

Wave dark matter structure

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Collaboration with A.L. Maroto,
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Isotropy theorem (arbitrary spin)

Isotropy Theorem: The average Energy-Momentum tensor of a field of any spin minimally coupled to gravity is diagonal and isotropic if 1.- the field evolves rapidly with respect to the background metric evolution.

2.- $\phi^a{}_i$ and $\dot{\phi}^a{}_i$ are bounded.

Power-law theories:

$$\mathcal{H} = (\lambda^{AB} g_{00} \Pi_A^0 \Pi_B^0)^{n_T} + (M_{AB} \phi^A \phi^B)^{n_V}$$

Average equation of state:

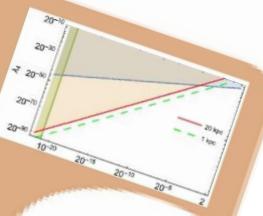
$$\omega = \frac{2 n_V}{1 + \frac{n_V}{n_T}} - 1$$

JARC, Hallabrin, Maroto, Nunez Jareño, Phys. Rev. D86 (2012)

JARC, Maroto, Nunez Jareño, Phys. Rev. D87 (2013) 043523

Repulsive Self-interactions

- Generic interaction: derivative and non-derivative terms.
- Low energy regime: nonrelativistic limit; conservation of matter + Euler equation
- Scalar field mass $10^{-21} eV < m < 10^{-4} eV$
- Negligible quantum pressure on cosmological and galactic scales
- Self-interaction generate a significant repulsive pressure.
- The hydrostatic equilibrium obtained by balancing the gravitational and scalar interactions imply that virialized structures have a solitonic core of finite size depending on the speed of sound of the dark matter fluid.



P. Brax, JARC, and P. Valageas, Phys. Rev. D 100, 023526 (2019) 2

Perturbations

CDM		$\Psi = \Phi \sim \text{const.}$ $\delta \rho \sim a^3$ $Q \sim a^2$	$\Psi = \Phi \sim \text{const.}$ $\delta \rho \sim a^2$ $Q \sim a^2$
Scalar	Vector	Particle Regime	Wave Regime
$\Psi = \Phi \sim \text{const.}$ $\delta \rho \sim a^2$ $Q \sim a^2$	$\Psi = \Phi \sim \text{const.}$ $\delta \rho \sim a^2$ $Q \sim a^2$	Cut-off	Cut-off
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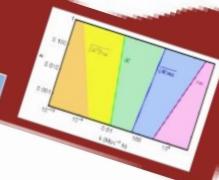
JARC, A.L.Maroto, Núñez Jareño, JHEP 1702 (2017) 064

$$\text{De Broglie wavelength: } \lambda_{\text{DB}} = \frac{l}{mv} = \frac{l}{mHn}$$

Localization in a sphere with radius:

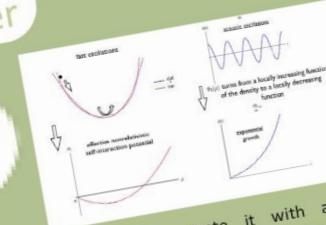
$$r \geq \lambda_{\text{DB}}$$

$$r \geq \frac{l}{\sqrt{Hn}}$$



Compact clusters as Dark Matter

The clumps aggregate and reach a universal regime.
They play the role of cold dark matter.



We illustrate it with a particular example provided by a negative quartic interaction stabilized by a positive six term.

P. Brax, JARC, and P. Valageas, Phys. Rev. D 102, 083012 (2020) 8

-When the squared speed of sound of the scalar fluid becomes negative, an instability arises and the fluctuations of the scalar energy-density field start growing. They eventually become nonlinear and clumps form..

