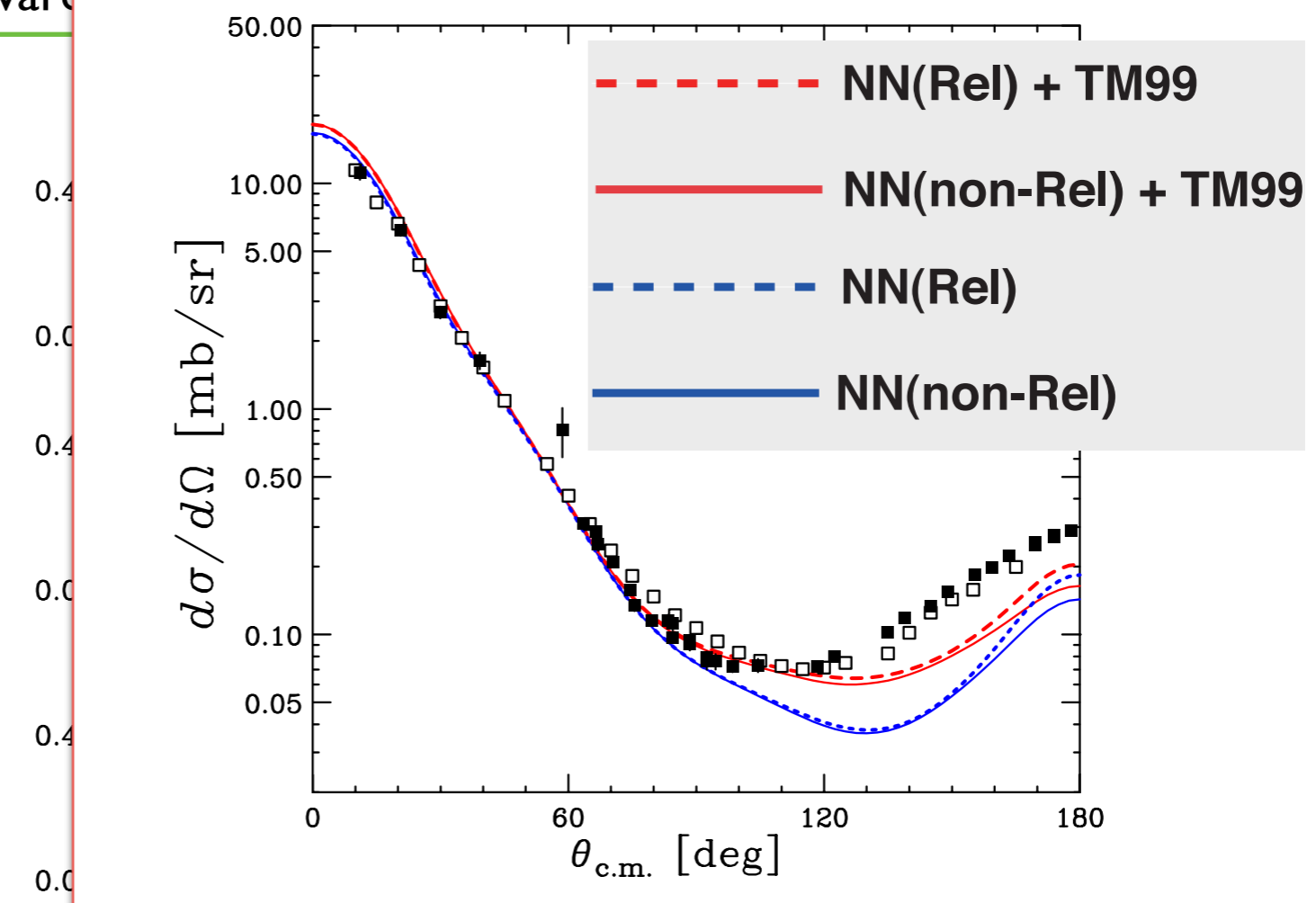
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Relativistic Faddeev Calculations with TM'99 3NF

pd/nd @ 250 MeV



Relativistic effects are visible at backward angles, but small.

So far ...

Nucleon-Deuteron Scattering at ~ 100 MeV/nucleon

- First Evidence of 3NF effects
- Defects of existing 3NF models

From Now

 Deuteron-Proton Scattering at ~ 100 MeV/N : *Golden window of 3NFs*

- Determine 3NFs based on χ EFT Nuclear Potential
- High-precision measurement of Spin Correlation Coefficients

 Proton- ^3He Scattering at ~ 100 MeV/N : *New Probe of 3NF Study*

- First Step from Few to Many
- 3NFs of isospin channel of $T=3/2$

χ EFT & dp elastic scattering

χ EFT 2NFs have achieved to high-precision.

5th order of NN potentials (N4LO+) reproduce pp(np) data with $\chi^2/\text{datum}=1.00$

P. Reinert, H. Krebs, E. Epelbaum EPJA 54, 86 (2018)

dp elastic scattering data show necessities for the N4LO 3NFs.

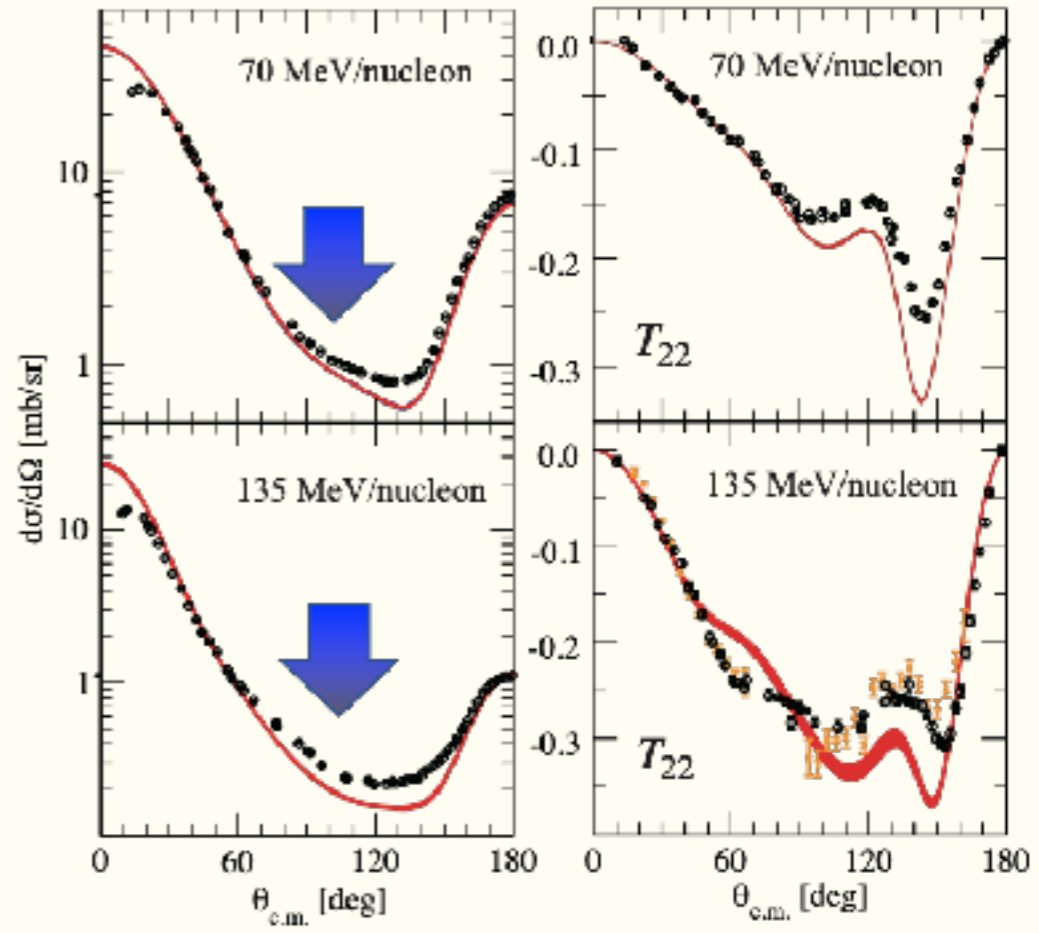


Cross Section minimum region for dp elastic scattering at $\sim 100\text{MeV}/\text{nucleon}$ are "Golden windows for N4LO 3NFs".

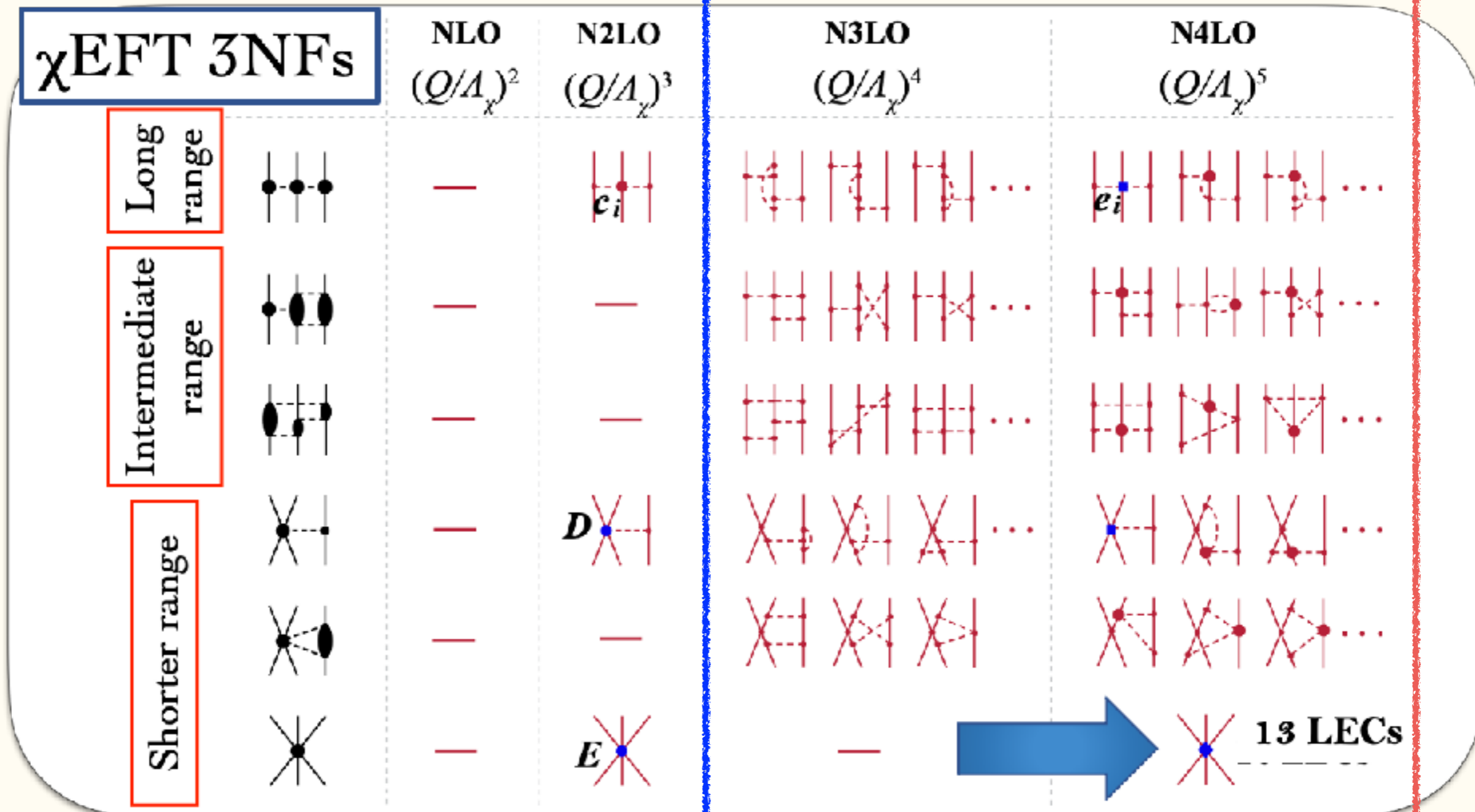
LENPIC collaboration,
Phys. Rev. C 98, 014002 (2018)

dp scattering & N4LO χ EFT 2NFs

K. S. et al., Phys. Rev. C 96, 064001 (2017)



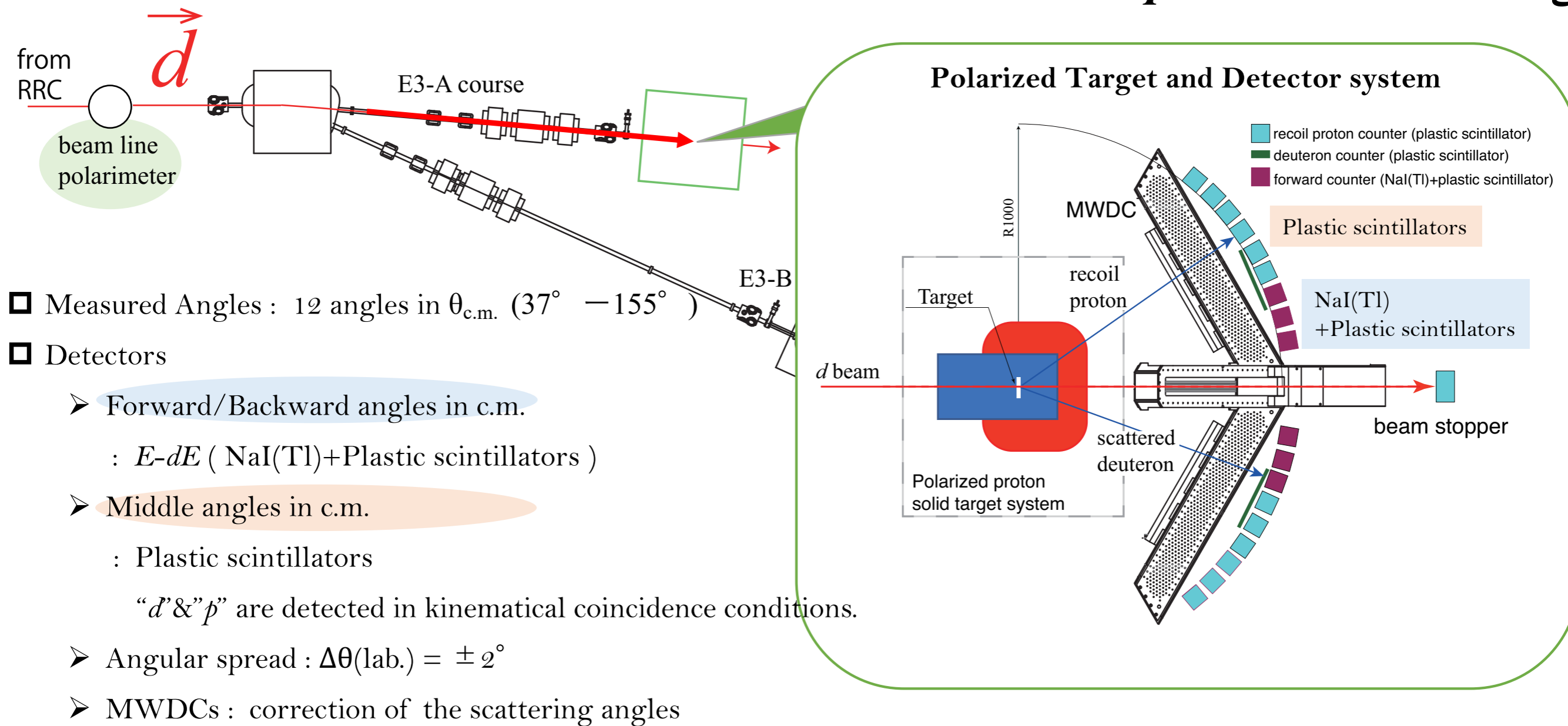
NN Interactions with $R = 0.9$ fm
E. Epelbaum, H. Krebs, and U.-G. Meißner,
Phys. Rev. Lett. 115, 122301 (2015)



L. Girlanda, et al., Phys. Rev. C 84, 014001 (2011)

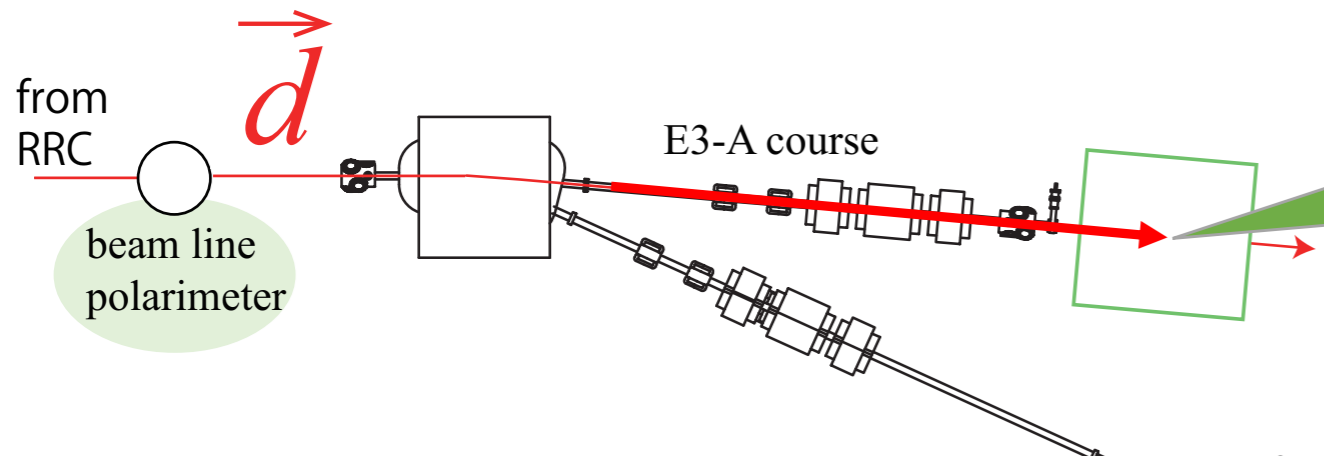
L. Girlanda, et al., Phys. Rev. C 102, 019903 (2020).

Layout of Experiment of the spin correlation coefficients for dp Elastic Scattering

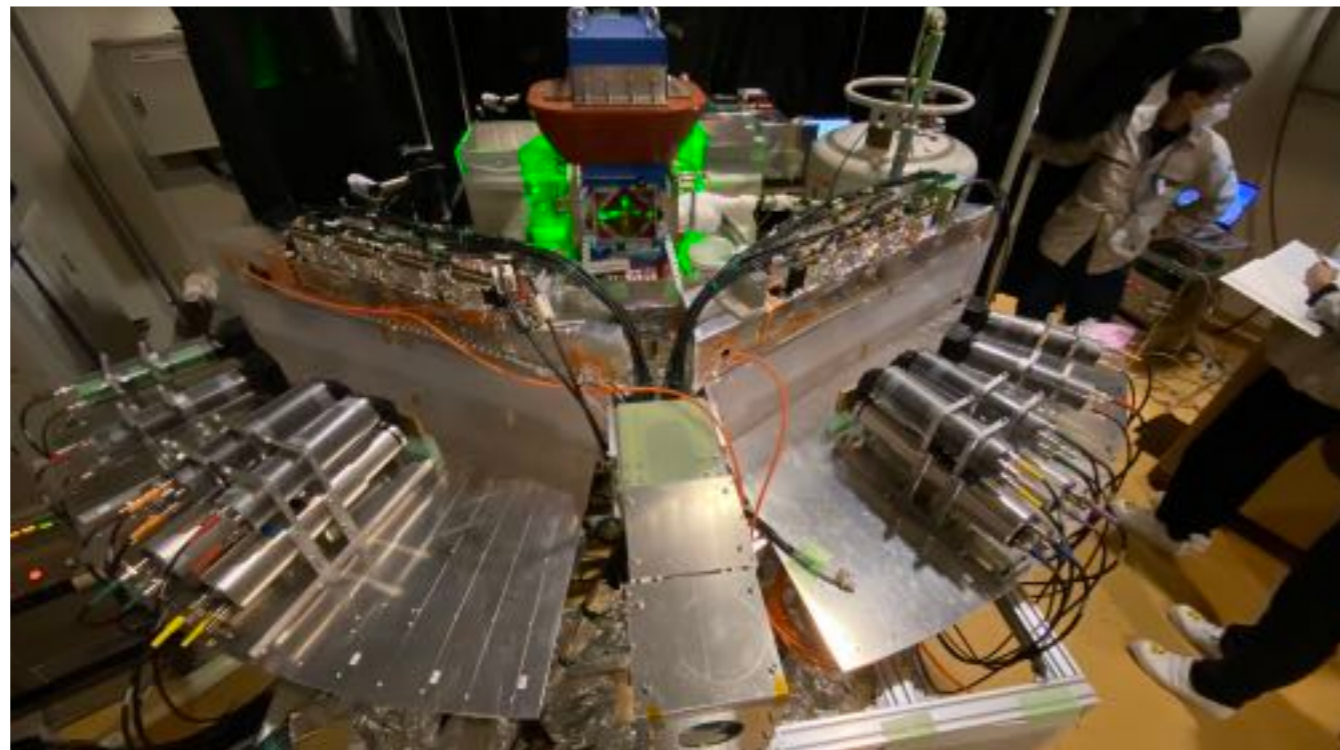
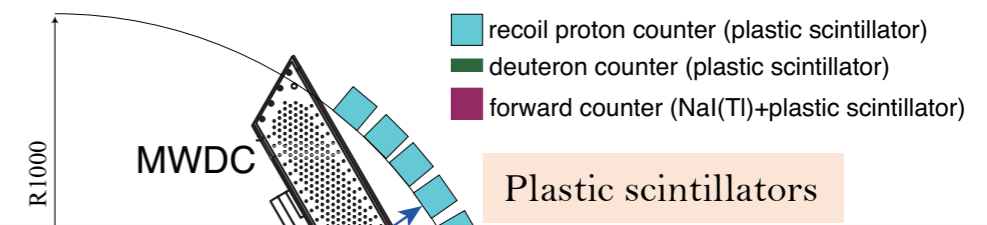


All experimental equipments are in preparation now.

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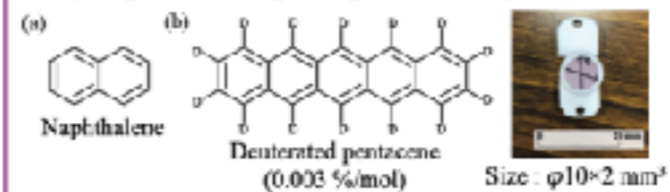
Polarized Target and Detector system



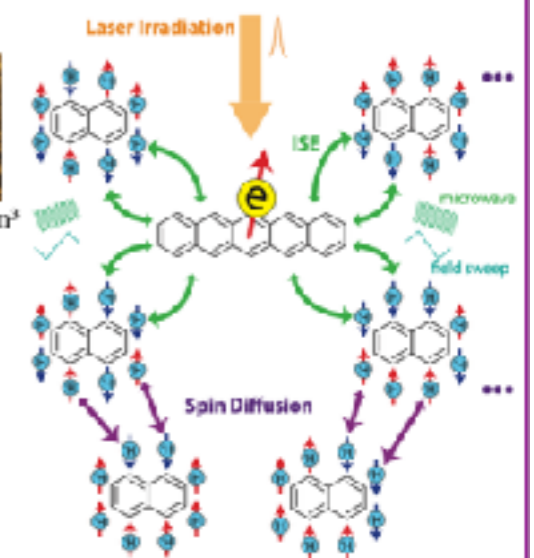
Polarized Solid Proton Target

Triplet Dynamic Nuclear Polarization (Triplet-DNP)

Target : pentacene doped naphthalene single crystal



- Optical excitation of electrons in pentacene and decay to triplet state (T_1)
→ **Electron polarization of ~90%**
- Polarization transfer** from electrons to protons via microwave irradiation + field sweep
- Proton polarization localized around pentacene spontaneously diffuse and average out
= **Spin diffusion**



All experimental equipments are in preparation now.

Poster by Yuko Saito

$p+{}^3\text{He}$ Scattering

Talk by Atomu Watanabe

1. Four Nucleon Scattering *First Step from Few to Many*
2. Isospin Dependence of 3NFs : $T=3/2$ 3NFs
3. Large 3NF effects *in cross section minimum at intermediate energies*

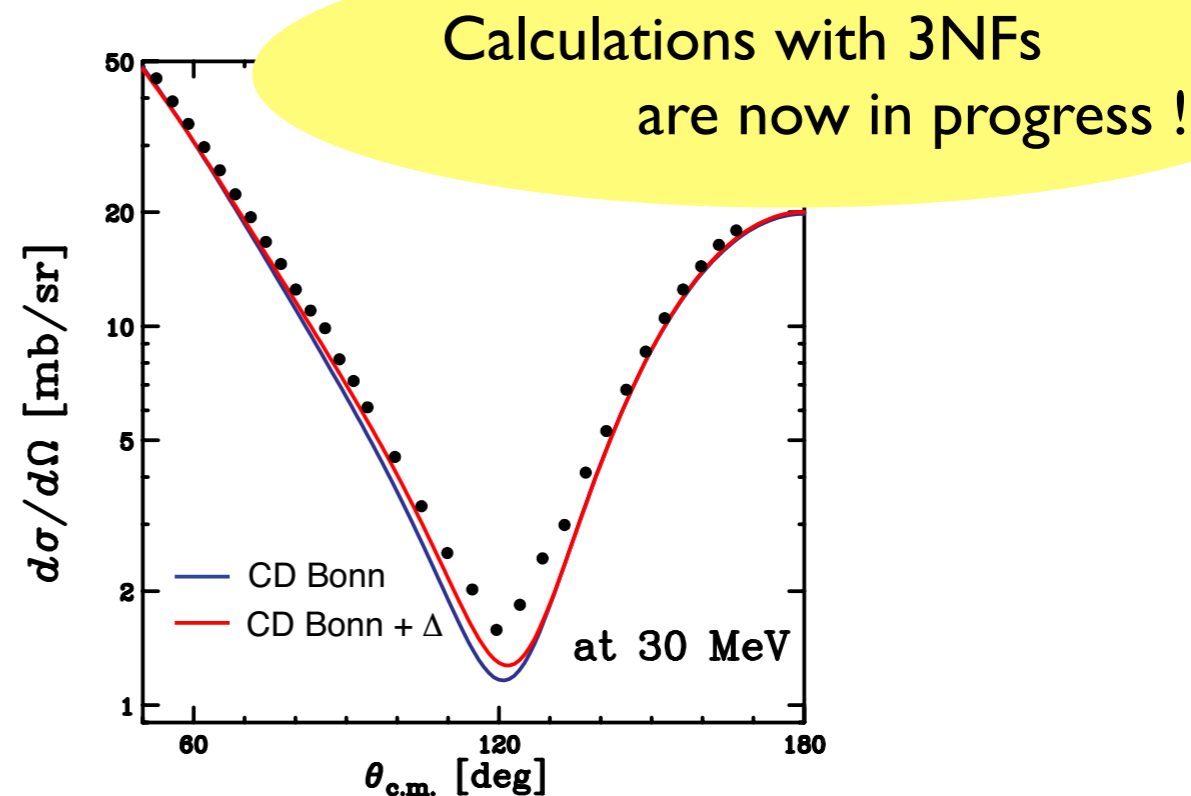
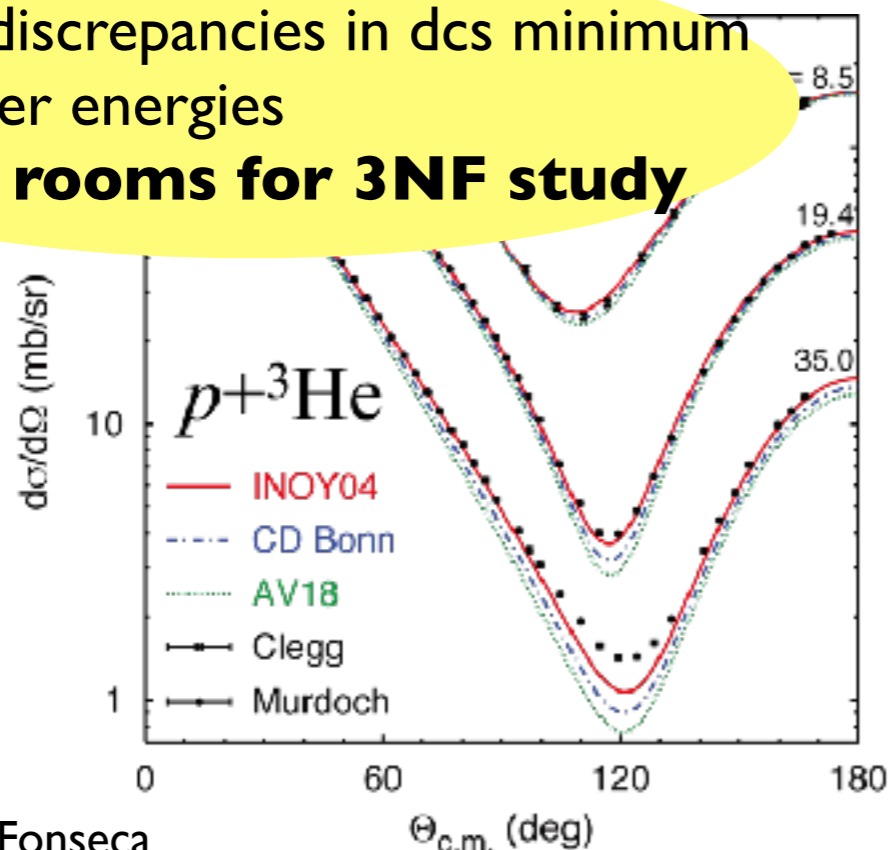
Theory in Progress

Calculations above 4-body breakup threshold energy are available by A. Deltuva et al.

 **new possibilities** for 3NF study in 4N scattering at higher energies

Large discrepancies in dcs minimum at higher energies

New rooms for 3NF study

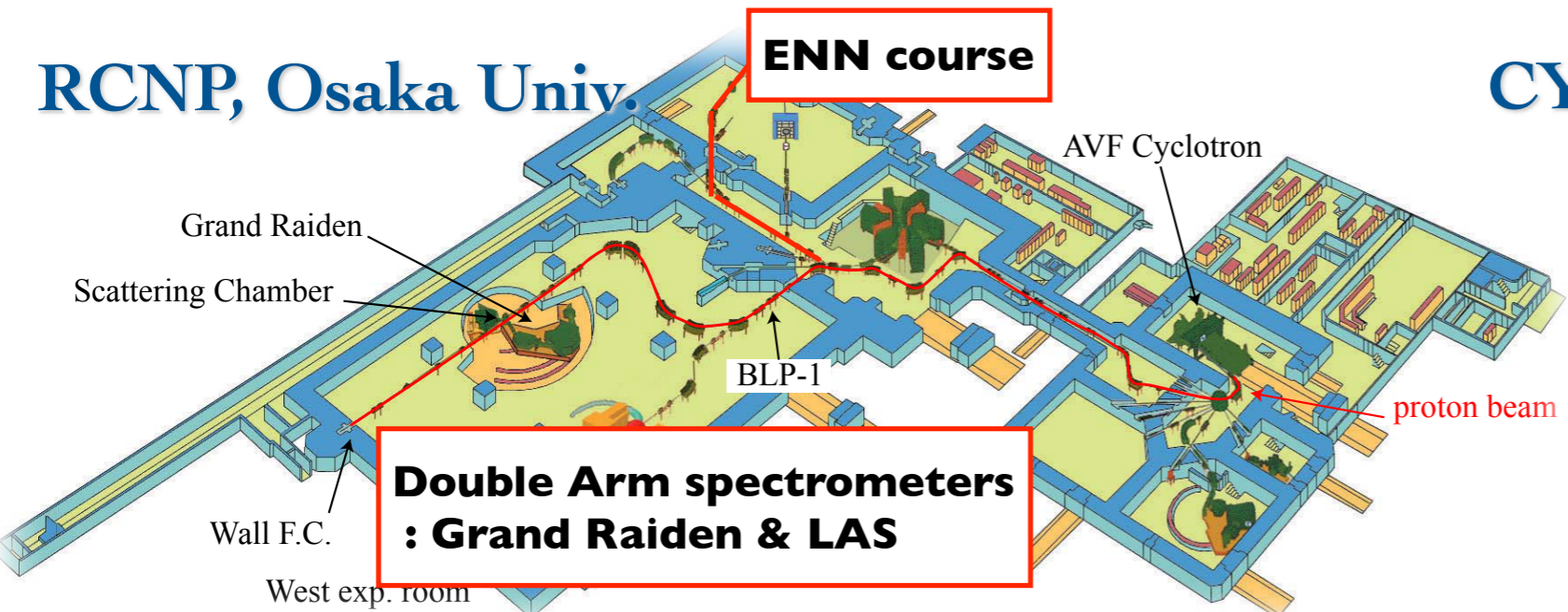


Calculations with 3NFs are now in progress !

Experiments of $p+^3\text{He}$ at Intermediate Energies from RCNP & CYRIC

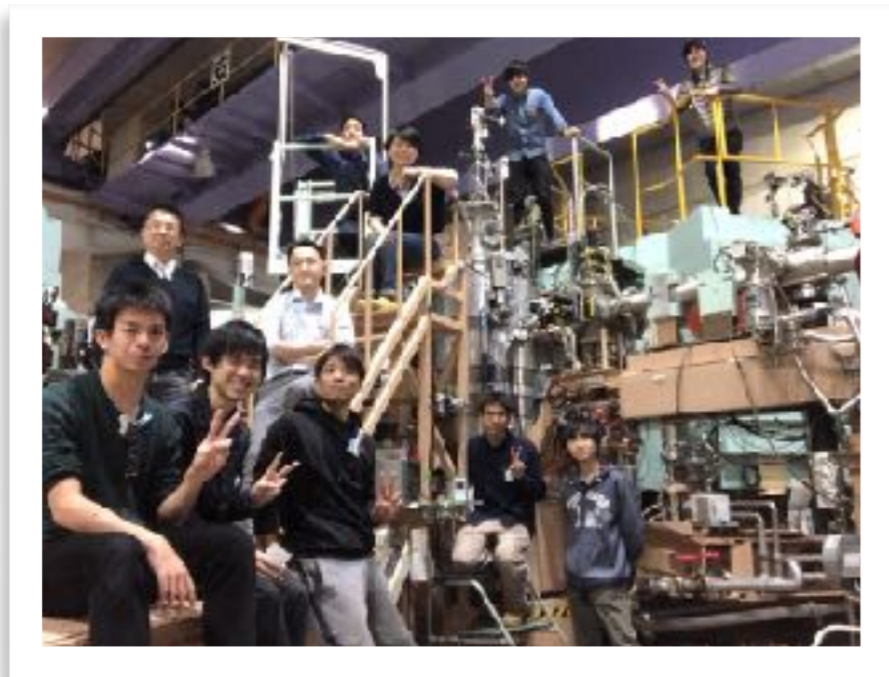
RCNP, Osaka Univ.

CYRIC, Tohoku Univ.



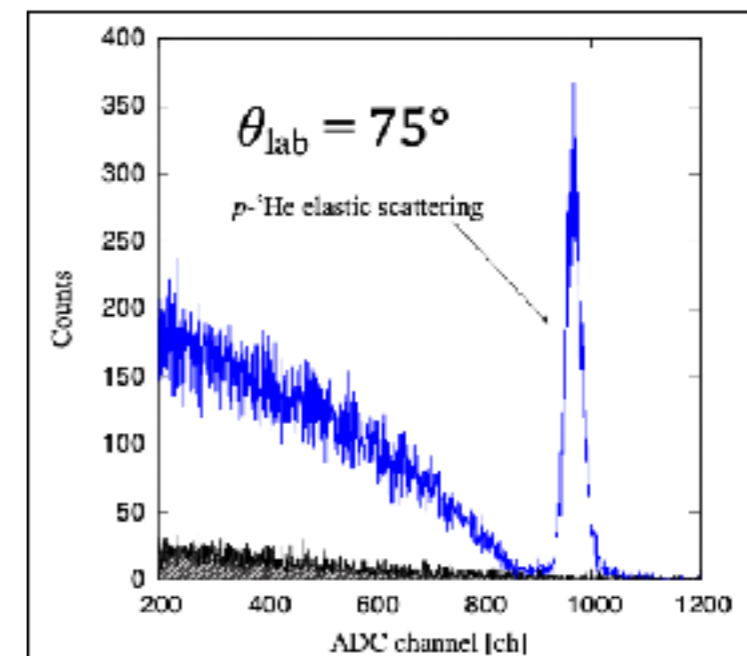
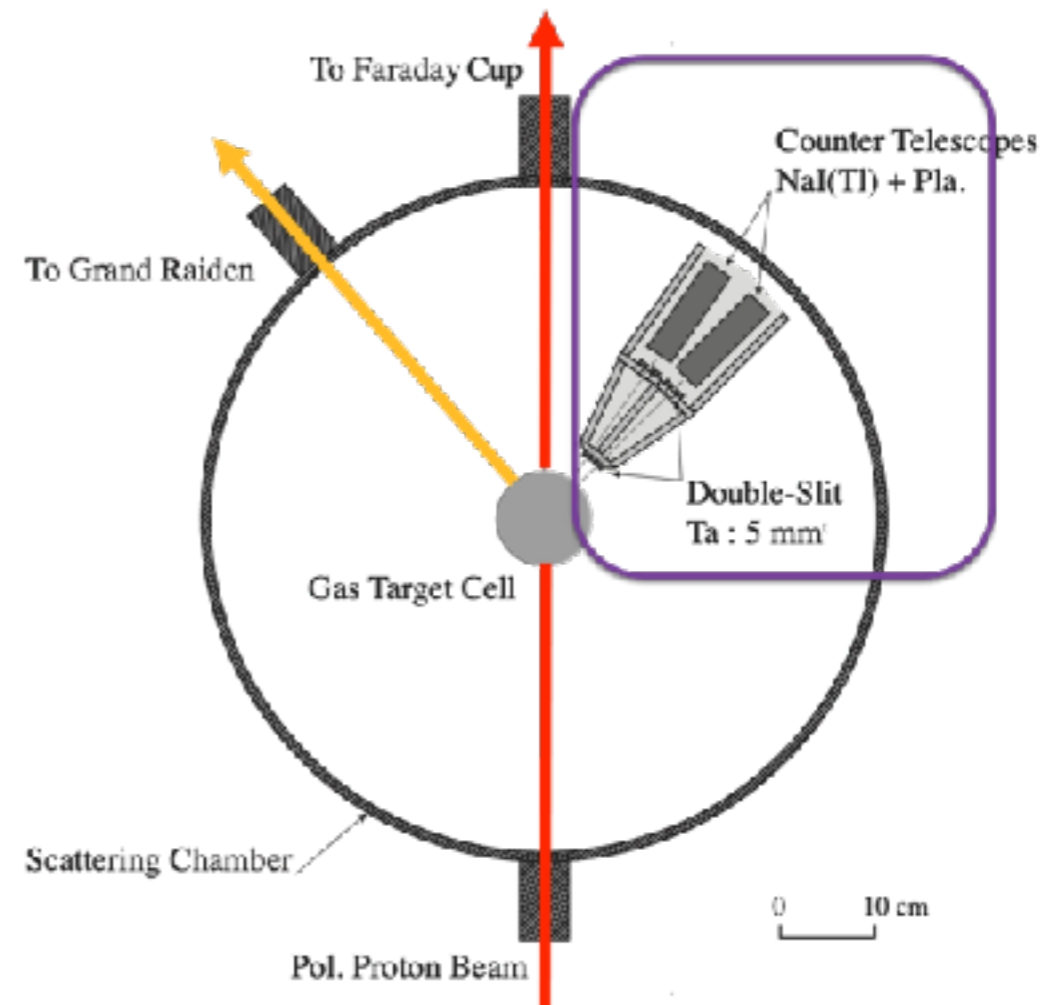
- Polarized p beam : 10 - 420 MeV
 - Polarizations : $< 70\%$
- Beam Intensity : $< 1\mu\text{A}$

- p beam : 10 - 80 MeV
- Beam Intensity : 10-20 nA

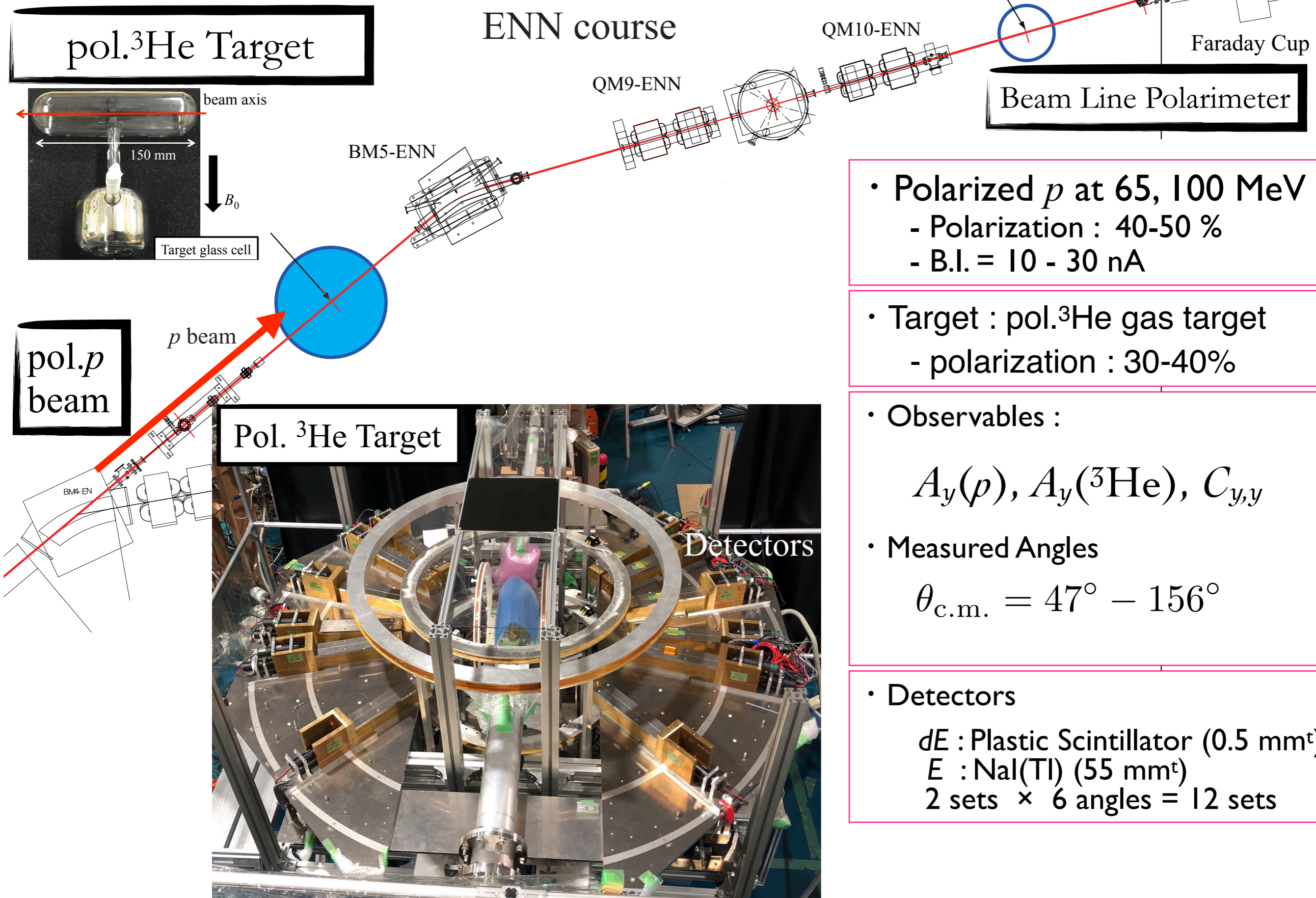


Measurement Condition

- Beam Energy 65 MeV
- Target : ^3He gas
with double slit system
 - 1 atm, room temperature
- Detector system
 - ΔE - E detectors (Plastic+Nal(Tl))
in the scattering chamber
 - Grand Raiden : beam monitor
- Measured Angles :
 $\theta_{\text{c.m.}} = 27^\circ - 170^\circ$ ($\theta_{\text{lab.}} = 20^\circ - 165^\circ$)
- pp scattering
with the same detection setup
 - estimate of the overall systematic uncertainties



pol.p+pol.³He experiment at RCNP



- Polarized p at 65, 100 MeV
 - Polarization : 40-50 %
 - B.I. = 10 - 30 nA

- Target : pol.³He gas target
 - polarization : 30-40%

- Observables :

$$A_y(p), A_y(^3\text{He}), C_{y,y}$$
- Measured Angles

$$\theta_{\text{c.m.}} = 47^\circ - 156^\circ$$

- Detectors
 - dE : Plastic Scintillator (0.5 mm^t)
 - E : NaI(Tl) (55 mm^t)
 - 2 sets × 6 angles = 12 sets

Summary of Measurements for $p+{}^3\text{He}$					
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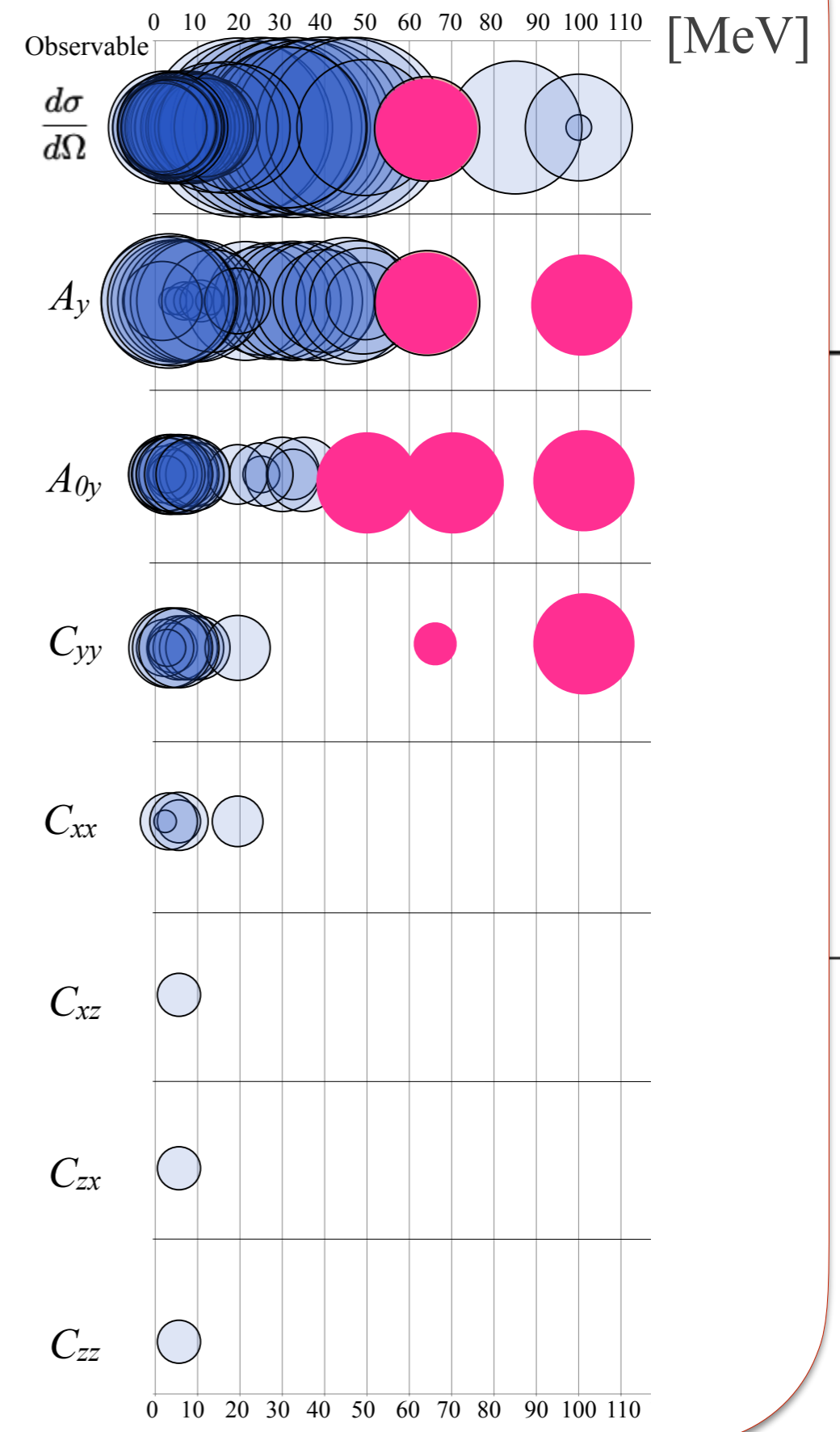
Incident Energy	70 MeV	50 MeV	65 MeV	65 MeV	100 MeV
Beam	p	p	pol. p	pol. p	pol. p
Observables	A_{0y}	A_{0y}	$d\sigma/d\Omega, A_y$	$A_y, A_{0y}, C_{y,y}$	$A_y, A_{0y}, C_{y,y}$
Measured Angles ($\theta_{\text{c.m.}}$)	$46^\circ - 141^\circ$	$47^\circ - 120^\circ$	$27^\circ - 170^\circ$	$47^\circ - 133^\circ$	$47^\circ - 149^\circ$
Facility	CYRIC, Tohoku Univ.	CYRIC, Tohoku Univ.	RCNP, Osaka Univ.	RCNP, Osaka Univ.	RCNP, Osaka Univ.
Exp. Course	41 course	41 course	WS course	ENN course	ENN course

p - ^3He scattering at 5-100 MeV

Summary of Measurements for $p+^3\text{He}$

Incident Energy	70 MeV	50 MeV
Beam	p	p
Observables	A_{0y}	A_{0y}
Measured Angles ($\theta_{\text{c.m.}}$)	$46^\circ - 141^\circ$	$47^\circ - 120^\circ$
Facility	CYRIC, Tohoku Univ.	CYRIC, Tohoku Univ.
Exp. Course	41 course	41 course

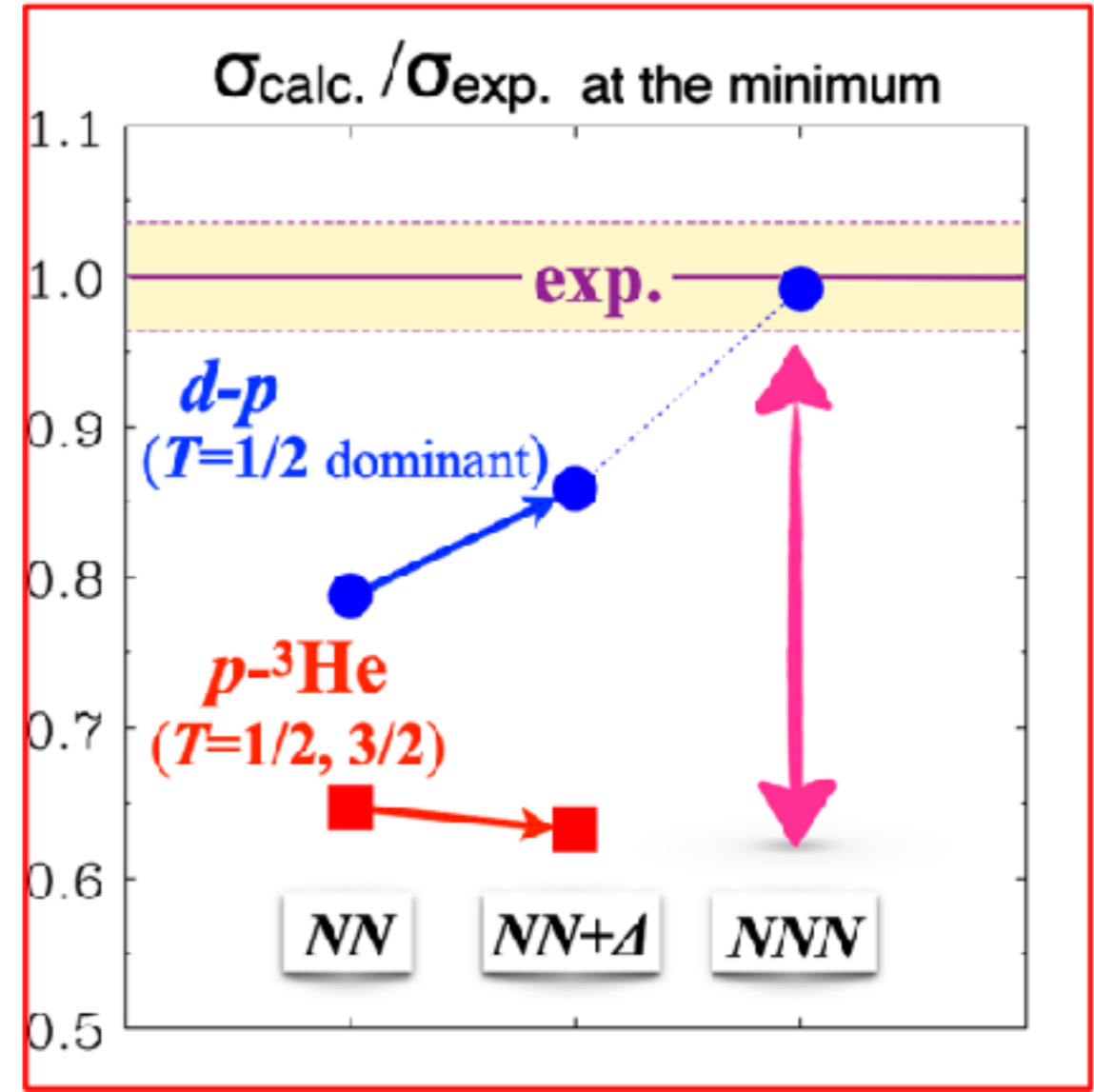
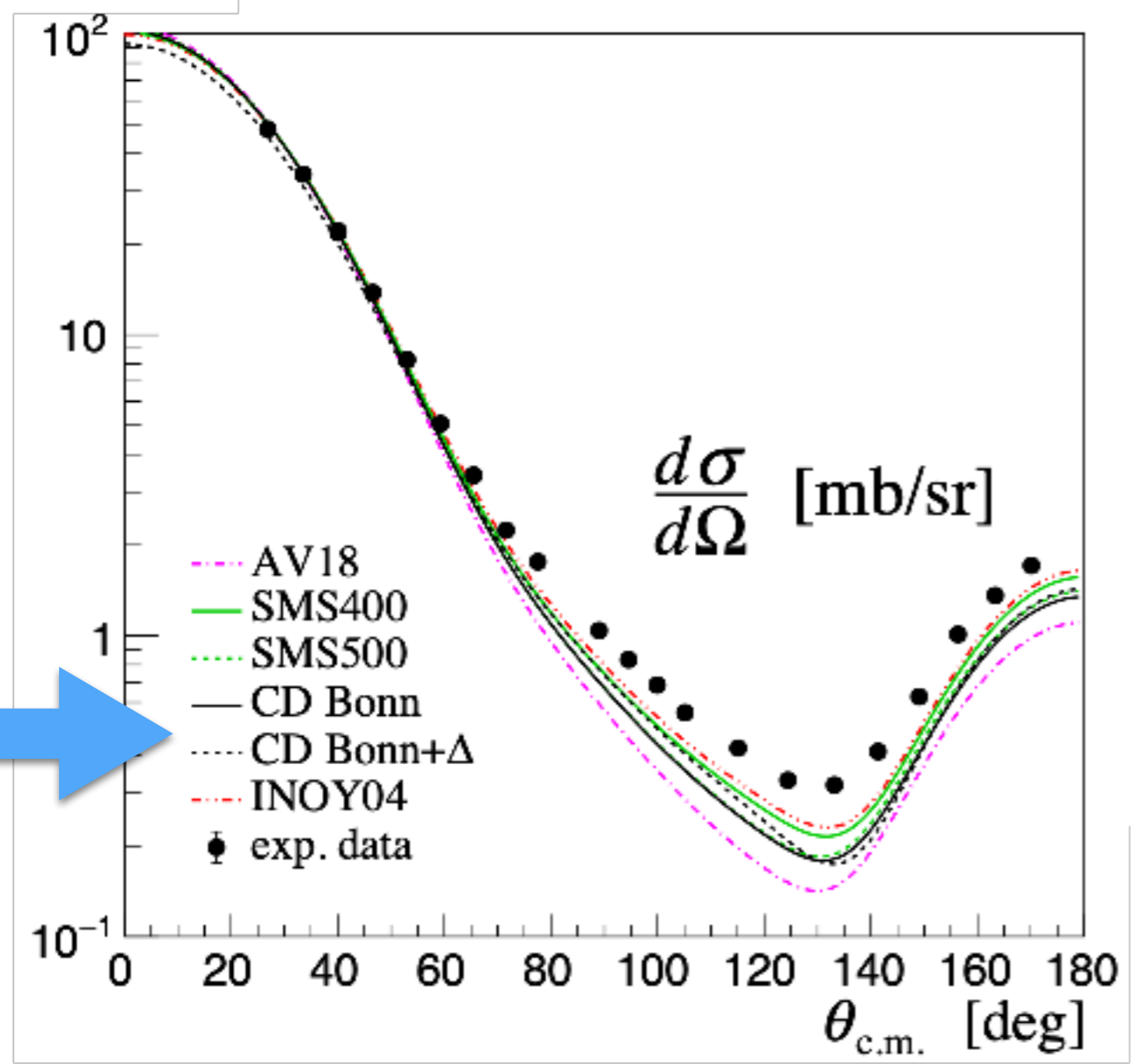
● data from RCNP/CYRIC



New Data of $p+^3\text{He}$ at Intermediate Energies

A. Watanabe et al., Phys. Rev. C 103, 044001 (2021)

Cross Section at 65 MeV

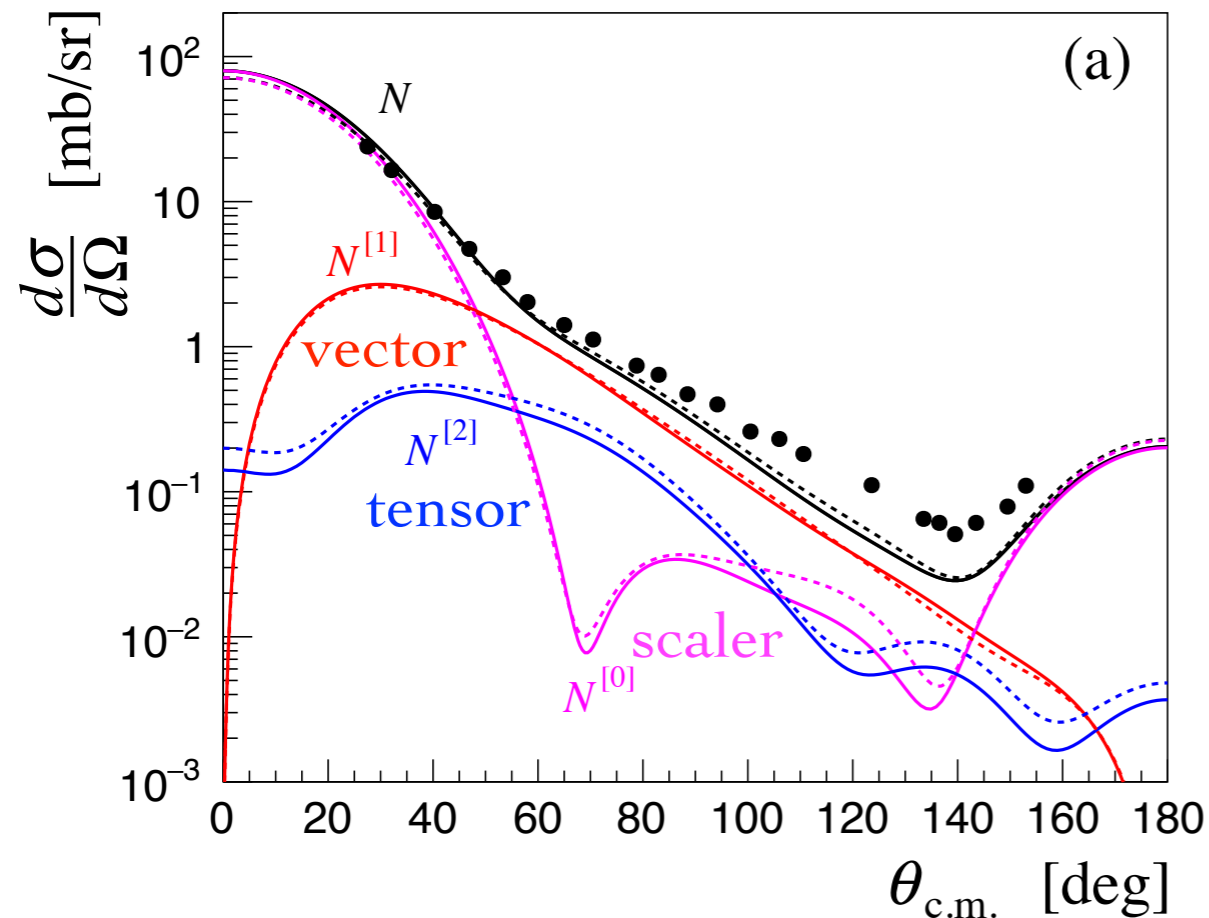


$p+^3\text{He}$ scattering at intermediate energies is an excellent tool to explore nuclear interactions not accessible by Nd scattering.

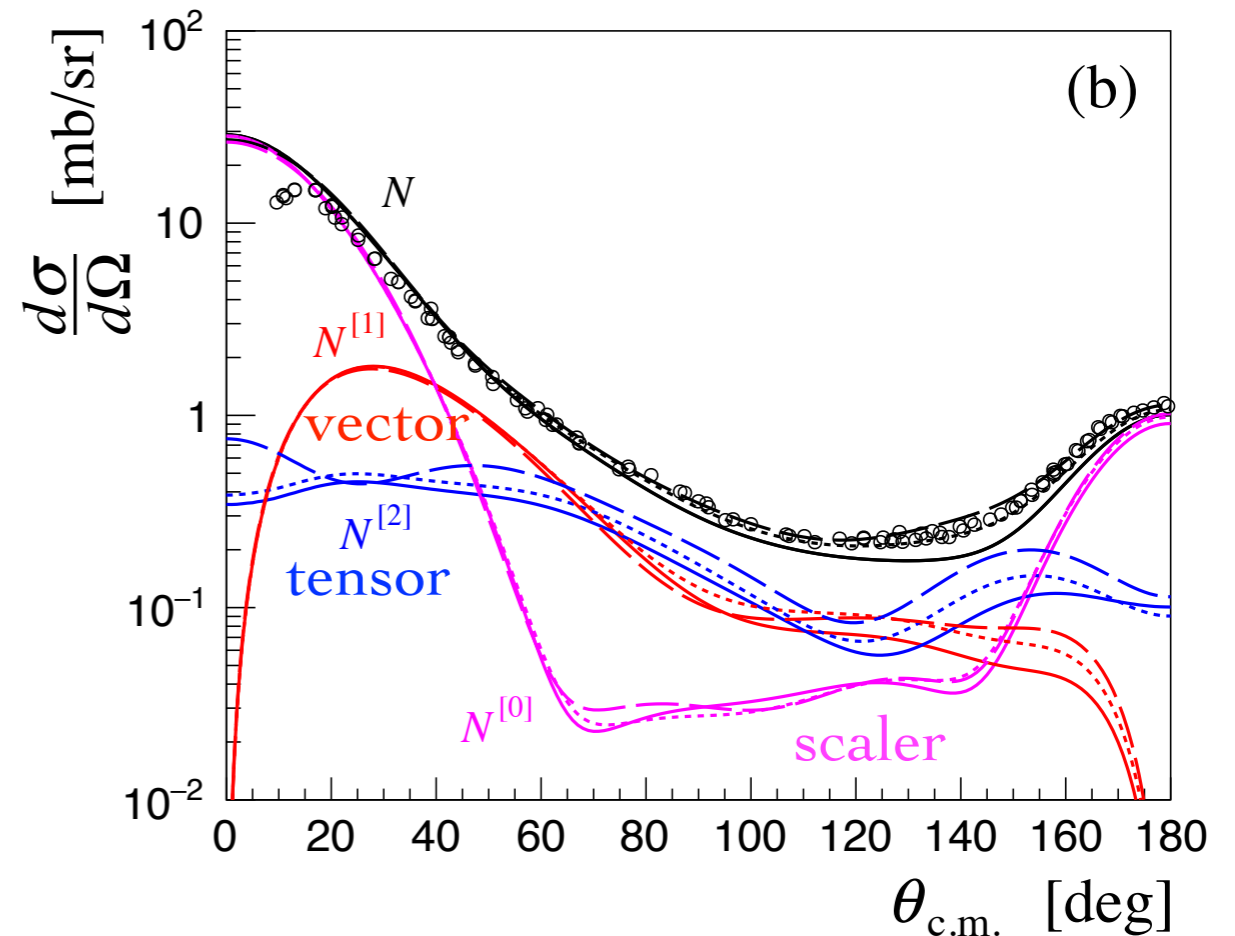
New Data of $p+{}^3\text{He}$ at Intermediate Energies

A. Watanabe et al., Phys. Rev. C 106, 054002 (2022)

$p-{}^3\text{He}$ at 100 MeV



$d-p$ at 135 MeV/N

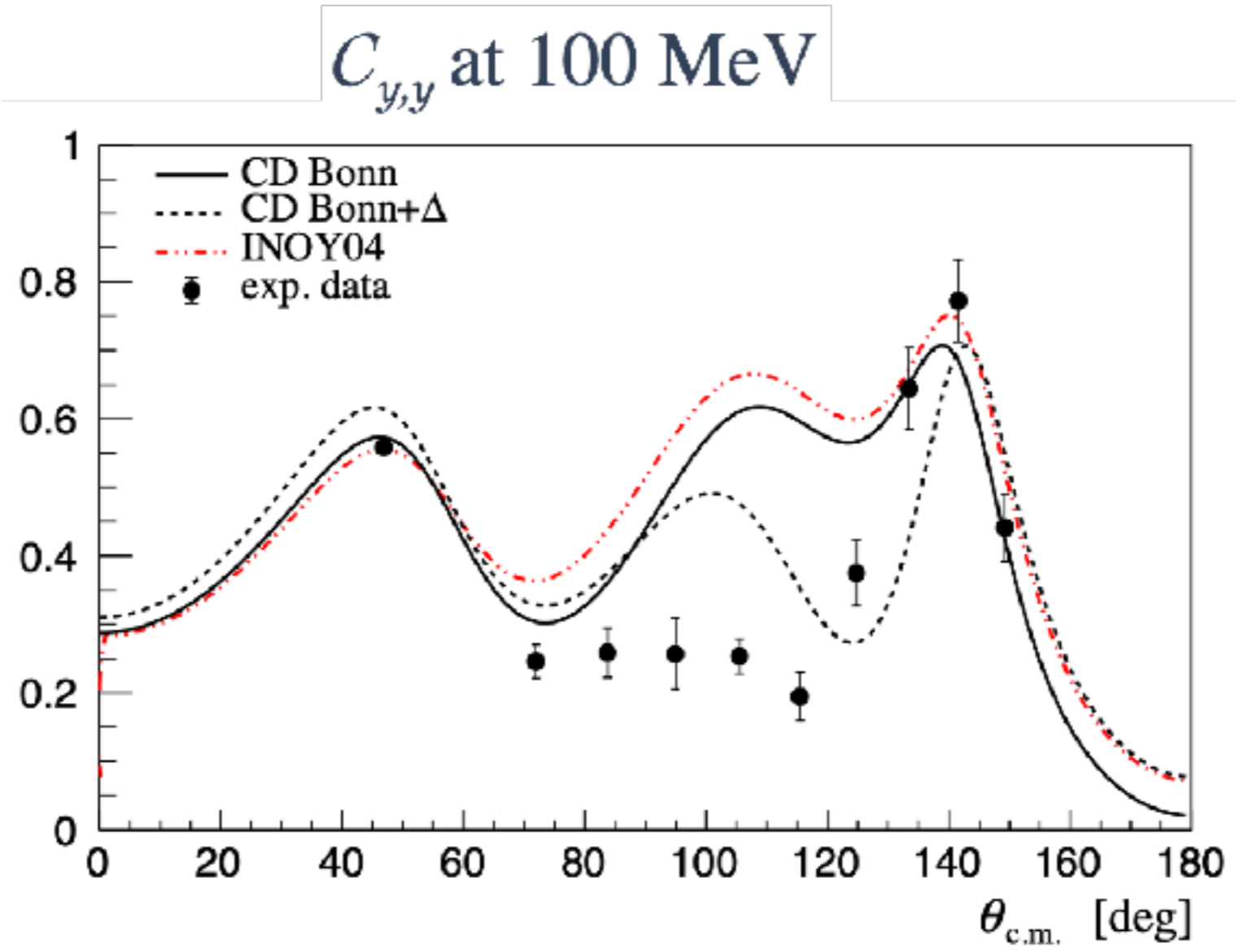


Analysis of Scattering Amplitudes :

Vector components are sensitive for $p-{}^3\text{He}$,
while **vector** and **tensor** components for $d-p$.

New Data of $p+^3\text{He}$ at Intermediate Energies

A.Watanabe et al., Phys. Rev. C 106, 054002 (2022)



Spin correlation coefficient $C_{y,y}$ is sensitive to Δ -isobar or those including 3NFs that are masked in nucleon-deuteron elastic scattering.

Summary (1/2)

Three-Nucleon Forces

are key elements to fully understand nuclear properties.
e.g. nuclear binding energies, EOS of nuclear matter

Few-Nucleon Scattering

is a good probe to investigate the dynamics of 3NFs.
- Momentum, Spin & Iso-spin dependence - .

Nucleon-Deuteron Scattering - 3N Scattering -

Precise data of $\partial\sigma/\partial\Omega$ and spin observables at 70- 300 MeV/nucleon from RIKEN/RCNP

Cross Sections : Large discrepancy at backward angles. **3NFs are clearly needed.**

Spin Observables : 3NF effects are spin dependent.

Serious discrepancy at backward angles at higher energies : short-range terms of 3NFs ?

New Project :

Measurement of spin correlation coefficients at 100 MeV/nucleon

- Determination of LECs N4LO 3NFs from ∂p scattering data is about to start.

Proton- ^3He Scattering - 4N Scattering -

- Approach to Iso-spin states of $T=3/2$ 3NF
- Rigorous numerical calculations : New possibilities for 3NF study in 4N Scatt.

New Data from CYRIC & RCNP : ^3He & p Analyzing powers, & Spin Correlation Coefficient

Cross section minimum region at higher energies : Source of rich information of 3NFs

Spin correlation coefficient : Very sensitive to dynamics of Nuclear forces

RIBF-*d*. Collaboration (2009~)

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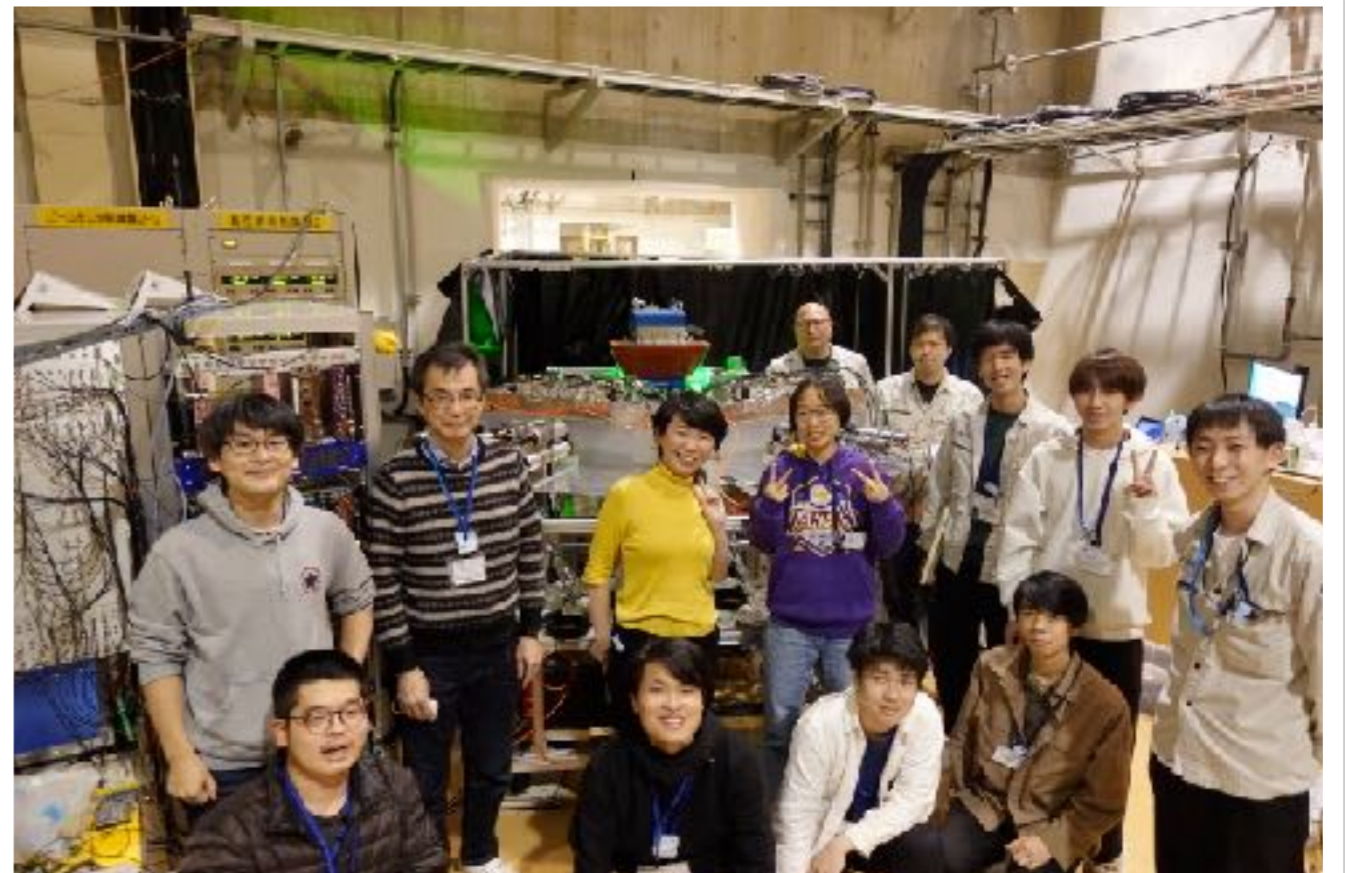
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