
Fermilab Measurement of Muon $g-2$

Dave Kawall, University of Massachusetts Amherst, on behalf of the Muon $g-2$ Collaboration

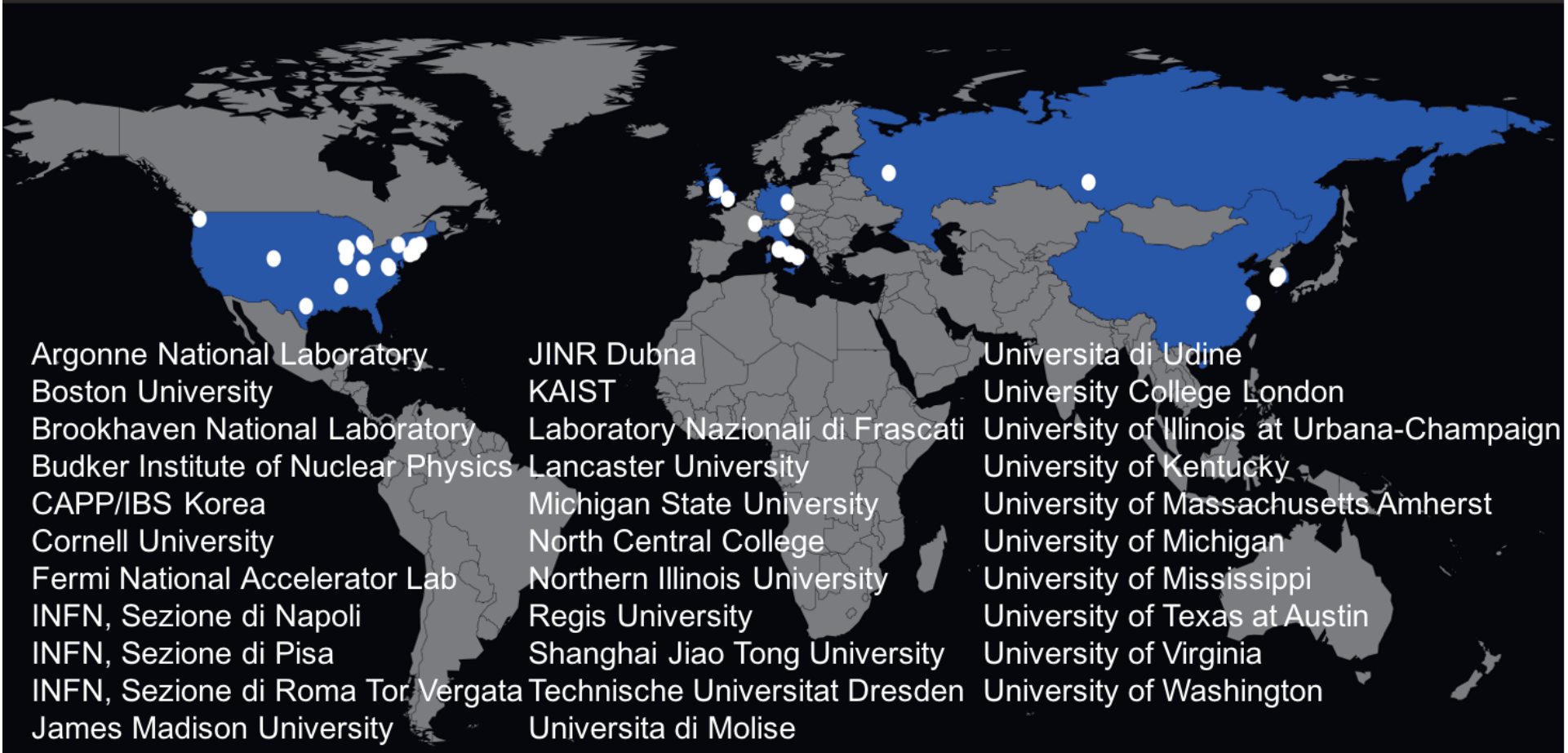


Goal: Measure the muon anomalous magnetic moment a_μ to 140 ppb, a fourfold improvement over the 540 ppb precision of Brookhaven

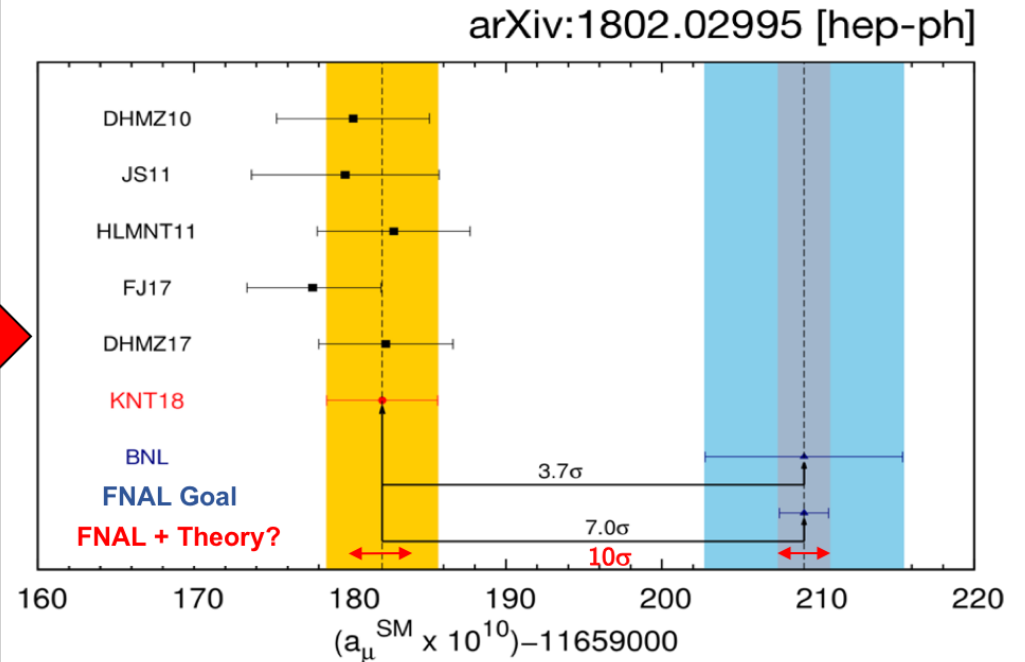
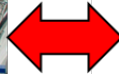
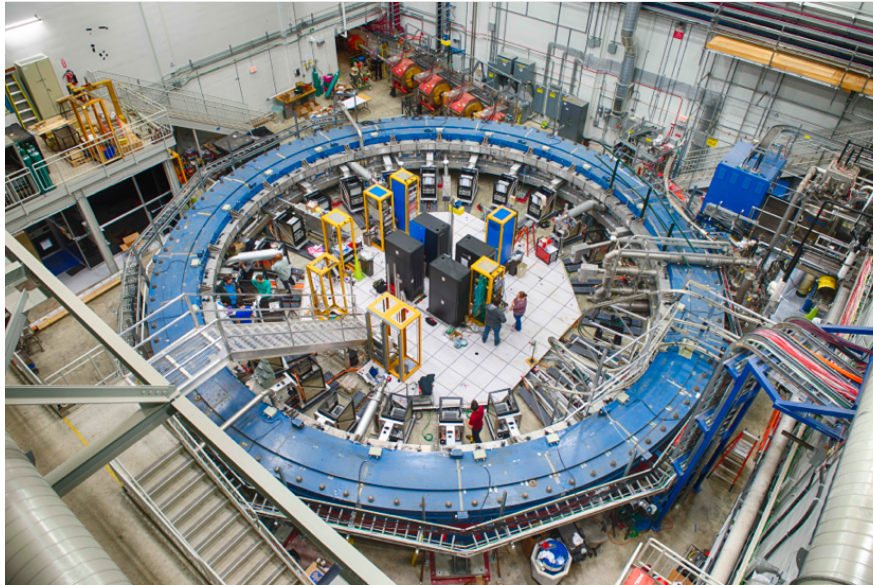


Muon $g-2$ Collaboration

7 Countries, 34 Institutions, 185 Collaborators

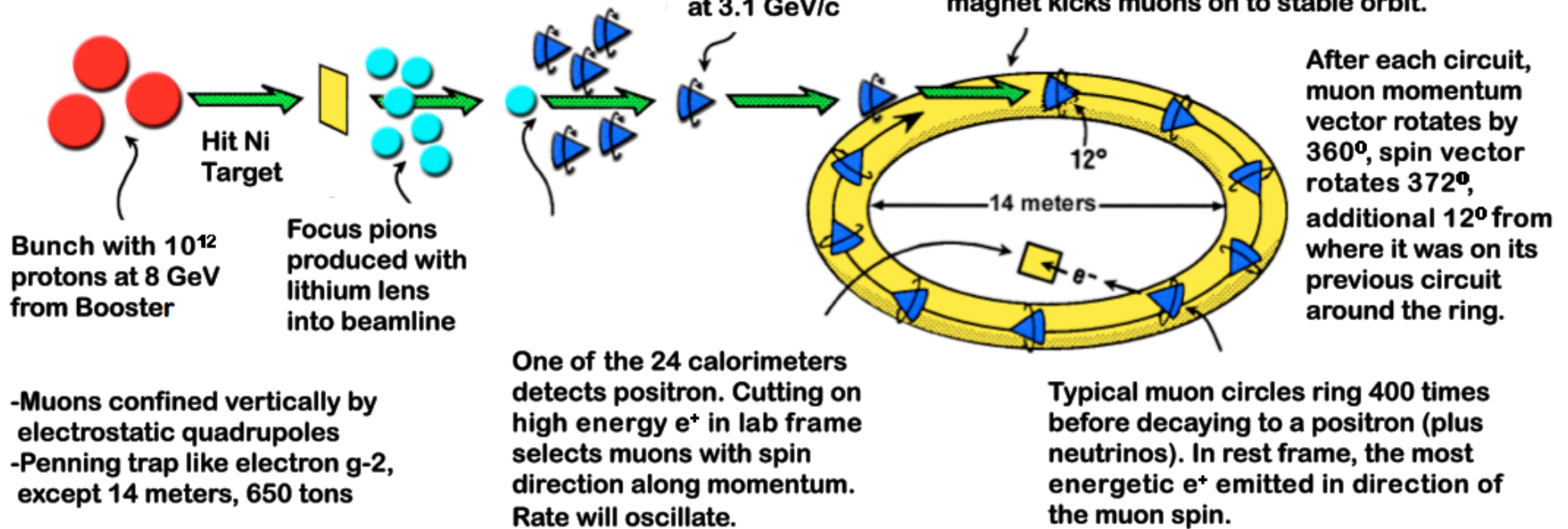


Thanks to Everyone for your Effort!



- All here to improve SM Prediction and Measurement of a_μ
- Wouldn't be here except for rare combination of circumstances:
 - (1) We can measure a_μ really well
 - (2) You can predict a_μ really well
 - (3) The comparison can change future direction of physics
- 3.5σ discrepancy on a_μ large compared to EW contribution: 27×10^{-10} vs 15.36×10^{-10}
- Great challenge for physics! Thanks for your efforts!

Overview of the g-2 experiment



- 14 meter radius, 650 tons Penning trap for 3.1 GeV muons
- Radial confinement: 1.45 T B field; vertical confinement: electric quadrupoles
- Superconducting inflector to inject muons in ring
- Pulsed magnetic kickers put muons on stored orbit

Overview of the *Idealized* Measurement Technique

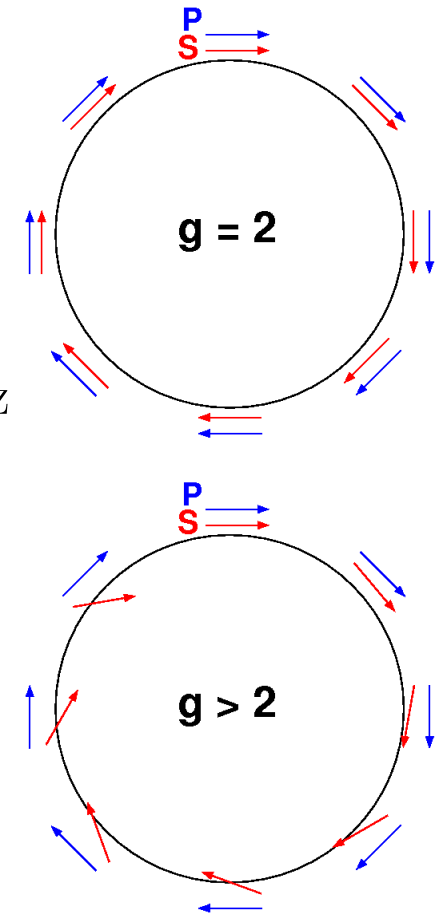
- Inject polarized muons into magnetic storage ring 1.45 T

$$\vec{\omega}_{\text{cyclotron}} = \frac{e}{\gamma m} \vec{B} \approx 2\pi \times 6.7 \text{ MHz}$$

$$\vec{\omega}_{\text{spin}} = g \frac{e}{2m} \vec{B} - (1 - \gamma) \frac{e}{\gamma m} \vec{B} \approx 2\pi \times 6.9 \text{ MHz}$$

$$\vec{\omega}_a \equiv \vec{\omega}_s - \vec{\omega}_c = \left(\frac{g - 2}{2} \right) \left[\frac{e}{m} \vec{B} \right]$$

$$\Rightarrow \vec{\omega}_a = a_\mu \left[\frac{e}{m} \vec{B} \right] \approx 229 \text{ kHz}$$



- Difference between spin and cyclotron frequencies: ω_a proportional to a_μ
- Difference sensitive to $a_\mu \approx 0.00116\dots$, not $g_\mu \approx 2.00232\dots$

\Rightarrow Experiment measures two quantities:

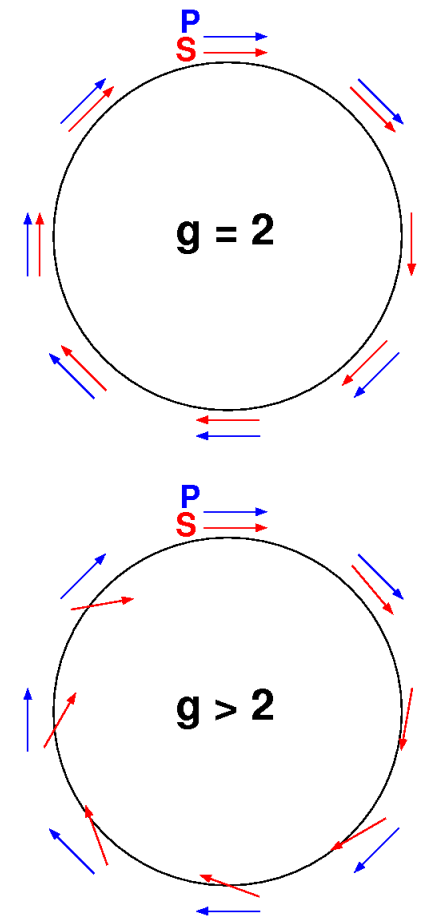
- (1) Muon anomalous precession frequency ω_a to ± 100 ppb (stat) ± 70 ppb (syst)
- (2) Magnetic field \vec{B} in terms of proton NMR frequency ω_p to ± 70 ppb (syst)

- Inject polarized muons into magnetic storage ring with electric vertical focusing
- Muon cyclotron frequency $\omega_c \approx 2\pi \times 6.7$ MHz
- Muon spin vector precession $\omega_s \approx 2\pi \times 6.9$ MHz

$$\vec{\omega}_a = \vec{\omega}_S - \vec{\omega}_C$$

$$\vec{\omega}_a \approx \frac{e}{mc} \left[a_\mu \vec{B} - \left(a_\mu - \left[\frac{mc}{p} \right]^2 \right) \vec{\beta} \times \vec{E} \right]$$

$$\vec{\omega}_a \approx 229 \text{ kHz}$$



⇒ Cancel term from electrostatic vertical focusing at $p_{\text{magic}} = \frac{mc}{\sqrt{a_\mu}} \approx 3.094 \text{ GeV}/c$

⇒ Experiment measures two quantities:

- (1) Muon anomalous precession frequency ω_a to ± 100 ppb (stat) ± 70 ppb (syst)
- (2) Magnetic field \vec{B} in terms of proton NMR frequency ω_p to ± 70 ppb (syst)

Why Fermilab? Statistics!

⇒ Brookhaven statistics limited:

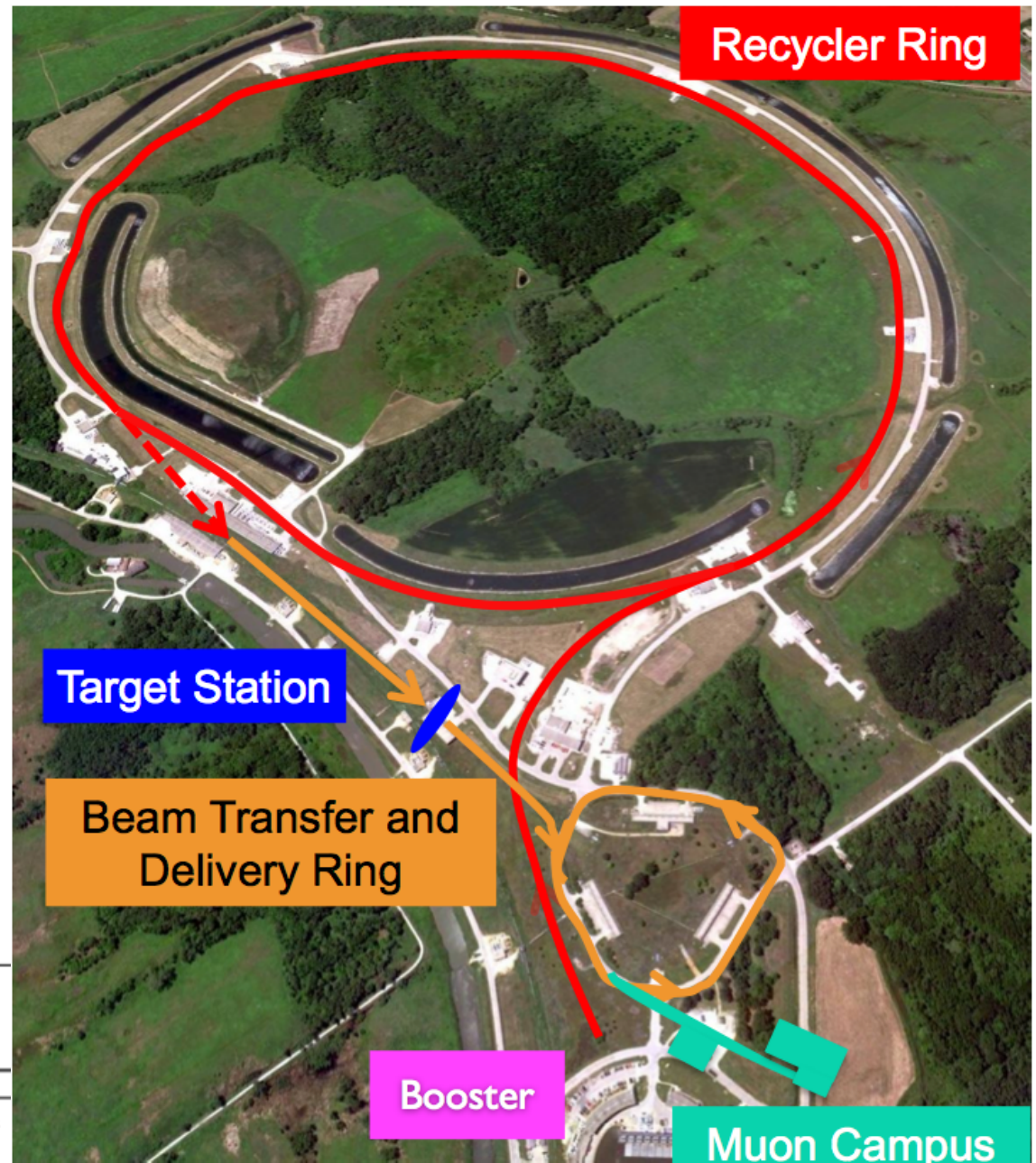
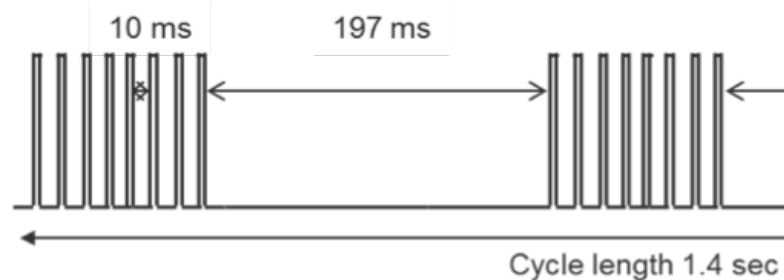
$$a_{\mu}^{\text{BNL}} = 0.001\,165\,920\,89\,(54)_{\text{stat}}\,(33)_{\text{sys}}$$

- BNL ± 540 ppb uncertainty on a_{μ} ,
 9×10^9 events

⇒ Fermilab goal 2×10^{11} , factor 21

Fermilab Advantages:

- Long decay channel for $\pi \Rightarrow \mu$
 - Reduced π and p in ring
 - Factor 20 reduction in hadronic flash
- ⇒ $4 \times$ higher fill frequency than BNL
- Muons per fill about the same
- ⇒ 21 times more detected e^+ , 2×10^{11}



From Brookhaven to Fermilab

- 650 ton magnet disassembled, put on trucks to Fermilab, coils went by barge down Atlantic coast, up Mississippi in 2013

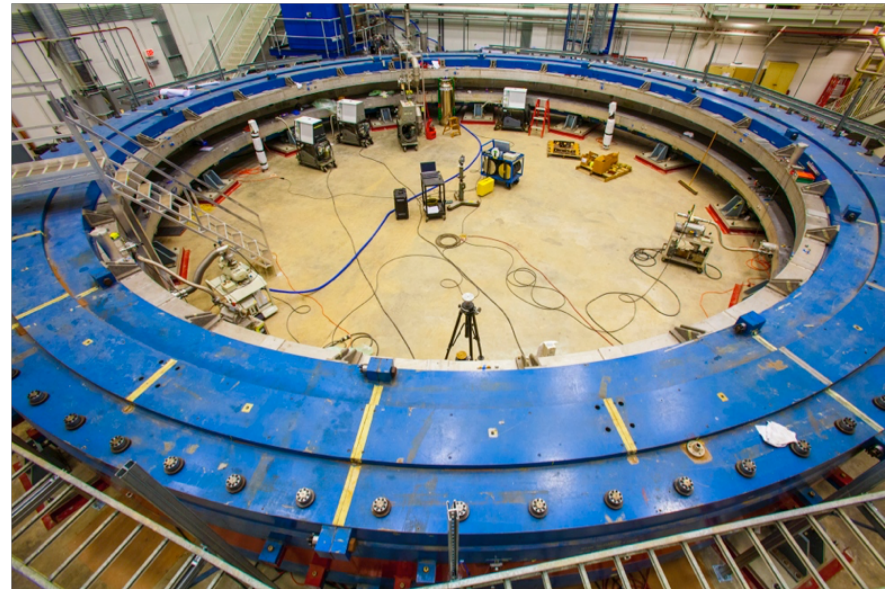
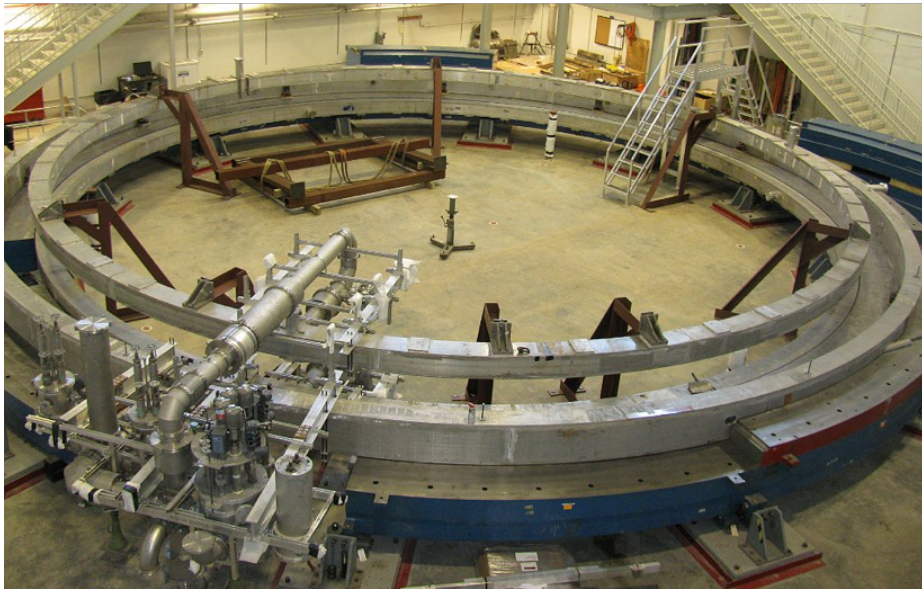


From Brookhaven to Fermilab

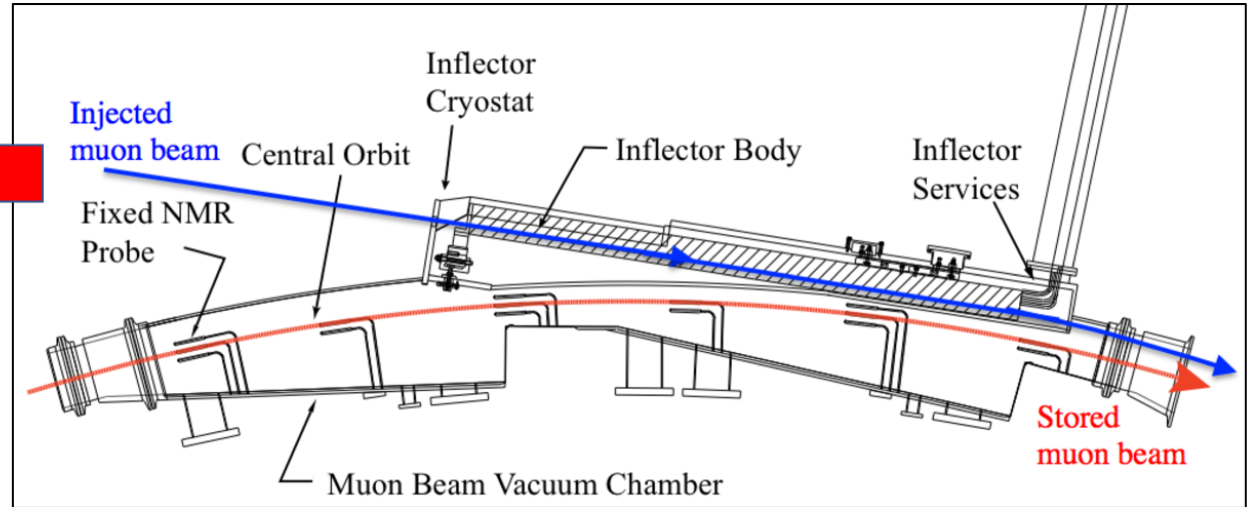
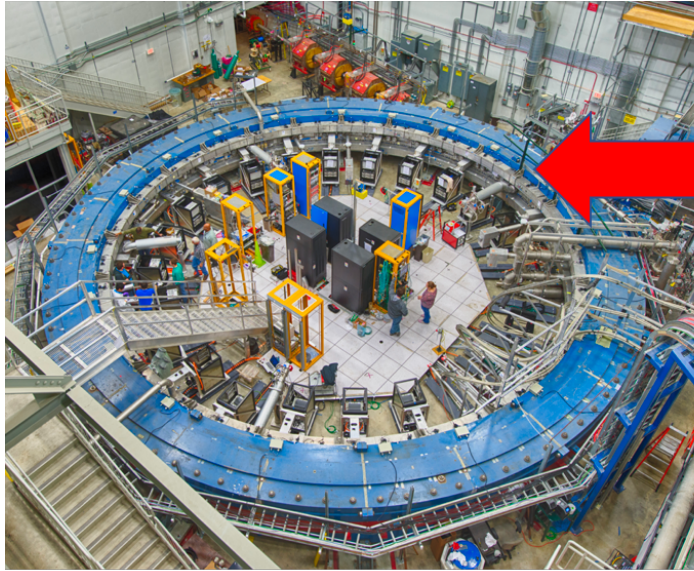


- Closed two interstates near Chicago to transport coils to Fermilab
- Coils pass toll arches with 6" clearance on each side

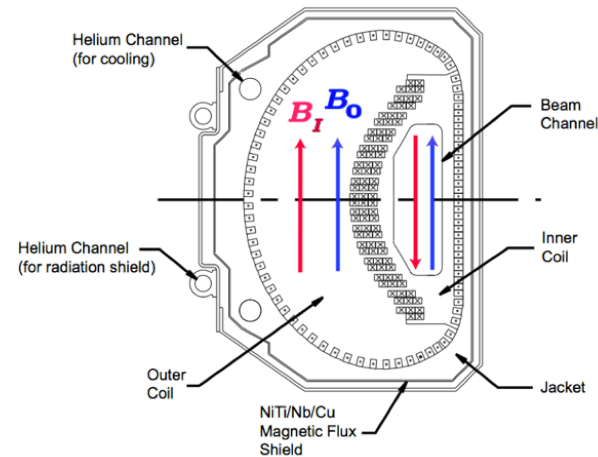
Magnet Reassembly at Fermilab June 2014 - June 2015



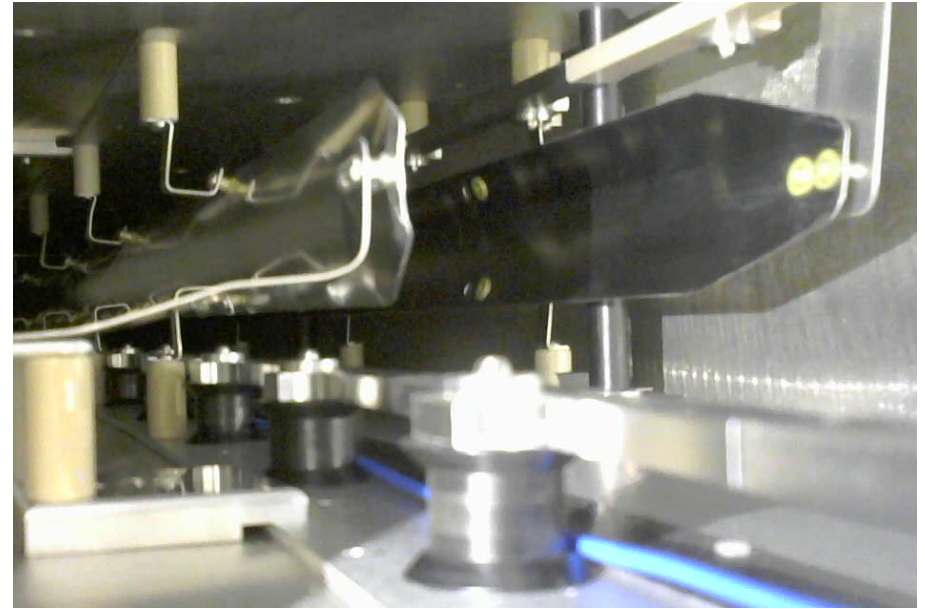
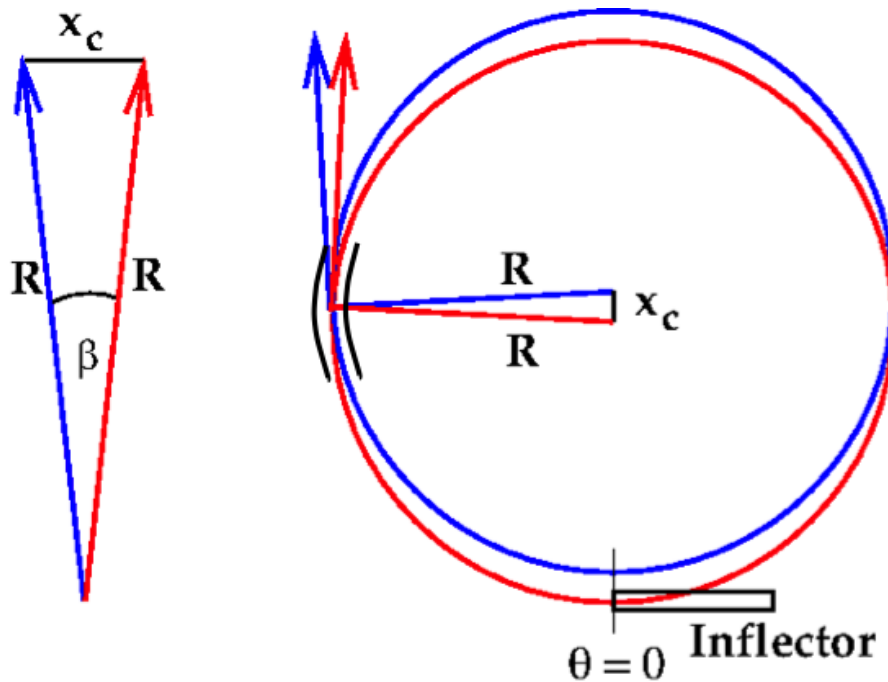
How do we get muons into the ring? Superconducting Inflector



- Cancel 1.45 T field inside channel
- Prevents strong deflection of beam
- Minimal perturbation of field in muon storage volume



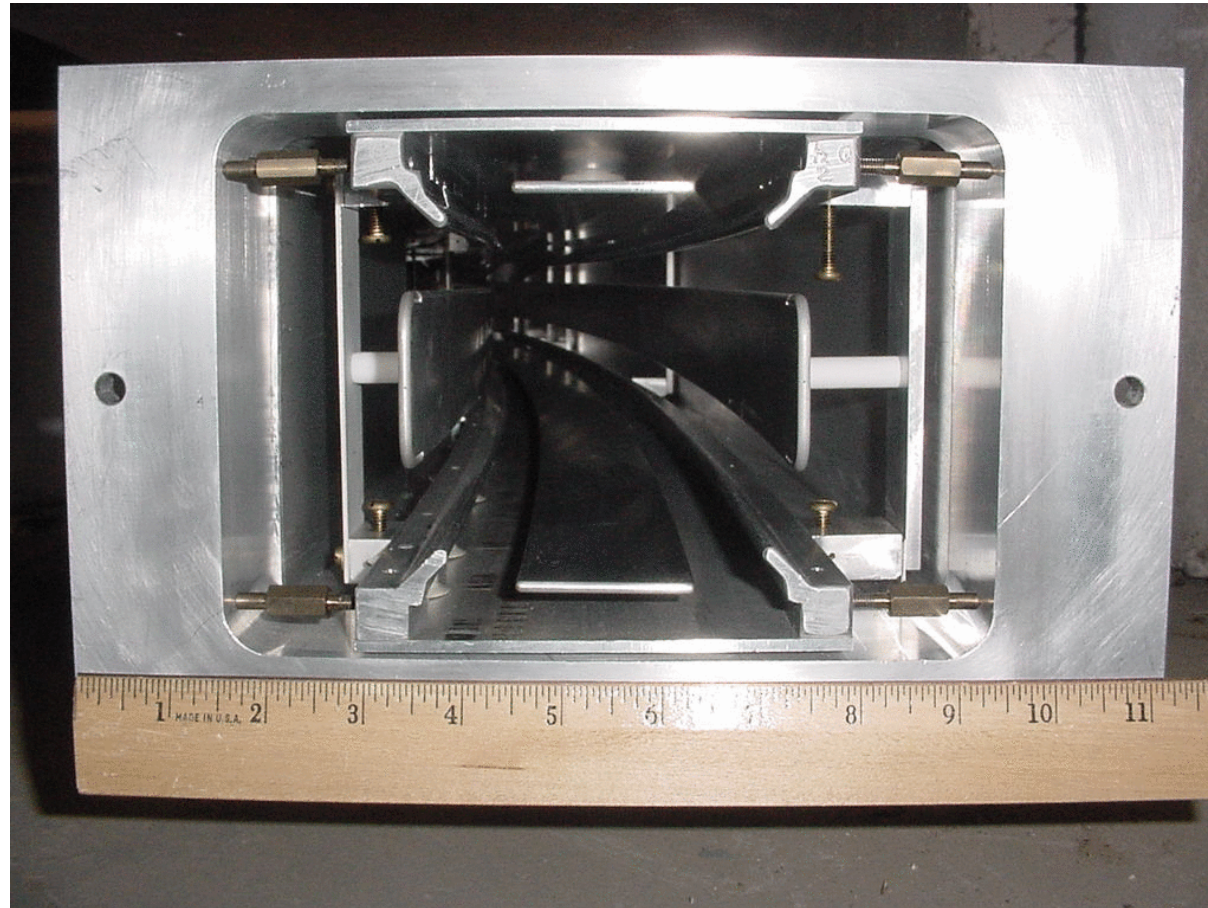
Storing the Muon Beam: The Fast Muon Kicker



- Muons enter 77 mm outside ideal closed orbit with radius 7112 mm
- Muons cross ideal orbit at 90° , angle off by $77 \text{ mm}/7112 \text{ mm} \approx 11 \text{ mrad}$
- ⇒ Reduce \mathbf{B} by $\approx 300 \text{ Gauss}$ over 4 metres for 149 ns at 100 Hz, 10% homogeneity
- Kicker steers muons onto stored orbit with $\approx 50 \text{ kV}$, 5000 Amp pulse

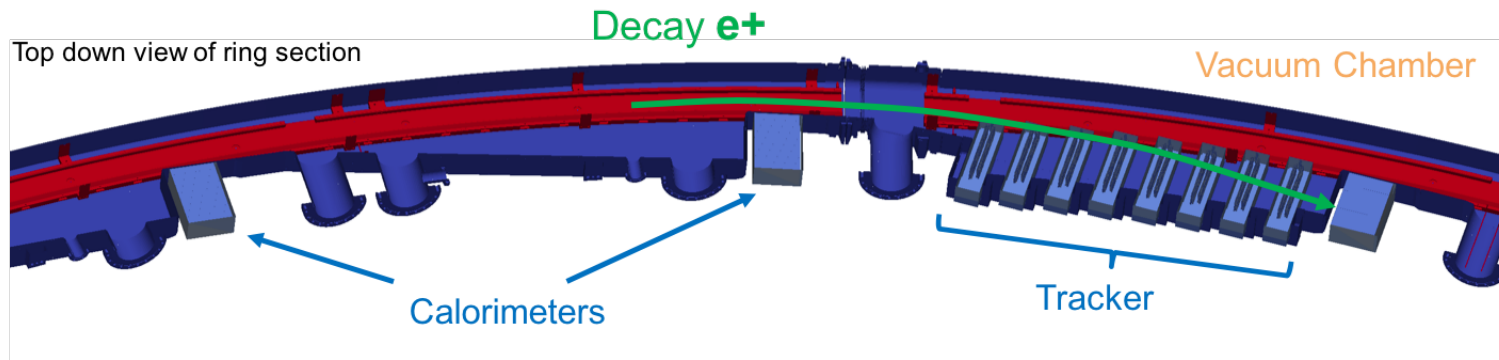
Storing the Muon Beam: Vertical Focusing Electric Quadrupoles

- Use electric quadrupoles for linear restoring force in vertical
- Uniform quadrupole field leads to simple harmonic motion about closed orbit

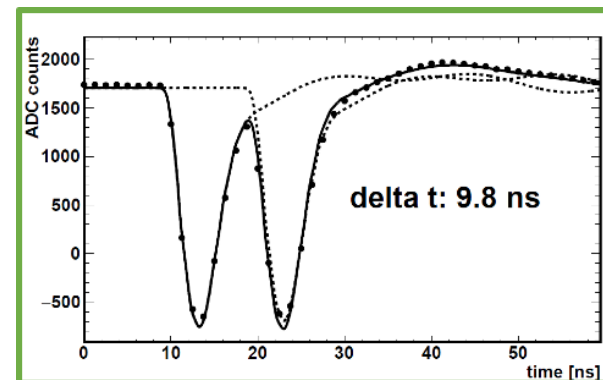
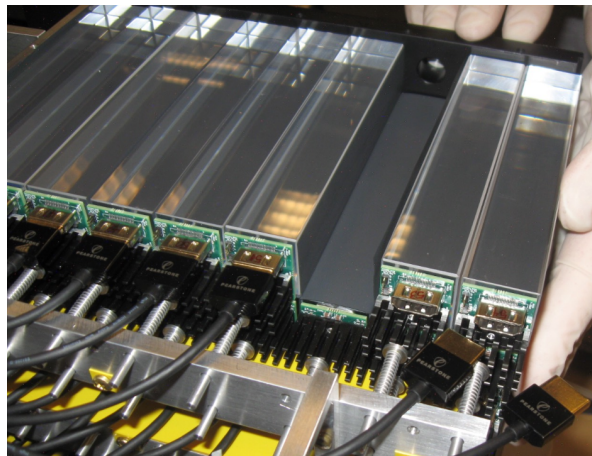


$$x = x_e + A_x \cos \left(\nu_x \frac{s}{R_0} + \delta_x \right), \quad y = A_y \cos \left(\nu_y \frac{s}{R_0} + \delta_y \right)$$

Measuring ω_a : Detecting the e^+ from muon decay with calorimeters



- ⇒ Muon Rest Frame: highest energy decay e^+ emitted in muon spin direction, rotates around
- ⇒ Lab Frame Positron Energy: $E_{\text{lab}} \approx \gamma E^* [1 + \cos(\omega_a t)]$
- ⇒ Positron detection rate above threshold $\propto \cos(\omega_a t)$
 - 24 calorimeters of 9×6 PbF_2 crystals + SiPMs detect e^+ from μ decay,
 - Digitize at 800 MSPS 12 bits for 700 μs , timing resolution 25 ps, gain stability 10^{-4}
 - Reconstruct e^+ energy and time \Leftrightarrow extrapolate for phase of μ^+ spin at decay



$$\omega_a \approx a_\mu \left[\frac{eB}{m_\mu} \right]$$

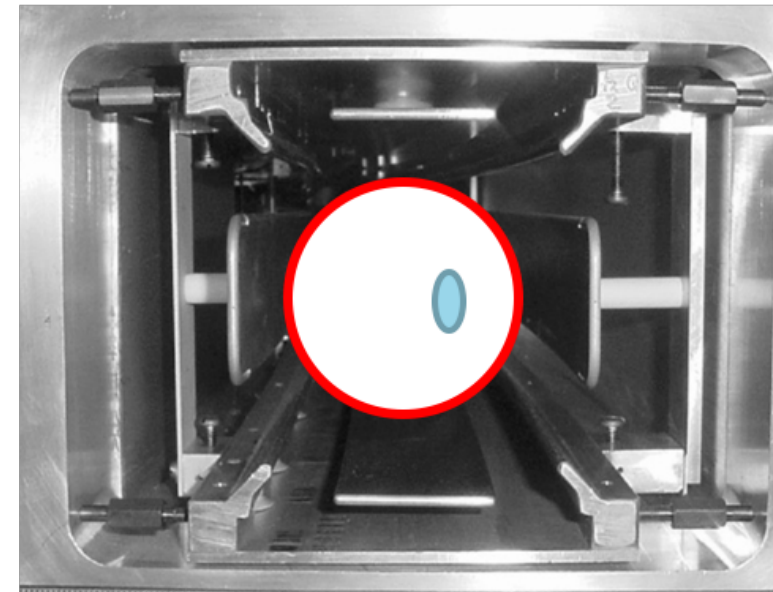
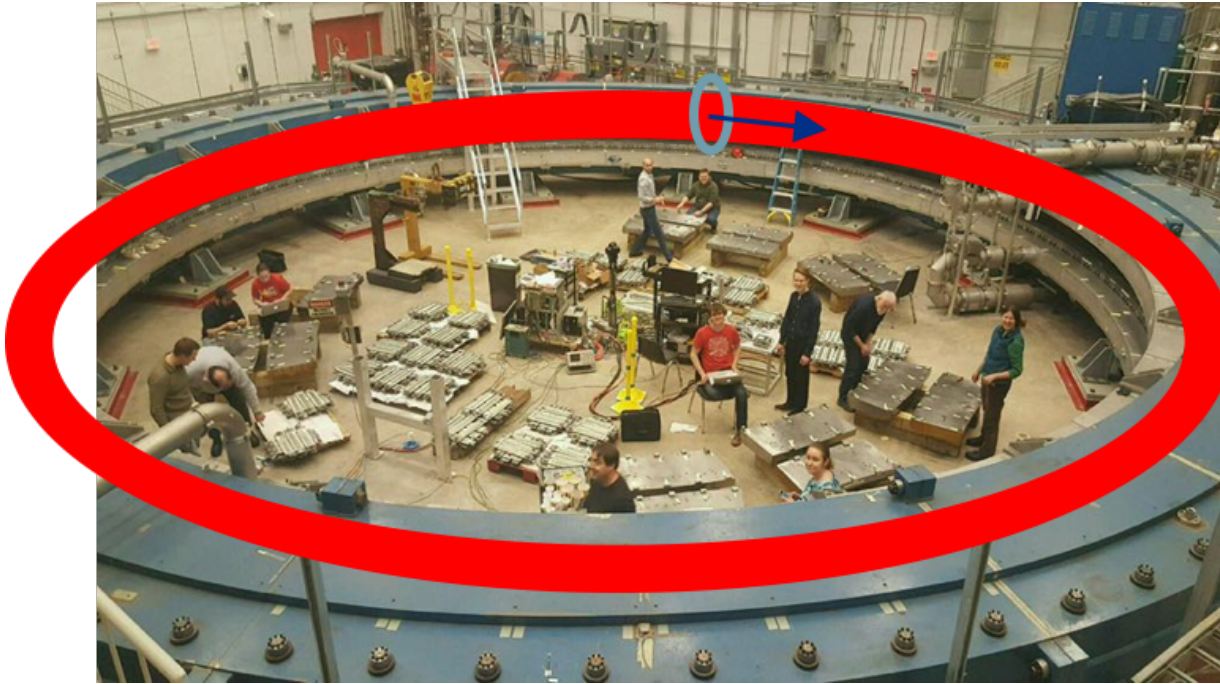
- Want $a_\mu \Rightarrow$ need to measure ω_a and eB/m_μ
 - Measure B in terms of *equivalent free proton precession frequency* ω_p using proton NMR: $\hbar\omega_p = 2\mu_p|\vec{B}|$
-

$$a_\mu = \frac{\omega_a}{\omega_p} \frac{2\mu_p}{\hbar} \frac{m_\mu}{e} = \frac{\omega_a}{\omega_p} \frac{\mu_p}{\mu_e} \frac{m_\mu}{m_e} \frac{g_e}{2}$$

\Rightarrow Experiment must measure ratio of two frequencies: ω_a/ω_p

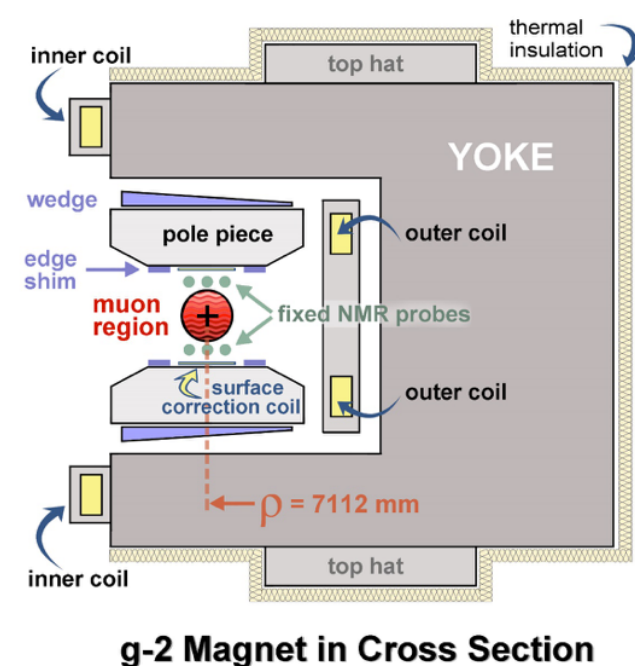
- Other ratios known to 22 ppb precision or better (but some subtleties involved!)
- $\omega_p \approx 2\pi \times 61.79$ MHz when $B = 1.45$ T
- Magnetic field team measures ω_p to 70 ppb

Storage Ring Magnetic Field Homogeneity



- Muons occupy volume determined by vertical and radial B fields, betatron oscillations
- Muon spin precesses according to B in small volume
- Need B field weighted by stored muon distribution $\Rightarrow \tilde{\omega}_p$
- Reasons for homogeneous field:
 - Stable beam dynamics, adiabaticity
 - Smaller uncertainty on $\tilde{\omega}_p$ from convolution of muon distribution with field
 - Easier to measure

Storage Ring Magnet: Centerpiece of the Experiment



- 682 tons, 4 coils \times 24 windings \times 5200 Amps/winding, 72 poles, $B=1.4513$ T
- $B \times \text{gap} \approx \mu_0 I \Rightarrow 1.45 \text{ T} \times 0.2 \text{ m} \approx 4\pi \times 10^{-7} \times 48 \times 5200 \text{ Amps}$, $\frac{\Delta B}{B} \approx -\frac{\Delta \text{gap}}{\text{gap}}$
- Oct 2015-Aug 2016: adjustments of pole gaps, tilts, 8000+ fine iron laminations
- B uniformity at ± 15 ppm level (RMS) \Leftrightarrow gap uniform at 2.7 micron level over 45 m!

Fermilab Goal: Measurement of B -Field to 70 ppb using Pulsed Proton NMR

⇒ Want precession frequency of free protons ω_p in storage volume while muons stored

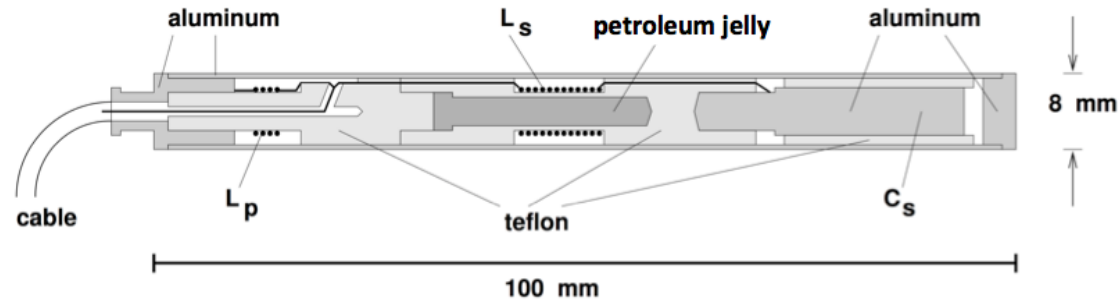
Fermilab Goal: Measurement of B -Field to 70 ppb using Pulsed Proton NMR

- ⇒ Want precession frequency of free protons ω_p in storage volume while muons stored
- Can't have NMR magnetometer probes in storage volume at same time/place as muons!

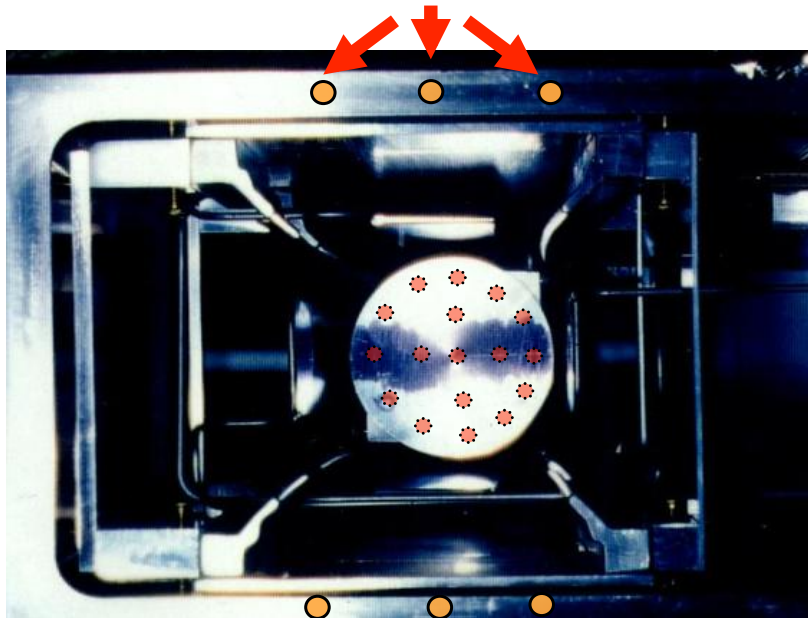
- ⇒ Want precession frequency of free protons ω_p in storage volume while muons stored
- Can't have NMR probes in storage volume at same time/place as muons!
 - Whatever we use to measure B-field perturbs the local field!
⇒ measured B-field different than what muons see!
 - Calibration/corrections necessary to go from magnetometer measurements to free proton ω_p

Fermilab Goal: Measurement of B -Field to 70 ppb using Pulsed Proton NMR

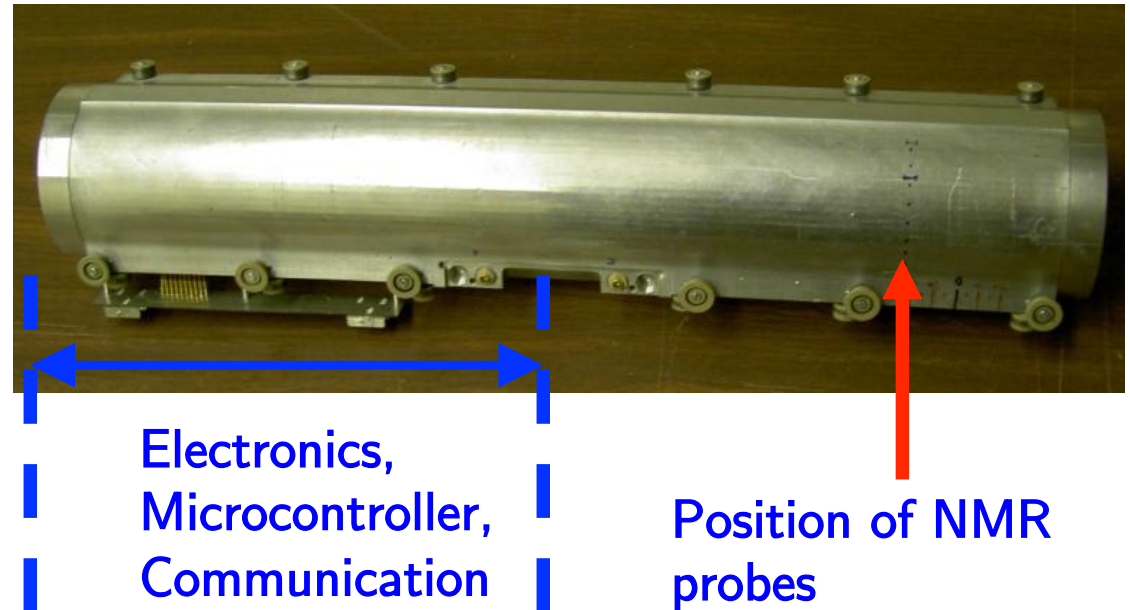
- 387 Fixed NMR probes outside storage volume measure field while muons stored
- Field inside storage volume measured by NMR trolley periodically
- Fixed probes calibrated when trolley passes; can infer field inside storage volume



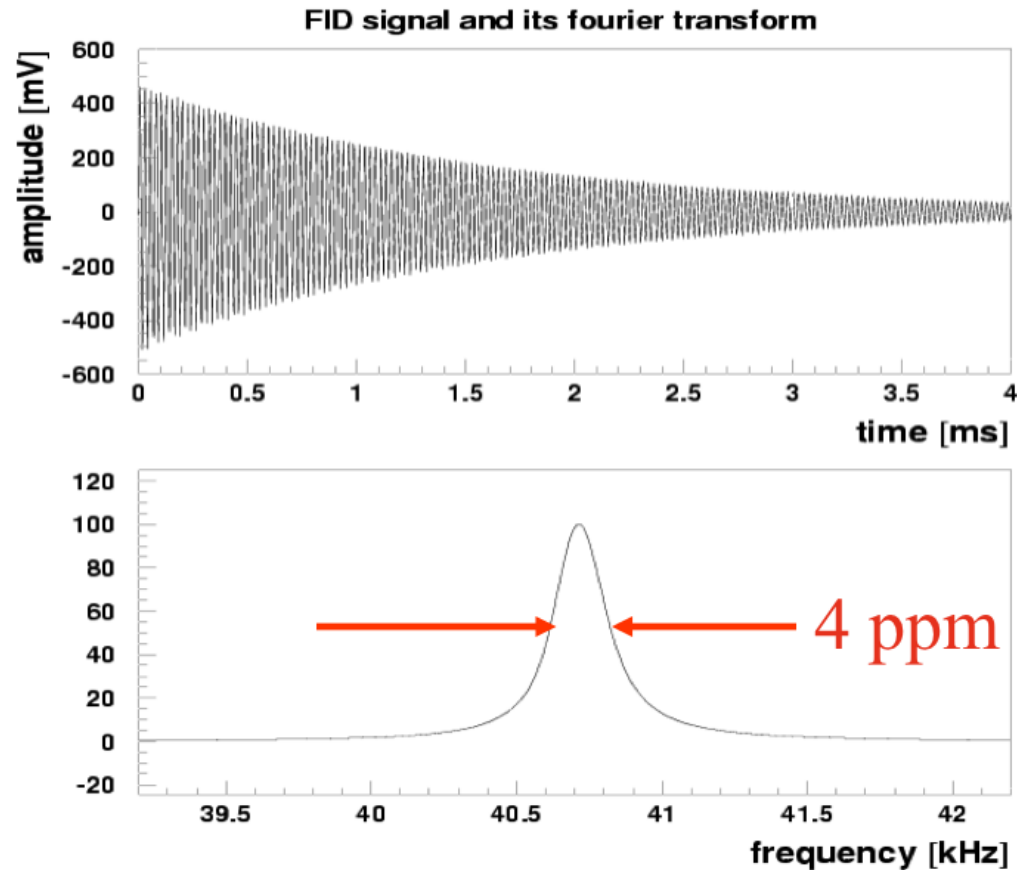
Fixed probes on vacuum chambers



Trolley with matrix of 17 NMR probes



Field Measurement with Pulsed NMR



⇐ Free induction decay (FID) and Fourier transform

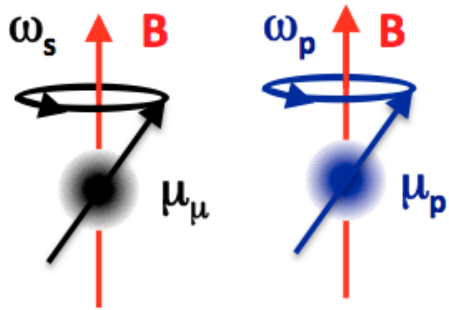
- Signal : noise $\geq 200 : 1$
- Frequency resolution
 $\approx \text{linewidth} / [S/N]$
 $\approx 120 \text{ Hz} / 200 = 0.6 \text{ Hz}$

- Resolution of field measurement in single NMR pulse:

$$\frac{\delta B}{B} \approx \frac{\delta f_{\text{NMR}}}{f_{\text{NMR}}} \approx \frac{0.6 \text{ Hz}}{61.79 \text{ MHz}} \approx 10 \text{ ppb}$$

- All ≈ 400 probe read out every 1.7 seconds
- Corrections necessary to get from f_{NMR} of NMR magnetometers to ω_p of free proton

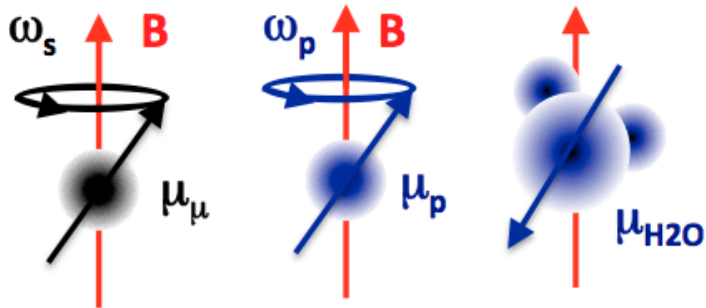
How do we go from NMR probe precession frequencies to ω_p



$$\omega_p^{\text{probe}} = \left[1 \right] \omega_p^{\text{free}}$$

⇒ Determine B seen by muons from measurement of ω_p of free protons

How do we go from NMR probe precession frequencies to ω_p

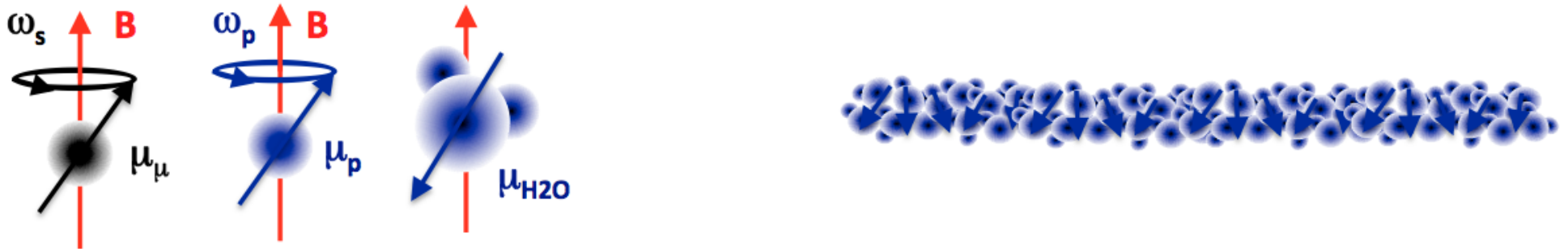


$$\omega_p^{\text{probe}} = \left[1 - \sigma(\text{H}_2\text{O}, T) \right] \omega_p^{\text{free}}$$

⇒ Determine B seen by muons from measurement of ω_p of free protons

- **Complication:** protons in H_2O molecules, diamagnetism of electrons screens protons, *changes local B*
- $\sigma(\text{H}_2\text{O}, T) = 25\,680(\pm 2.5) \times 10^{-9}$ at 25.0°C (Y. Neronov and N. Seregin, Metrologia 51, 54 (2014))

How do we go from NMR probe precession frequencies to ω_p

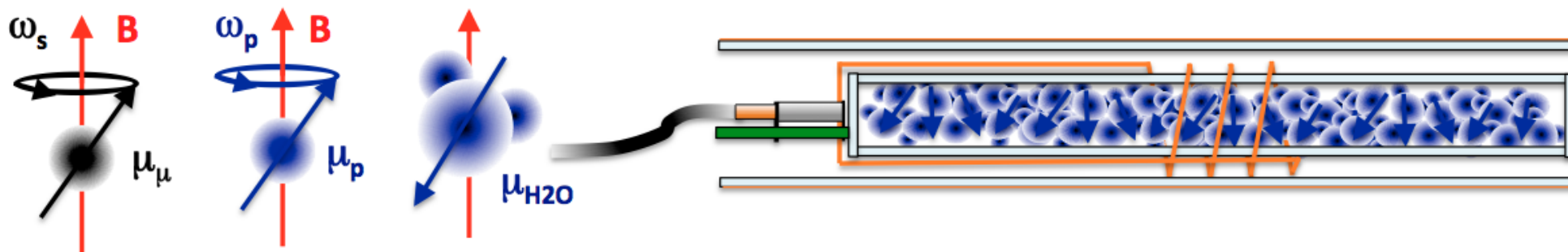


$$\omega_p^{\text{probe}} = \left[1 - \sigma(\text{H}_2\text{O}, T) - \left(\epsilon - \frac{4\pi}{3} \right) \chi_{\text{H}_2\text{O}}(T) \right] \omega_p^{\text{free}}$$

⇒ Determine B seen by muons from measurement of ω_p of free protons

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How do we go from NMR probe precession frequencies to ω_p



$$\omega_p^{\text{probe}} = \left[1 - \sigma(\text{H}_2\text{O}, T) - \left(\epsilon - \frac{4\pi}{3} \right) \chi_{\text{H}_2\text{O}}(T) - \delta_{\text{probe}} \right] \omega_p^{\text{free}}$$

⇒ Determine B seen by muons from measurement of ω_p of free protons

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- **Complication:** Magnetization of water sample gives shape-dependent field perturbation: $\epsilon = 4\pi/3$ for a sphere, $\epsilon = 2\pi$ for cylinder $\perp \vec{B}$
- **Complication:** Magnetization of probe materials perturbs field at protons

⇒ Need special NMR electronics and probes to determine corrections to 35 ppb accuracy

Corrections to ω_a : Pitch and Electric Field Correction

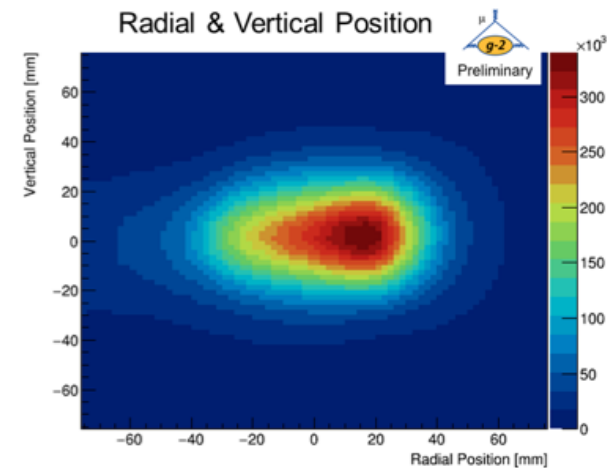
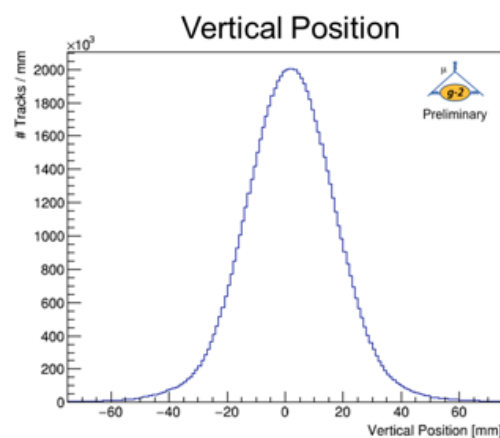
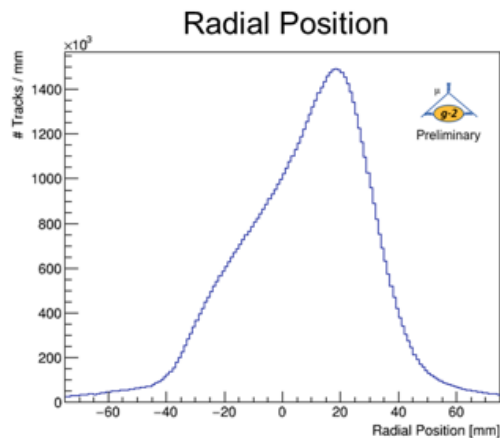
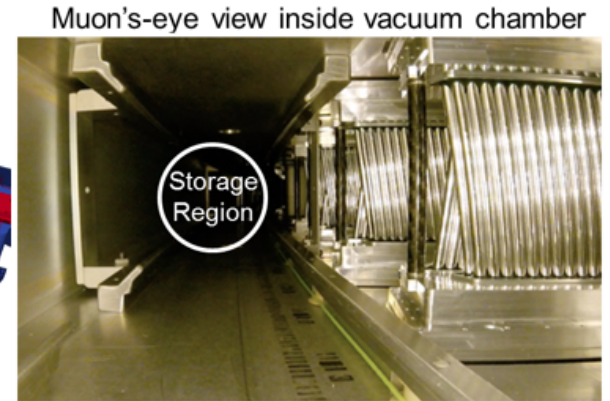
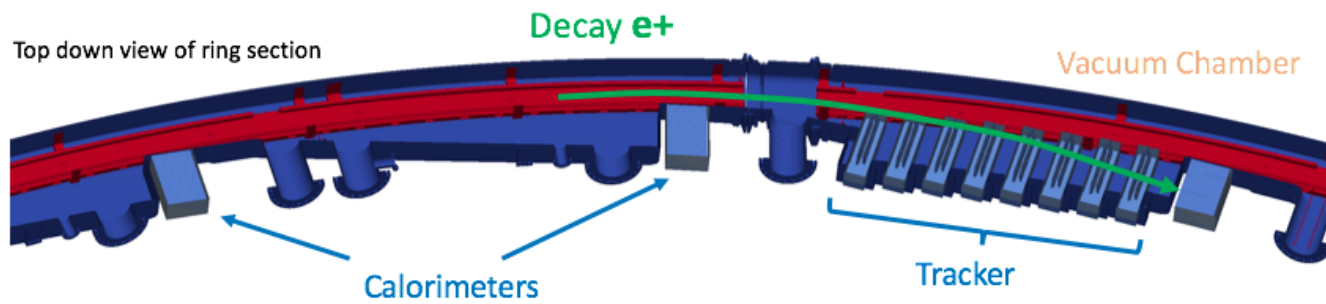
- Corrections to ω_a determined by calorimeter required because:
 - (1) Not all muons at magic momentum \Rightarrow not on center orbit \Rightarrow see net electric field
 - (2) Vertical betatron motion: muons pitching up/down out of horizontal plane

$$\vec{\omega}_a \approx \vec{\omega}_S - \vec{\omega}_C = \underbrace{-\frac{e}{m} a_\mu \vec{B}}_{\text{What we want}} - \underbrace{a_\mu \left(\frac{\gamma}{\gamma + 1} \right) (\vec{\beta} \cdot \vec{B}) \vec{\beta}}_{\text{Pitch Correction}} - \underbrace{\left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c}}_{\text{E-Field Correction}}$$

- **E-field correction needs momentum distribution:** from fast-rotation (de-bunching) analysis, straw tracking chambers, muon beam fiber monitors
- For BNL: electric field correction $\approx +0.47 \pm 0.05$ ppm
- **Pitch correction: needs muon distribution:** from straw tracking chambers
- For BNL: pitch correction $\approx +0.27 \pm 0.04$ ppm

Corrections verified from detailed spin tracking analysis using complete relativistic equations, actual discontinuous quad geometry, actual magnetic field distributions, ...

Measuring Stored Muon Distribution with Straw Tracker Chambers



- Two sets of straw trackers: exquisite measurement of stored muon distribution
- Important for optimizing injection parameters
- Required for electric field and pitch corrections, convolution with magnetic field
- Center of mass of muon distribution currently above ideal value

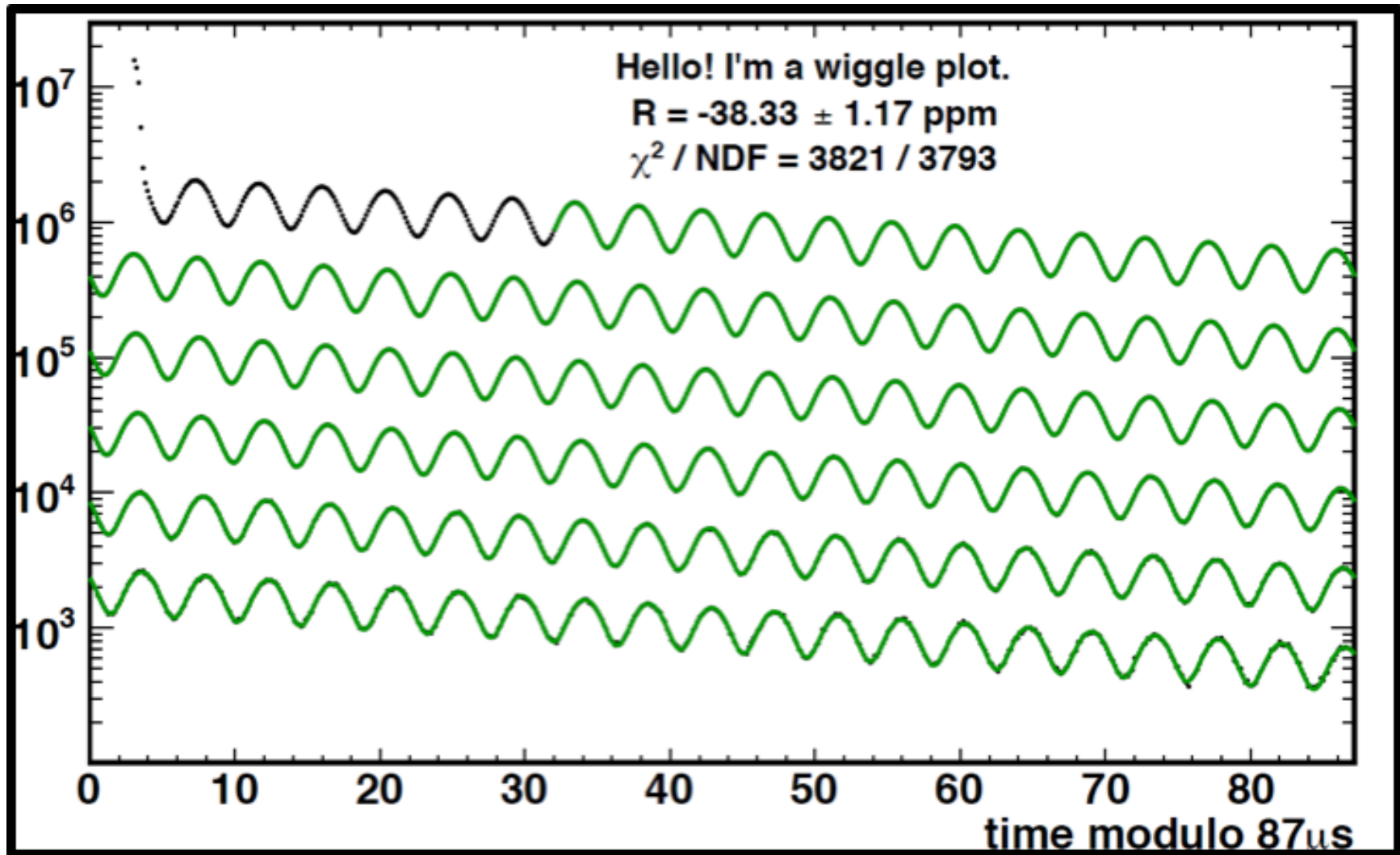
Systematic Uncertainty Goals on B Field Measurement ω_p

Source of uncertainty	1999	2000	2001		E989
Systematics of calibration probes	50	50	50	→	35
Calibration of trolley probes	200	150	90	→	30
Trolley measurements of B_0	100	100	50	→	30
Interpolation with fixed probes	150	100	70	→	30
Uncertainty from muon distribution	120	30	30	→	10
Inflector fringe field uncertainty	200	–	–		–
Time dependent external B fields	–	–	–	→	5
Others †	150	100	100	→	30
Total systematic error on ω_p	400	240	170	→	70
Muon-averaged field [Hz]: $\omega_p/2\pi$	61 791 256	61 791 595	61 791 400		–

- Implemented new electronics, new probes, new techniques reduce uncertainties factor 2.5
- Main issue: magnet not currently insulated, field not as stable as we'd like (1°C change \Rightarrow 35 ppm !)

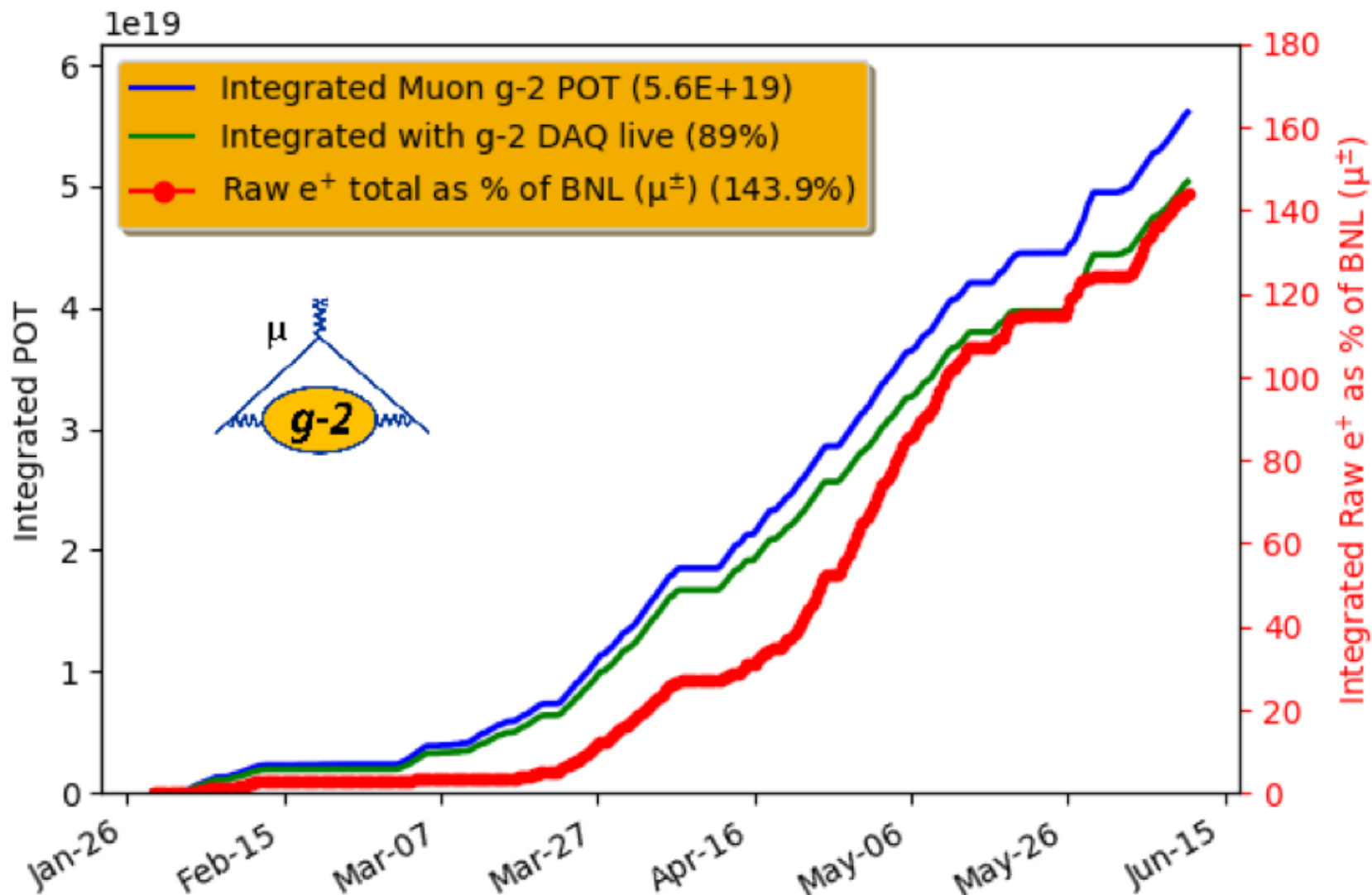
Category	E821 [ppb]	E989 Improvement Plans	Goal [ppb]
Gain changes	120	Better laser calibration low-energy threshold	20
Pileup	80	Low-energy samples recorded calorimeter segmentation	40
Lost muons	90	Better collimation in ring	20
CBO	70	Higher n value (frequency) Better match of beamline to ring	< 30
E and pitch	50	Improved tracker Precise storage ring simulations	30
Total	180	Quadrature sum	70

- Implemented new calorimeters, trackers, new techniques to reduce uncertainties factor 2.6
- Main issues: muons underkicked, momentum of stored muon above p_{magic} , fixes planned
- Stored muon flux below design value, fixed planned



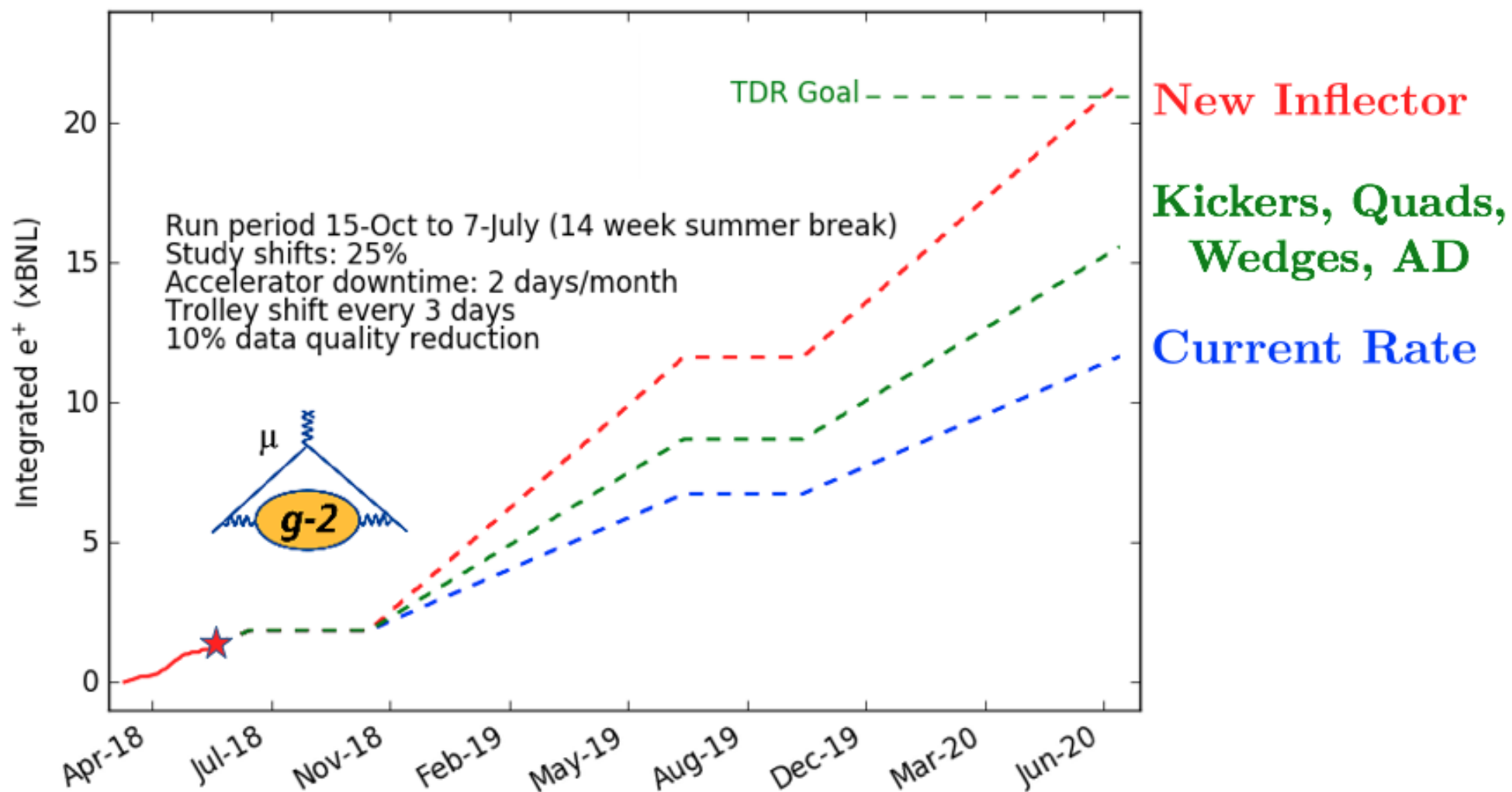
e^+ Signal from Muon Decay: $N_{\text{ideal}}(t) = N_0 \exp(-t/\gamma\tau_\mu) [1 - A \cos(\omega_a t + \phi)]$

- Data from 60 hour period, ω_p offline analysis very advanced
- Corrections for pileup, muon losses, CBO effects, long-term gain changes



- Have data set comparable to BNL statistics !
- Cuts on data quality (still to come) will reduce analyzable data set

The Path to Statistical Uncertainty Goals of 100 ppb



Summary and Thanks to Everyone Here

- Muon g-2 persists as interesting result: highly cited, community paying attention
- Significant progress by experiment:
 - ⇒ First muons stored in June 2017
 - ⇒ Result from 1st physics run with BNL level statistics by late 2018/early 2019?
 - ⇒ Full statistics on μ^+ \approx 2020, four-fold reduction in uncertainty to 140 ppb
- Theory community has made remarkable progress!
 - ⇒ Uncertainties projected in 2013 for final result already achieved!
 - ⇒ Remarkable progress on hadronic uncertainties, lattice

Your effort and improvements are what makes all of this interesting. Thank You!

Work supported by U.S. Department of Energy Office of Science



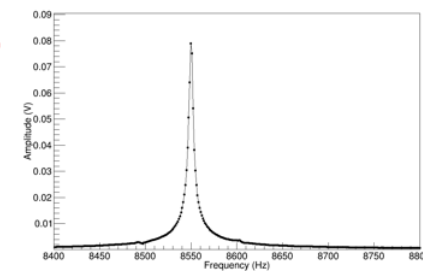
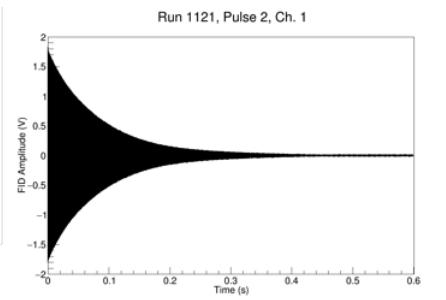
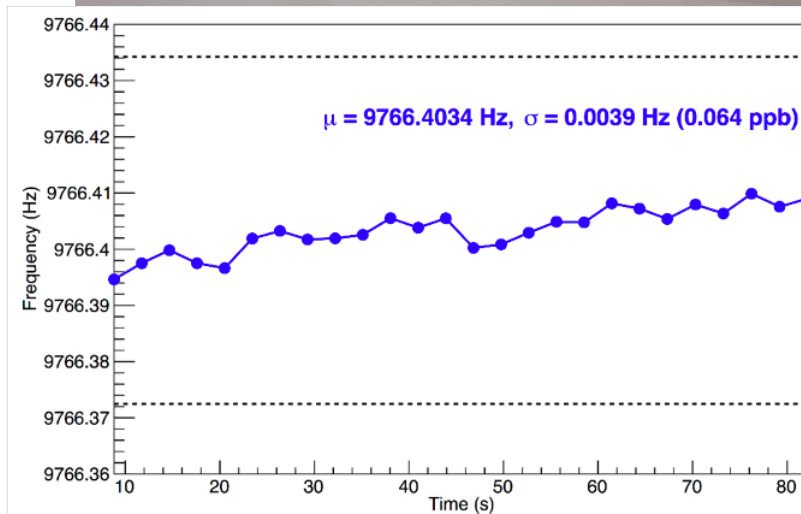
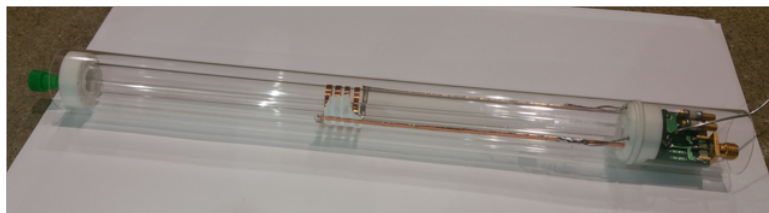
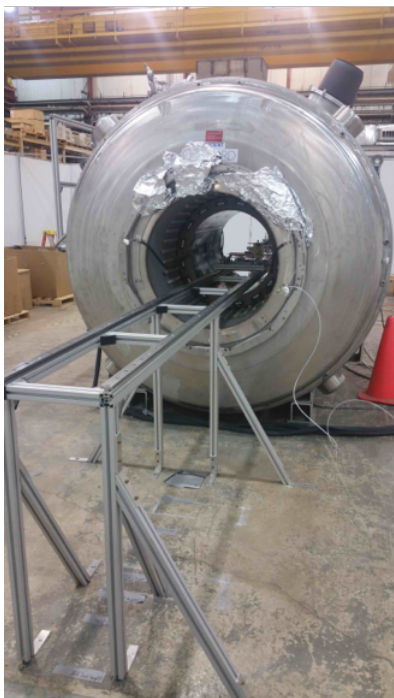
U.S. DEPARTMENT OF
ENERGY

Office of
Science

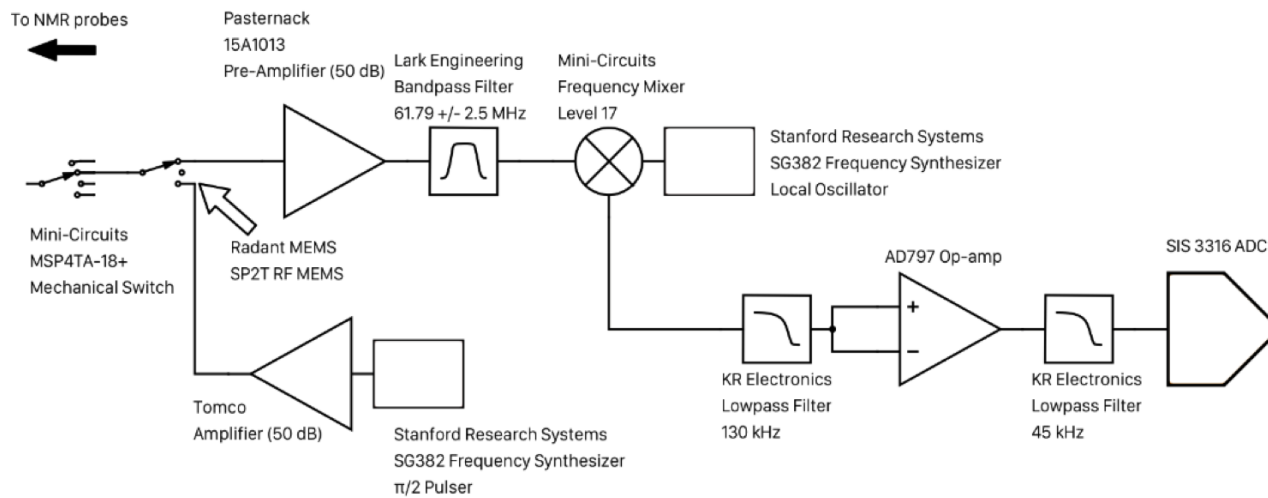
Event rate estimates at Fermilab

Item	Factor	Value per fill
Protons on target		10^{12} p
Positive pions captured in FODO, $\delta p/p = \pm 0.5\%$	1.2×10^{-4}	1.2×10^8
Muons captured and transmitted to SR, $\delta p/p = \pm 2\%$	0.67%	8.1×10^5
Transmission efficiency after commissioning	90%	7.3×10^5
Transmission and capture in SR	$(2.5 \pm 0.5)\%$	1.8×10^4
Stored muons after scraping	87%	1.6×10^4
Stored muons after $30 \mu s$	63%	1.0×10^4
Accepted positrons above $E = 1.86$ GeV	10.7%	1.1×10^3
Fills to acquire 1.6×10^{11} events (100 ppb)		1.5×10^8
Days of good data accumulation	17 h/d	202 d
Beam-on commissioning days		150 d
Dedicated systematic studies days		50 d
Approximate running time		402 ± 80 d
Approximate total proton on target request		$(3.0 \pm 0.6) \times 10^{20}$

Calibration NMR Probe Testing at MRI Solenoid at Argonne



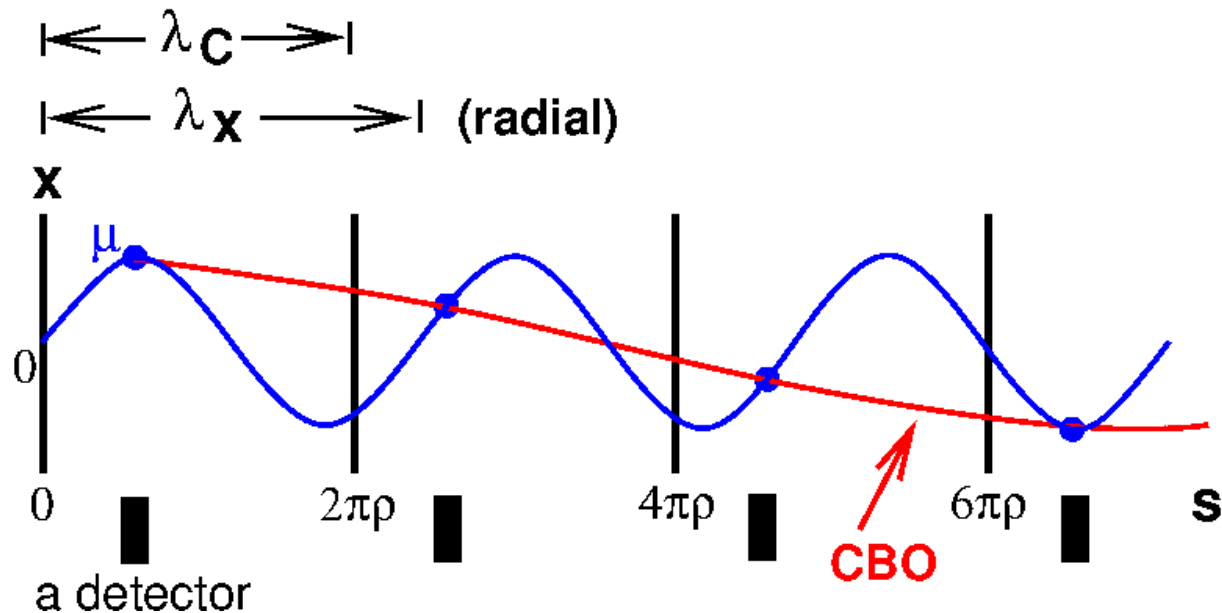
↑
1
ppb
↓



- Signal/Noise > 1500
- Linewidths of few Hz
- Frequency resolution < 100 ppt
- Easily see effects at ppb level

Coherent Betatron Oscillations (CBO)

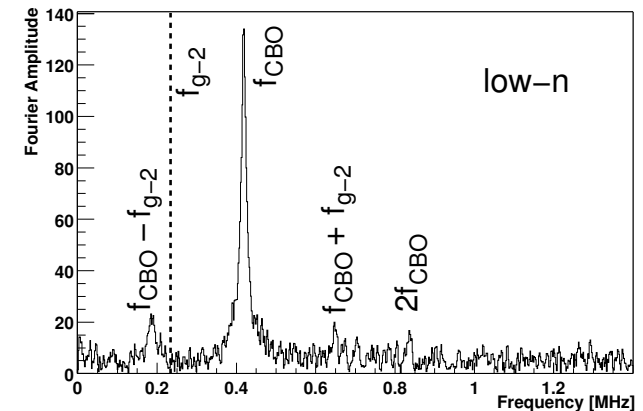
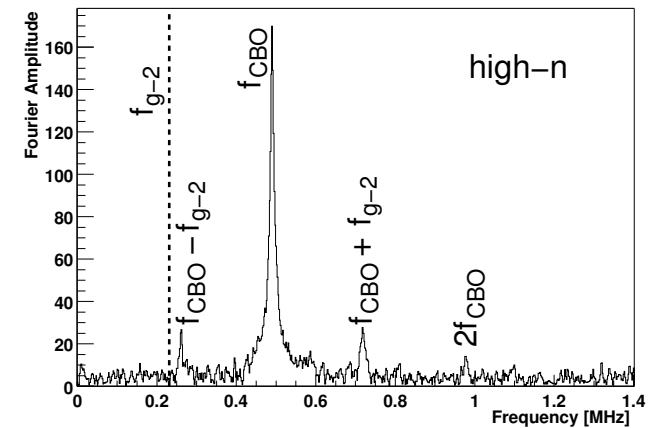
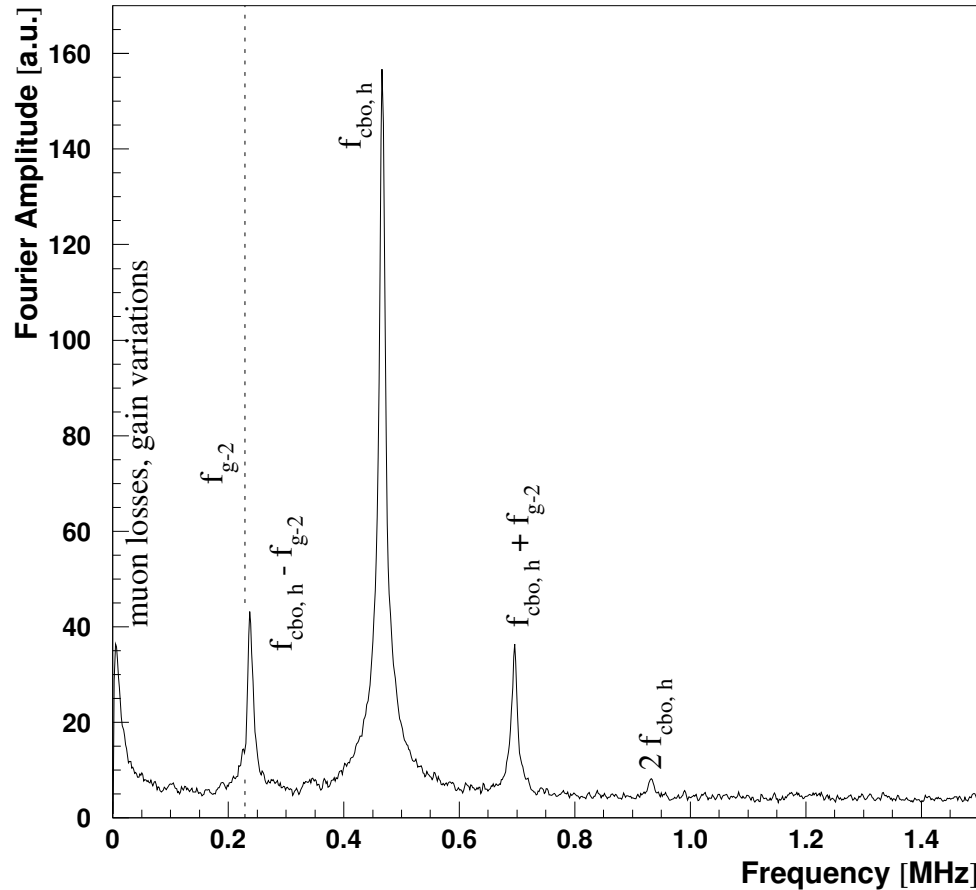
- Detector acceptance depends on muon radius at decay - coherent radial motion modulates electron time spectrum
- Radial betatron wavelength (blue line) is longer than circumference (cyclotron wavelength), $f_x < f_C$
- At fixed detector location, each pass of bunched beam appears at different radius - moving at f_{CBO}
- CBO frequency $f_{CBO} = f_C - f_x$ must be kept far from f_a



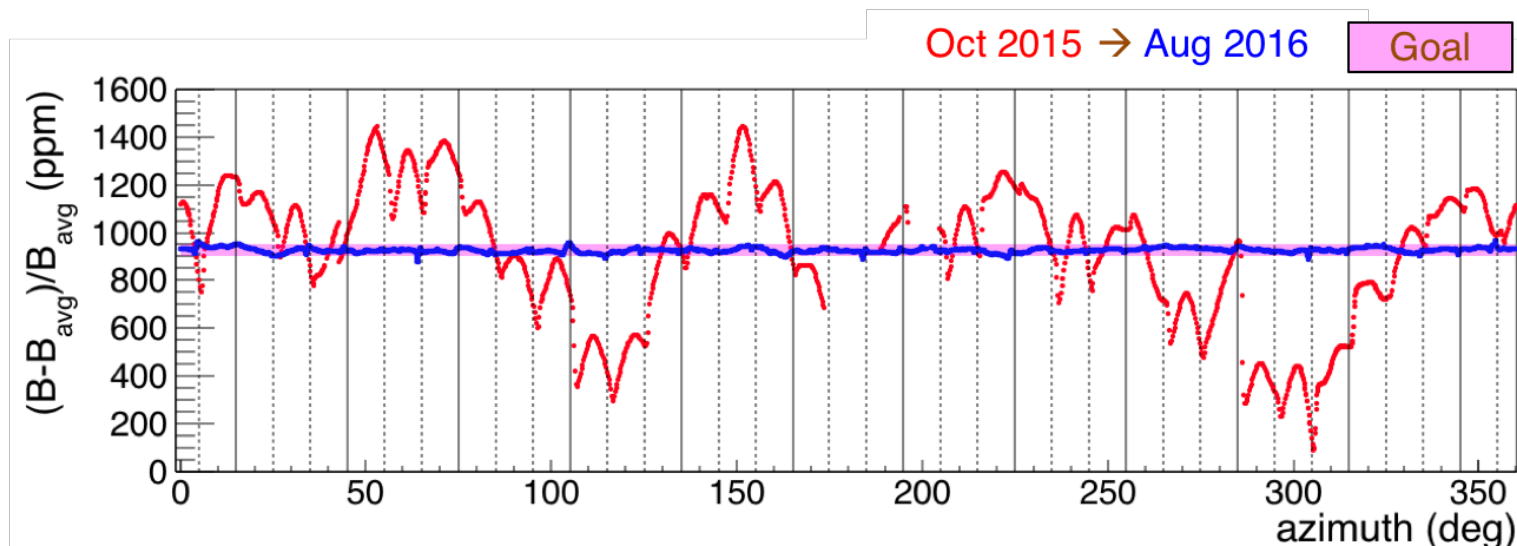
- Cyclotron wavelength marked by black lines, single detector by black block, betatron oscillations in blue
- Red line: apparent radial breathing in and out of beam at f_{CBO}
- Effect nearly cancels when all detectors added together

Coherent Betatron Oscillations (CBO)

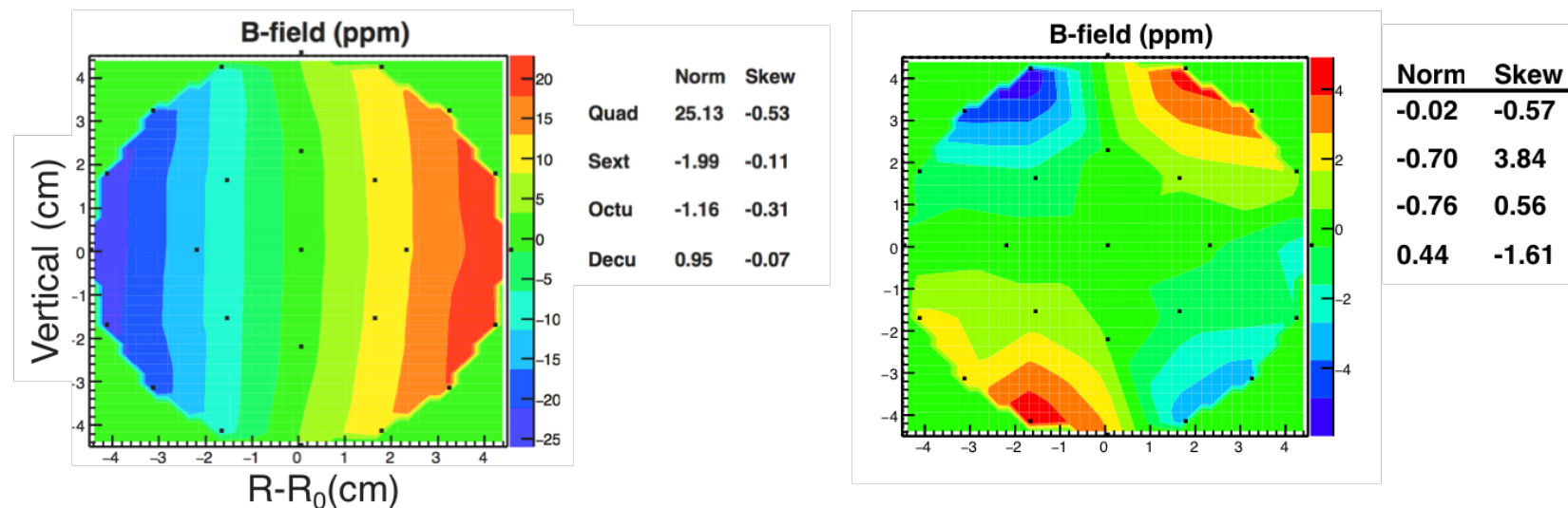
- BNL data taken in 2000 when CBO frequency close to f_a - can be seen in residual to 5 parameter fit
- In 2001, field index n changed to move f_{CBO} away from f_a



Progress in shimming the storage ring magnet to ± 25 ppm



Azimuthally Averaged Field Maps: Oct 2015 → Aug 2016



- Field nearly 3 times more homogeneous than BNL: easier to measure, smaller systematics
- Final shimming with surface coils will reduce remaining inhomogeneity