The BabaYaga event generator

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668 WE-Heraeus-Seminar Baryon Form Factors: Where do we stand?

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in collaboration with G. Montagna, O. Nicrosini, F. Piccinini

Outline

- * Motivations for precise luminometry
- * QED processes & radiative corrections
- * The BabaYaga and BabaYaga@NLO event generators
 - theoretical framework
 - improving theoretical accuracy: QED Parton Shower and matching with NLO corrections
- ⋆ Results, tuned comparisons, theoretical accuracy
- ★ Extension to (a few) hadronic final states
- ⋆ The MUonE project



⋆ Conclusions

http://www.pv.infn.it/hepcomplex/babayaga.html
(or better ask the authors!)

Baba¥aga core references:

- Barzè et al., Eur. Phys. J. C 71 (2011) 1680
- Balossini et al., Phys. Lett. 663 (2008) 209
- Balossini et al., Nucl. Phys. B758 (2006) 227
- C.M.C.C. et al., Nucl. Phys. Proc. Suppl. 131 (2004) 48
- C.M.C.C., Phys. Lett. B 520 (2001) 16
- C.M.C.C. et al., Nucl. Phys. B 584 (2000) 459
- ★ Related work:
 - S. Actis et al.

"Quest for precision in hadronic cross sections at low energy: Monte Carlo tools vs. experimental data", Eur. Phys. J. C **66** (2010) 585 Report of the Working Group on Radiative Corrections and Monte Carlo Generators for Low Energies

 C.M.C.C. et al., JHEP 1107 (2011) 126 NNLO massive pair corrections BabaYaga with dark photon BabaYaga@NLO for $e^+e^- \rightarrow \gamma\gamma$ BabaYaga@NLO for Bhabha BabaYaga@NLO improved PS BabaYaga BabaYaga

Why high precision generators for luminosity?

- Precision measurements require a precise knowledge of the machine luminosity
- *e.g.*, the measurement of the R(s) ratio is a key ingredient for the predictions of a_{μ}^{HLO} and $\Delta \alpha_{\text{had}}(M_Z)$ and in turn for SM precision tests



 Instead of getting the luminosity from machine parameters, it's more effective to exploit the relation

 $\sigma = \frac{N}{L} \quad \rightarrow \quad L = \frac{N_{\rm ref}}{\sigma_{\rm theory}} \qquad \frac{\delta L}{L} = \frac{\delta N_{\rm ref}}{N_{\rm ref}} \oplus \frac{\delta \sigma_{\rm theory}}{\sigma_{\rm theory}}$

- Reference (*normalization*) processes are required to have a clean topology, high statistics and be calculable with high theoretical accuracy
- ★ Large-angle QED processes as $e^+e^- \rightarrow e^+e^-$ (Bhabha), $e^+e^- \rightarrow \gamma\gamma$, $e^+e^- \rightarrow \mu^+\mu^-$ are golden processes at flavour factories to achieve a typical precision at the level of $1 \div 0.1\%$

→ QED radiative corrections are mandatory

→ BabaYaga has been developed for high-precision simulation of QED processes at flavour factories (primarily for luminosity determination)

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Theory of QED corrections into Monte Carlo generators

 The most precise MC generators include exact O(α) (NLO) photonic corrections matched with higher-order leading logarithmic contributions [multiple photon corrections]

[+ vacuum polarization, using a data driven routine for the calculation of the non-perturbative $\Delta \alpha_{had}^{(5)}(q^2)$ hadronic contribution]

- Common methods used to account for multiple photon corrections are the analytical collinear QED Structure Functions (SF), YFS exponentiation and QED Parton Shower (PS)
- The QED PS [implemented in Babayaga/Babayaga@NLO] is an exact MC solution of the QED DGLAP equation for the non-singlet electron SF $D(x, Q^2)$

$$Q^2 \frac{\partial}{\partial Q^2} D(x, Q^2) = \frac{\alpha}{2\pi} \int_x^1 \frac{dt}{t} P_+(t) D(\frac{x}{t}, Q^2)$$

The PS solution can be cast into the form

 $D(x,Q^2) = \Pi(Q^2) \sum_{n=0}^{\infty} \int \frac{\delta(x-x_1\cdots x_n)}{n!} \prod_{i=0}^{n} \left[\frac{\alpha}{2\pi} P(x_i) \ L \ dx_i \right]$

- → $\Pi(Q^2) \equiv e^{-\frac{\alpha}{2\pi}LI+}$ Sudakov form factor, $I_+ \equiv \int_0^{1-\epsilon} P(x)dx$, $L \equiv \ln Q^2/m^2$ collinear log, ϵ soft–hard separator and Q^2 virtuality scale
- → the kinematics of the photon emissions can be recovered → exclusive photons generation
- The accuracy is improved by matching exact NLO with higher-order leading log corrections
 - * theoretical error starts at $\mathcal{O}(\alpha^2)$ (NNLO) QED corrections, for all QED channels [Bhabha, $\gamma\gamma$ and $\mu^+\mu^-$]

The Structure Function (SF) approach

$$\sigma_{corrected} = \int dx_{-}dx_{+}dy_{-}dy_{+} \int d\Omega D^{ISR}(x_{-},Q^{2})D^{ISR}(x_{+},Q^{2})$$
$$\times D^{FSR}(y_{-},Q^{2})D^{FSR}(y_{+},Q^{2})\frac{d\sigma_{0}}{d\Omega}(x_{-}x_{+}s,\theta)\Theta(cuts)$$



\mapsto The QED PS algorithm numerically gives the $D^{ISR/FSR}(z,Q^2)$'s

* First step are QED $O(\alpha)$ (i.e. QED NLO, next-to-leading order) RCs

The NLO cross section is split into two contributions,

 $\sigma_{NLO} = \sigma_{2\to2} + \sigma_{2\to3} = \sigma_{e^+e^- \to e^+e^-} + \sigma_{e^+e^- \to e^+e^-\gamma}$

 \mapsto IR singularities are regularized with a vanishingly small photon mass λ

→ $[2 \rightarrow 2]/[2 \rightarrow 3]$ phase space splitting at an arbitrarily small γ-energy cutoff ω_s • $e^+e^- \rightarrow e^+e^-$

$$\sigma_{2\to 2} = \sigma_{LO} + \sigma_{NLO}^{virtual} = \int d\Phi_2 (|\mathcal{A}_{LO}|^2 + 2\Re[\mathcal{A}_{LO}^* \times \mathcal{A}_{NLO}^{virtual}(\boldsymbol{\lambda})])$$

• $e^+e^- \rightarrow e^+e^-\gamma$

$$\begin{split} \sigma_{2\to3} &= \int_{\omega>\lambda} d\Phi_3 |\mathcal{A}_{NLO}^{1\gamma}|^2 = \int_{\boldsymbol{\lambda}<\omega<\omega_s} d\Phi_3 |\mathcal{A}_{NLO}^{1\gamma}|^2 + \int_{\omega>\omega_s} d\Phi_3 |\mathcal{A}_{NLO}^{1\gamma}|^2 \\ &= \Delta_s(\boldsymbol{\lambda},\omega_s) \int d\Phi_2 |\mathcal{A}_{LO}| + \int_{\omega>\omega_s} d\Phi_3 |\mathcal{A}_{NLO}^{1\gamma}|^2 \end{split}$$

 the integration over the 2/3-particles phase space is done with MC techniques and fully-exclusive events are generated Exact $\mathcal{O}(\alpha)$ (NLO) soft+virtual (SV) corrections and hard-bremsstrahlung (H) matrix elements can be combined with QED PS via a matching procedure

•
$$d\sigma_{PS}^{\infty} = \Pi(Q^2, \varepsilon) \sum_{n=0}^{\infty} \frac{1}{n!} |\mathcal{M}_{n,PS}|^2 d\Phi_n$$

•
$$d\sigma_{PS}^{\alpha} = [1 + C_{\alpha, PS}] |\mathcal{M}_0|^2 d\Phi_2 + |\mathcal{M}_{1, PS}|^2 d\Phi_3 \equiv d\sigma_{PS}^{SV}(\varepsilon) + d\sigma_{PS}^{H}(\varepsilon)$$

•
$$d\sigma_{\mathrm{NLO}}^{\alpha} = [1 + C_{\alpha}] |\mathcal{M}_0|^2 d\Phi_2 + |\mathcal{M}_1|^2 d\Phi_3 \equiv d\sigma_{\mathrm{NLO}}^{SV}(\varepsilon) + d\sigma_{\mathrm{NLO}}^H(\varepsilon)$$

•
$$F_{SV} = 1 + (C_{\alpha} - C_{\alpha, PS})$$
 $F_H = 1 + \frac{|\mathcal{M}_1|^2 - |\mathcal{M}_{1, PS}|^2}{|\mathcal{M}_{1, PS}|^2}$

$$l\sigma_{\text{matched}}^{\infty} = F_{SV} \prod(Q^2, \varepsilon) \sum_{n=0}^{\infty} \frac{1}{n!} (\prod_{i=0}^{n} F_{H,i}) |\mathcal{M}_{n,PS}|^2 d\Phi_n$$

 $d\Phi_n$ is the exact phase space for *n* final-state particles (2 fermions + an arbitrary number of photons)

- F_{SV} and $F_{H,i}$ are infrared/collinear safe and account for missing $O(\alpha)$ non-logs, avoiding double counting of leading-logs
- $\left[\sigma_{matched}^{\infty}\right]_{\mathcal{O}(\alpha)} = \sigma_{\text{NLO}}^{\alpha}$
- resummation of higher orders LL (PS) contributions is preserved
- the cross section is still fully differential in the momenta of the final state particles $(e^+, e^- \text{ and } n\gamma)$

(F's correction factors are applied on an event-by-event basis)

• as a by-product, part of photonic $\alpha^2 L$ included by means of terms of the type $F_{SV \mid H,i} \otimes$ [leading-logs]

G. Montagna et al., PLB 385 (1996)

 the theoretical error is shifted to O(α²) (NNLO, 2 loop) not infrared, singly collinear terms: very naively and roughly (for photonic corrections)

$$\frac{1}{2}\alpha^2 L \equiv \frac{1}{2}\alpha^2 \log \frac{s}{m_e^2} \sim 5 \times 10^{-4}$$

Loosely and schematically, the corrections to the LO cross section can be arranged as (collinear log $L \equiv \log \frac{s}{m_e^2}$)

$$\begin{array}{c|c} \mathsf{LO} & \alpha^{0} \\ \mathsf{NLO} & \alpha L & \alpha \\ \mathsf{NNLO} & \frac{1}{2}\alpha^{2}L^{2} & \frac{1}{2}\alpha^{2}L & \frac{1}{2}\alpha^{2} \\ \mathsf{h.o.} & \sum_{n=3}^{\infty} \frac{\alpha^{n}}{n!}L^{n} & \sum_{n=3}^{\infty} \frac{\alpha^{n}}{n!}L^{n-1} & \cdots \end{array}$$

Blue: Leading-Log PS, Leading-Log YFS, SF

Loosely and schematically, the corrections to the LO cross section can be arranged as (collinear log $L \equiv \log \frac{s}{m_e^2}$)

$$\begin{array}{c|c|c} \mathsf{LO} & \alpha^0 \\ \mathsf{NLO} & \alpha L & \alpha \\ \mathsf{NNLO} & \frac{1}{2}\alpha^2 L^2 & \frac{1}{2}\alpha^2 L & \frac{1}{2}\alpha^2 \\ \mathsf{h.o.} & \sum_{n=3}^{\infty} \frac{\alpha^n}{n!} L^n & \sum_{n=3}^{\infty} \frac{\alpha^n}{n!} L^{n-1} & \cdots \end{array}$$

Red: matched PS, YFS, SF + NLO

Loosely and schematically, the corrections to the LO cross section can be arranged as (collinear log $L \equiv \log \frac{s}{m_e^2}$)



Tipically at flavour factories (on integrated Bhabha σ)

• to show the typical size of RC, the following setups and definitions are used (for Bhabha)

$$\delta_{VP} \equiv \frac{\sigma_{0,VP} - \sigma_{0}}{\sigma_{0}} \qquad \qquad \delta_{\alpha} \equiv \frac{\sigma_{\alpha}^{NLO} - \sigma_{0}}{\sigma_{0}}$$
$$\delta_{HO} \equiv \frac{\sigma_{matched}^{PS} - \sigma_{\alpha}^{NLO}}{\sigma_{0}} \qquad \qquad \delta_{HO}^{PS} \equiv \frac{\sigma_{\alpha}^{PS} - \sigma_{\alpha}^{PS}}{\sigma_{0}}$$
$$\delta_{\alpha}^{non-log} \equiv \frac{\sigma_{\alpha}^{NLO} - \sigma_{\alpha}^{PS}}{\sigma_{0}} \qquad \qquad \delta_{\infty}^{non-log} \equiv \frac{\sigma_{matched}^{PS} - \sigma_{\alpha}^{PS}}{\sigma_{0}}$$

setup	(a)	(b)	(C)	(d)
δ_{VP}	1.76	2.49	4.81	6.41
δ_{lpha}	-11.61	-14.72	-16.03	-19.57
δ_{HO}	0.39	0.82	0.73	1.44
δ_{HO}^{PS}	0.35	0.74	0.68	1.34
$\delta^{non-log}_{\alpha}$	-0.34	-0.56	-0.34	-0.56
$\delta_{\infty}^{non-log}$	-0.30	-0.49	-0.29	-0.46

Table: Relative corrections (in per cent) to the Bhabha cross section for the four setups

- * in short, the fact that $\delta_{\alpha}^{non-log} \simeq \delta_{\infty}^{non-log}$ and $\delta_{HO} \simeq \delta_{HO}^{PS}$ means that the matching algorithm preserves both the advantages of exact NLO calculation and PS approach:
 - $\mapsto\,$ it includes the missing NLO RC to the PS
 - → it adds the missing higher-order RC to the NLO





OLD \rightarrow pure PS

 $\mathbf{NEW} \rightarrow \mathbf{matched PS}$ with NLO

 $\mathcal{O}(\alpha) \rightarrow \text{exact NLO}$

Luminosity/QED generators

Luminosity measured with $0.1 \div 1\%$ precision using large-angle Bhabha (and $e^+e^- \rightarrow \gamma\gamma$) as reference process, simulated with two independent generators

$$\mathcal{L} = \frac{N_{\rm obs}}{\sigma_{\rm theory}}$$

Generator	Processes	Theory	Accuracy
BabaYaga 3.5	$e^+e^-, \gamma\gamma, \mu^+\mu^-$	QED Parton Shower	$\sim 0.5\%$
BabaYaga@NLO	$e^+e^-, \gamma\gamma, \mu^+\mu^-$	$\mathcal{O}(\alpha) + QED PS$	$\sim 0.1\%$
BHWIDE	e^+e^-	$\mathcal{O}(\alpha)$ YFS	$\sim 0.1\%$
MCGPJ	$e^+e^-, \gamma\gamma, \mu^+\mu^-$	$\mathcal{O}(\alpha) + coll. \ SF$	$\sim 0.2\%$
KKMC	$\mu^+\mu^-, \tau^+\tau^-, \ldots$	$\mathcal{O}(\alpha) CEEX$	$\sim 0.1\%$

- BabaYaga 3.5/BabaYaga@NLO http://www2.pv.infn.it/~hepcomplex/babayaga.html Used by BaBar, Belle, BESIII, CLEO, KEDR and KLOE, Carloni Calame et al., 2000 / 2006, 2008
- BHWIDE http://placzek.web.cern.ch/placzek/bhwide/ Used by BaBar, BESIII, KEDR, KLOE and SND. Jadach, Placzek and Ward, 1997
- MCGPJ

Used by CMD, Belle and SND.

http://cmd.inp.nsk.su/~sibid/

Arbuzov et al., 2005 / Eidelman et al., 2011

□ KKMC http://jadach.web.cern.ch/jadach/KKindex.html Used by BaBar, Belle and BESIII (τ physics, ISR and NP studies). Jadach et al., 2000

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G. Montagna, Pavia University & INFN RCs & MCs at flavor factories September 2015 9/19 C.M. Carloni Calame (INFN, Pavia) WE-Heraeus-Seminar 15/27BabaYaga

Estimating the theoretical accuracy

S. Actis et al. Eur. Phys. J. C 66 (2010) 585

"Quest for precision in hadronic cross sections at low energy: Monte Carlo tools vs. experimental data"

- It is extremely important to compare independent calculations/implementations/codes, in order to
 - → asses the technical precision, spot bugs (with the same th. ingredients)
 - \mapsto estimate the theoretical error when including partial/incomplete higher-order corrections
- E.g. comparison BabaYaga@NLO vs. Bhwide at KLOE



Without vacuum polarization, to compare QED corrections consistently

At the Φ and τ -charm factories (cross sections in nb)

By BabaYaga group, Ping Wang and A. Sibidanov

setup	BabaYaga@NLO	BHWIDE	MCGPJ	$\delta(\%)$
$\sqrt{s} = 1.02 \text{ GeV}, 20^{\circ} \le \vartheta_{\mp} \le 160^{\circ}$	6086.6(1)	6086.3(2)	_	0.005
$\sqrt{s} = 1.02 \text{ GeV}, 55^{\circ} \le \vartheta_{\mp} \le 125^{\circ}$	455.85(1)	455.73(1)	_	0.030
$\sqrt{s} = 3.5 \text{ GeV}, \vartheta_+ + \vartheta \pi \le 0.25 \text{ rad}$	35.20(2)	—	35.181(5)	0.050

→ Agreement well below 0.1%

At BaBar (cross sections in nb)

By A. Hafner and A. Denig

angular acceptance cuts	BabaYaga@NLO	BHWIDE	$\delta(\%)$
$15^{\circ} \div 165^{\circ}$	119.5(1)	119.53(8)	0.025
$40^{\circ} \div 140^{\circ}$	11.67(3)	11.660(8)	0.086
$50^{\circ} \div 130^{\circ}$	6.31(3)	6.289(4)	0.332
$60^{\circ} \div 120^{\circ}$	3.554(6)	3.549(3)	0.141

 $\mapsto~$ Agreement at the $\sim 0.1\%$ level

Theoretical accuracy, comparisons with NNLO

- NLO RC being included, the theoretical error starts at $\mathcal{O}(\alpha^2)$ (NNLO)
 - \hookrightarrow anyway large NNLO RC already included by exponentiation (and by $\mathcal{O}(\alpha)$ PS \times non-log-NLO)
- The full set of NNLO QED corrections to Bhabha scattering has been calculated in the last years
- BabaYaga@NLO formulae can be truncated at $\mathcal{O}(\alpha^2)$ to be consistently and systematically compared with all the classes of NNLO corrections

$$\sigma^{\alpha^2} = \sigma^{\alpha^2}_{\rm SV} + \sigma^{\alpha^2}_{\rm SV,H} + \sigma^{\alpha^2}_{\rm HH}$$

- $\sigma_{SV}^{\alpha^2}$: soft+virtual photonic corrections up to $\mathcal{O}(\alpha^2)$ \mapsto compared with the corresponding available NNLO QED calculation
- $\sigma_{SV,H}^{\alpha^2}$: one–loop soft+virtual corrections to single hard bremsstrahlung \mapsto presently estimated relying on existing (partial) results
- $\sigma_{\rm HH}^{\alpha^2}$: double hard bremsstrahlung
 - \rightarrow compared with the exact $e^+e^- \rightarrow e^+e^-\gamma\gamma$ cross section, to register really negligible differences (at the 1×10^{-5} level)

NNLO Bhabha calculations

Photonic corrections A. Penin, PRL 95 (2005) 010408 & Nucl. Phys. B734 (2006) 185



here real γ is "soft"

Electron loop corrections

R. Bonciani *et al.*, Nucl. Phys. **B701** (2004) 121 & Nucl. Phys. **B716** (2005) 280
 S. Actis, M. Czakon, J. Gluza and T. Riemann, Nucl. Phys. **B786** (2007) 26



Heavy fermion and hadronic loops

R. Bonciani, A. Ferroglia and A. Penin, PRL 100 (2008) 131601

S. Actis, M. Czakon, J. Gluza and T. Riemann, PRL 100 (2008) 131602

J.H. Kühn and S. Uccirati, Nucl. Phys. B806 (2009) 300





here real γ is "soft"

One-loop soft+virtual corrections to single hard bremsstrahlung

S. Actis, P. Mastrolia and G. Ossola, Phys. Lett. B682 (2010) 419



here real γ is "hard"

Using realistic cuts for luminosity at KLOE

Comparison of $\sigma_{\rm SV}^{\alpha^2}$ calculation of BabaYaga@NLO with

Penin (photonic): function of the logarithm of the soft photon cut-off (left plot) and a fictitious electron
mass (right plot)



- * differences are infrared safe, as expected
- $\star \ \delta\sigma(\text{photonic})/\sigma_0 \propto \alpha^2 L$, as expected
- Numerically, for various selection criteria at the Φ and B factories

 $\sigma_{\rm SV}^{\alpha^2}({\rm Penin}) - \sigma_{\rm SV}^{\alpha^2}(\texttt{BabaYaga@NLO}) \, < \, \textbf{0.02\%} \times \sigma_0$

Leptonic and hadronic loops & pairs at NNLO

- The exact NNLO soft+virtual corrections and $2 \rightarrow 4$ matrix elements $e^+e^- \rightarrow e^+e^-(l^+l^-)$ $_{[l=e, \mu, \tau]}, e^+e^- \rightarrow e^+e^-(\pi^+\pi^-)$ are available
- Compared to the *approximation* in BabaYaga@NLO, using realistic luminosity cuts $(S_i \equiv \sigma_i^{\text{NLO}}/\sigma_{BY})$

	\sqrt{s}		$\sigma_{ m BY}$	$S_{e^+e^-}$ [%]	S_{lep} [‰]	S_{had} [‰]	S_{tot} [‰]
KLOE	1.020	NNLO		-3.935(4)	-4.472(4)	1.02(2)	-3.45(2)
		BB@NLO	455.71	-3.445(2)	-4.001(2)	0.876(5)	-3.126(5)
BES	3.650	NNLO		-1.469(9)	-1.913(9)	-1.3(1)	-3.2(1)
		BB@NLO	116.41	-1.521(4)	-1.971(4)	-1.071(4)	-3.042(5)
BaBar	10.56	NNLO		-1.48(2)	-2.17(2)	-1.69(8)	-3.86(8)
		BB@NLO	5.195	-1.40(1)	-2.09(1)	-1.49(1)	-3.58(2)
Belle	10.58	NNLO		-4.93(2)	-6.84(2)	-4.1(1)	-10.9(1)
		BB@NLO	5.501	-4.42(1)	-6.38(1)	-3.86(1)	-10.24(2)

 $\star\,$ The uncertainty due to leptonic and hadronic pair NNLO corrections is at the level of a few units in 10^{-4}

Carloni, Czyz, Gluza, Gunia, Montagna, Nicrosini, Piccinini, Riemann et al., JHEP 1107 (2011) 126

main conclusion of the Luminosity Section of Eur. Phys. J. C 66 (2010) 585

• Putting the sources of uncertainties (in large-angle Bhabha) all together:

Source of error (%)	$\Phi-factories$	\sqrt{s} = 3.5 GeV	<i>B</i> -factories
$ \delta_{\rm VP}^{\rm err} $ [Jegerlehner]	0.00	0.01	0.03
$ \delta_{\mathrm{VP}}^{\mathrm{err}} $ [HMNT]	0.02	0.01	0.02
$\delta_{\mathrm{SV},\alpha^2}^{\mathrm{err}}$	0.02	0.02	0.02
$ \delta_{\mathrm{HH},\alpha^2}^{\mathrm{err}} $	0.00	0.00	0.00
$\delta_{\rm SV,H,\alpha^2}^{\rm err}$	0.05	0.05	0.05
$ \delta_{ m pairs}^{ m err} $	0.03	0.016	0.03
$ \delta_{ ext{total}}^{ ext{err}} $ linearly	0.12	0.1	0.13
$ \delta_{\text{total}}^{\text{err}} $ in quadrature	0.07	0.06	0.06

- The present error estimate appears to be rather robust and sufficient for high-precision luminosity measurements. It is comparable with that achieved for small-angle Bhabha luminosity monitoring at LEP/SLC
- For the experiments on top of and closely around the narrow resonances $(J/\psi, \Upsilon, \ldots)$, the accuracy quickly deteriorates, because of the differences between the predictions of independent $\Delta \alpha_{had}^{(5)}(q^2)$ parameterizations and/or their intrinsic error

BabaYaga for hadronic final states

- As side projects, a few hadronic final states have been added to [pure PS]
 BabaYaga, to simulate only initial-state-radiation (ISR)
- Correct to the extent ISR can be factorized over a "kernel" cross section
- Developed mainly upon request from BESIII people:
 - R. Baldini, M. Maggiora, F. De Mori, M. De Stefanis, G. Mezzadri, P. Wang

$$e^{+}e^{-} \rightarrow \pi^{+}\pi^{-}$$

$$\rightarrow p\bar{p}$$

$$\rightarrow K^{+}K^{-}$$

$$\rightarrow \Lambda\bar{\Lambda} \rightarrow p\pi^{-}\bar{p}\pi^{+} \quad [+n \text{ ISR } \gamma]$$

in $\Lambda\bar{\Lambda}$ channel decay spin correlations are kept \hookrightarrow based on H. Czyż *et al.*, PRD **75** 074026 (2007)

 The accuracy is limited but *fair* for data analysis with a precision in the % range (my personal guess).
 The *physics* must sit in the "kernel"/"hard scattering" cross section.

CMCC *et al.*, PLB **746** (2015) 325 G. Abbiendi *et al.*, EPJC **77** (2017) no.3, 139

New space-like proposal for HLO

 At present, the leading hadronic contribution a_µ^{HLO} is computed via the time-like formula:



$$a_{\mu}^{\rm HLO} = \frac{1}{4\pi^3} \int_{4m_{\pi}^2}^{\infty} ds \, K(s) \, \sigma_{\rm had}^0(s)$$

$$K(s) = \int_0^1 dx \, \frac{x^2 \, (1-x)}{x^2 + (1-x) \left(s/m_\mu^2\right)}$$

• Alternatively, exchanging the x and s integrations in $a_{\mu}{}^{HLO}$



$$a_{\mu}^{\text{HLO}} = \frac{\alpha}{\pi} \int_{0}^{1} dx \left(1 - x\right) \Delta \alpha_{\text{had}}[t(x)]$$
$$t(x) = \frac{x^{2} m_{\mu}^{2}}{x - 1} < 0$$

 $\Delta \alpha_{had}(t)$ is the hadronic contribution to the running of α in the space-like region. It can be extracted from scattering data!

M. Passera MITP Feb 19 2018

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WE-Heraeus-Seminar 25/27

CMCC *et al.*, PLB **746** (2015) 325 G. Abbiendi *et al.*, EPJC **77** (2017) no.3, 139

New space-like proposal for HLO (2)



F. Jegerlehner, arXiv:1511.04473

C.M. Ca

Carloni Calame, MP, Trentadue, Venanzoni, PLB 2015

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CMCC *et al.*, PLB **746** (2015) 325 G. Abbiendi *et al.*, EPJC **77** (2017) no.3, 139



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BabaYaga

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CMCC *et al.*, PLB **746** (2015) 325 G. Abbiendi *et al.*, EPJC **77** (2017) no.3, 139

- The MUonE experiment is being proposed at CERN, scattering a 150 GeV μ[±] beam off e⁻ on a Be (or C) target
 - \star high-intensity beam, can access the right kinematical regime ($\sqrt{s} \simeq 0.4 \text{ GeV}$)
- In order to extract Δα_{had}(t) from data, RCs to the process μe → μe must be known with extremely high-accuracy (better than 10⁻⁴)
 - \mapsto NLO QED corrections calculated and available into a MC generator (with full μ & *e* mass dependency)
 - → Full QED NNLO needed

Pavia group, paper in preparation

P. Mastrolia et al., JHEP 1711 (2017) 198

- → Matching of NNLO with QED higher-orders (e.g. QED PS) needed
- → Firmly assess the residual theoretical error
- ★ RCs by far dominated by corrections on electron current. Possible cross-check/comparison (same "inverse kinematics" setup) with calculations of QED NLO RCs to $pe \rightarrow pe$ scattering?

G.I. Gakh et al., Phys. Rev. C 95 (2017) no.5, 055207

G.I. Gakh et al., arXiv:1804.01399 [hep-ph]

- ★ In the last 15(+) years BabaYaga/BabaYaga@NLO has been developed for high-precision luminometry at flavour factories
- ⋆ It simulates QED processes

 $\begin{array}{l} \hookrightarrow e^+e^- \to e^+e^- \ (+n\gamma) \\ \hookrightarrow e^+e^- \to \mu^+\mu^- \ (+n\gamma) \\ \hookrightarrow e^+e^- \to \gamma\gamma \ (+n\gamma) \end{array}$

with multiple-photon emission in a QED Parton Shower framework, matched with exact NLO matrix elements

- * A theoretical precision at the 0.5×10^{-3} level is achieved (at least for Bhabha), with a systematic comparison to independent calculations/codes and assessing the size of missing higher-order corrections
- Improving the accuracy of QED processes would imply the inclusion of exact full 2-loop corrections, which is (at least in principle) feasible although not trivial
- A bunch of hadronic final states have been added to simulate ISR in the pure PS approach, within its intrinsic accuracy limitations