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# Parallel Session Wrap-Up: Origin of Mass

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**Matter and the Universe Programtag, Helmholtz Institute Mainz  
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# Origin of Mass

- \* **Electroweak symmetry breaking**

- Mass generation via the Higgs mechanism

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## \* Electroweak symmetry breaking

- Mass generation via the Higgs mechanism
- Measure Higgs couplings  $\Rightarrow$  major LHC activity
- Constrain models for physics beyond the SM

## \* Mass generation of visible matter

- Strongly coupled QCD
- Hadron spectrum & resonances from first principles
- Hadronic uncertainties in precision tests of the SM

# Origin of Mass: Programme

## \* Higgs Physics

- Emanuele Bagnaschi (DESY): *Higgs mass computation in BSM physics*
- Florian Staub (KIT): *Generic approach for Higgs mass calculations*

## \* Strong QCD

- Max Hansen (HIM): *Scattering and resonances from finite-volume calculations*
- Andreas Nyffeler (JGU): *Theoretical status of the muon  $g-2$*

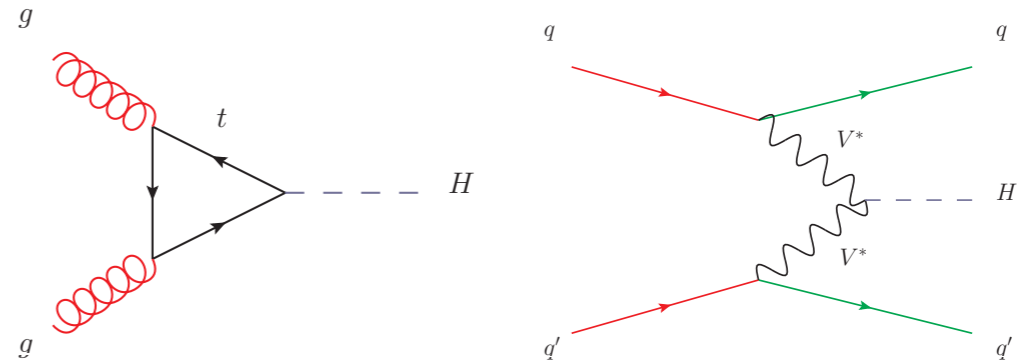
## \* Constraints on BSM physics

- Wolfgang G. Hollik (DESY): *Vacuum stability and the origin of mass*
- Marco Sekulla (KIT): *Unitarization and simplified models for vector boson scattering*

# Higgs Physics and BSM models

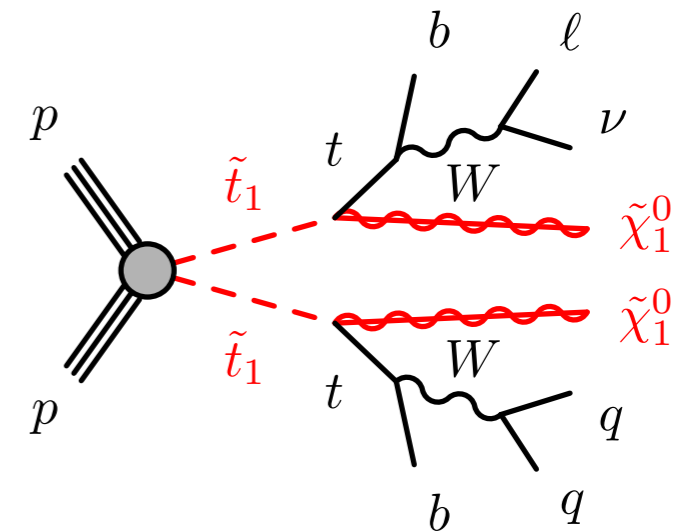
## \* Minimal Supersymmetric Standard Model (MSSM)

- solves the hierarchy problem
- provides a dark matter candidate
- null result at the LHC
- Higgs mass too heavy



## \* Renewed interest in “unnatural” SUSY models: scale for BSM physics far above EW scale

→ **Emanuele Bagnaschi**



## \* Confront MSSM and other BSM model with Higgs mass measurements

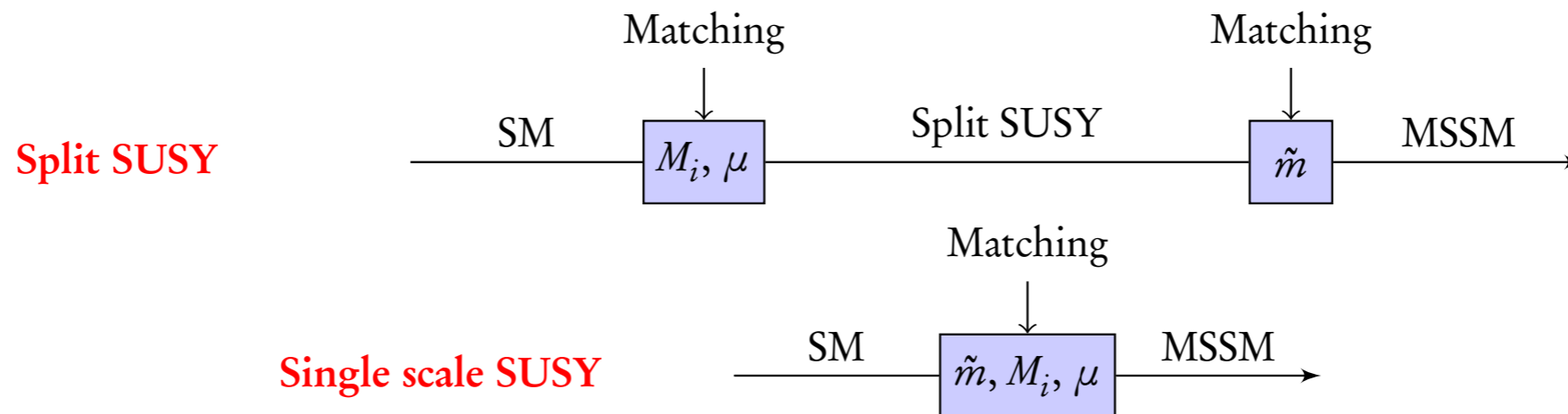
→ **Florian Staub**

# EFT Approach

\* Higher-order corrections to Higgs mass produce large logarithms

⇒ Employ Effective Field Theory approach

- ▶ **Problem:** mass gap in the physical spectrum makes large logs of the ratio  $m_{\text{ew}}/\tilde{m}$  appears in the perturbative expressions.
- ▶ **Solution:** For a proper computation these logs have to be resummed.
- ▶ **Method:** define a tower of effective field theories, where the heavy particles are integrated out, and match them at a proper scale. Use RGE to resum the large logarithms.



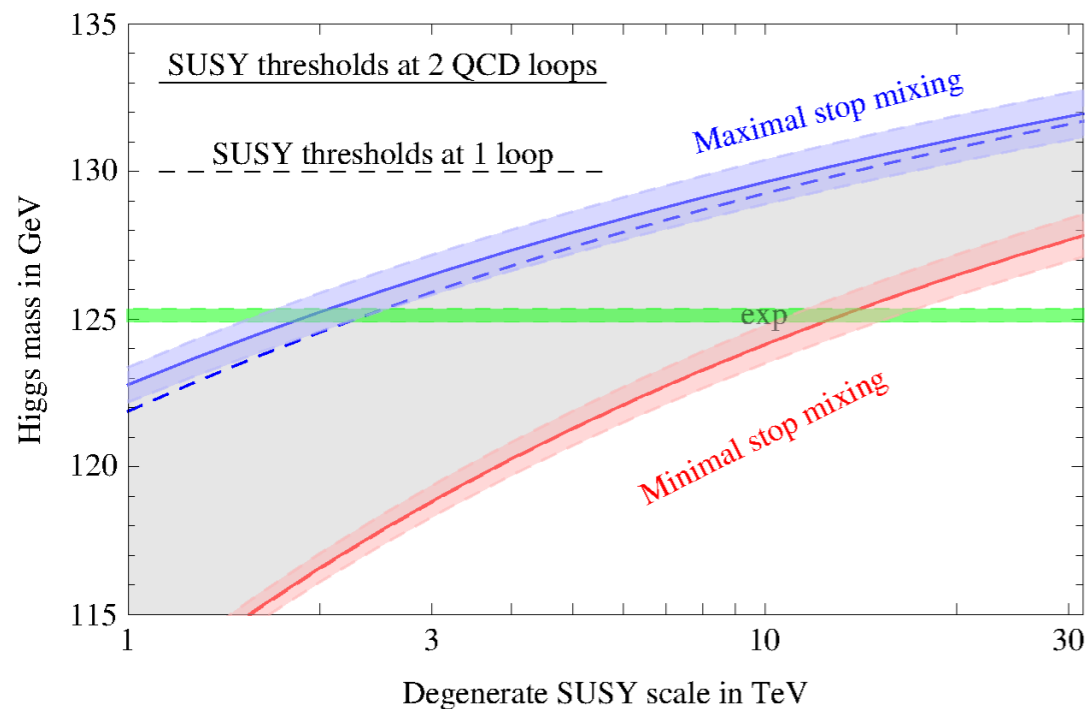
Emanuele Bagnaschi

# Higgs mass predictions in SUSY models

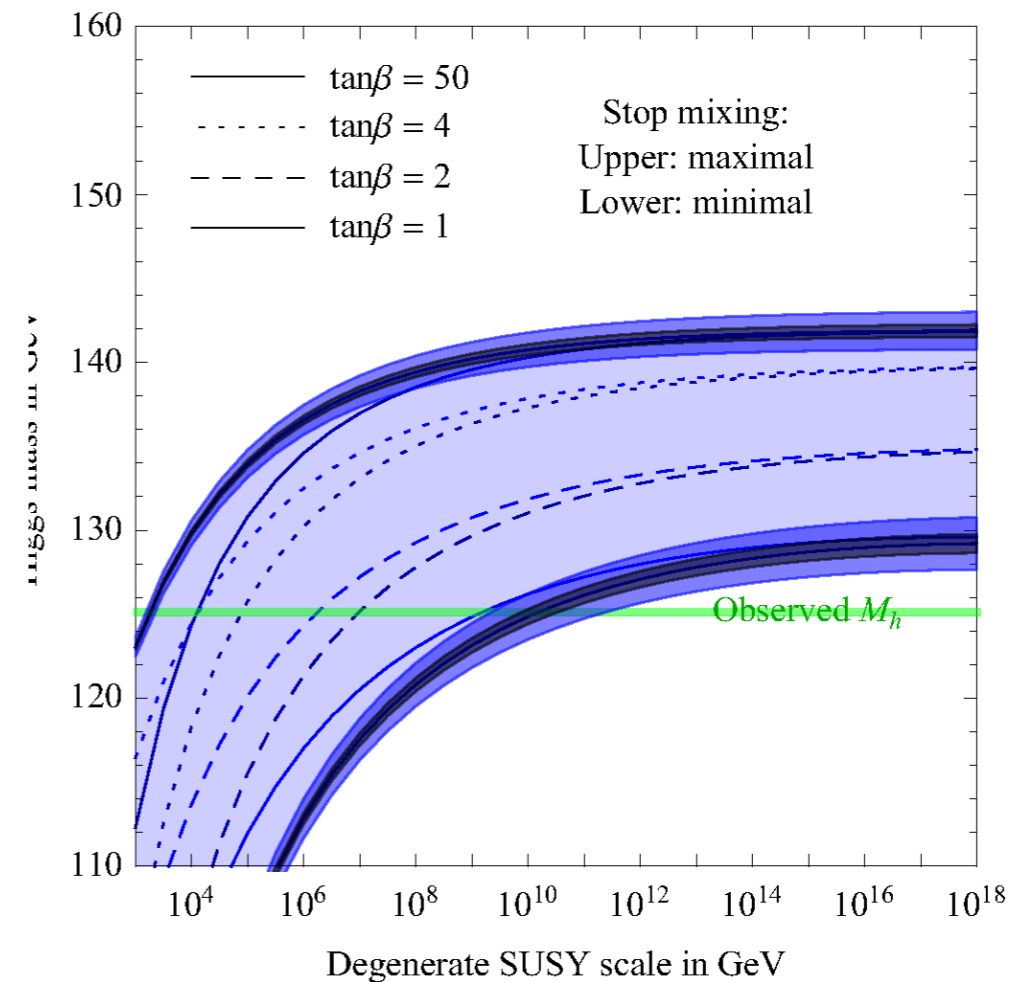
Quasi-natural SUSY:  
superpartners of  $O(10 \text{ TeV})$

High-scale SUSY: all SUSY  
particles of  $O(\tilde{m}) \gg \mu_{EW}$

Quasi-natural SUSY,  $\tan\beta = 20$



High-scale SUSY

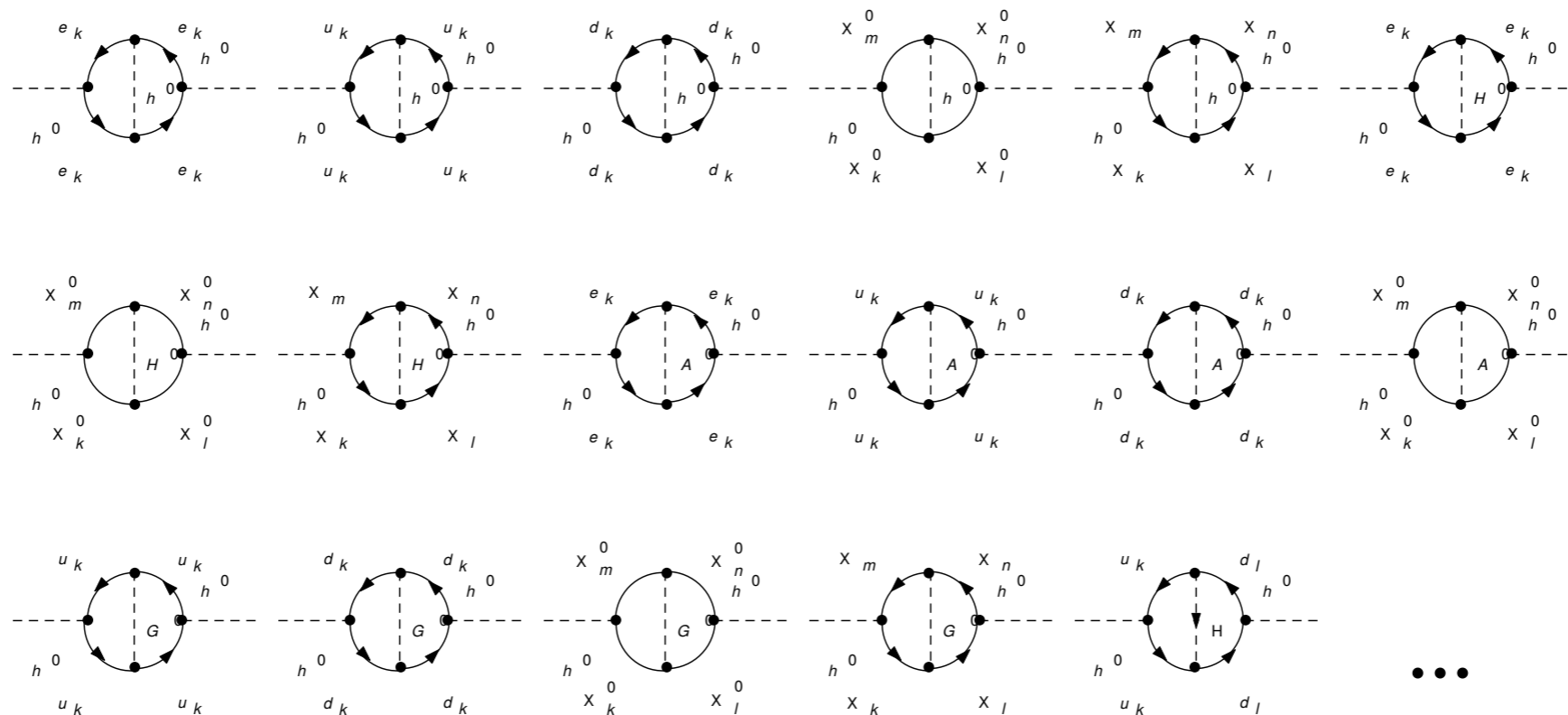


Emanuele Bagnaschi

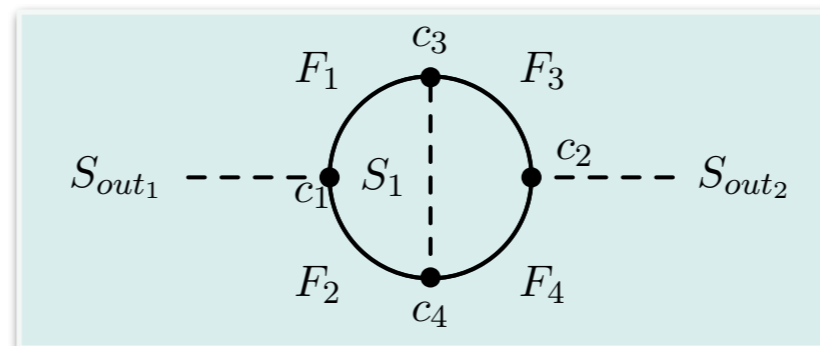


# Precision Higgs mass calculations in BSM

## \* Generic Higgs mass calculation



## \* Generic diagram:



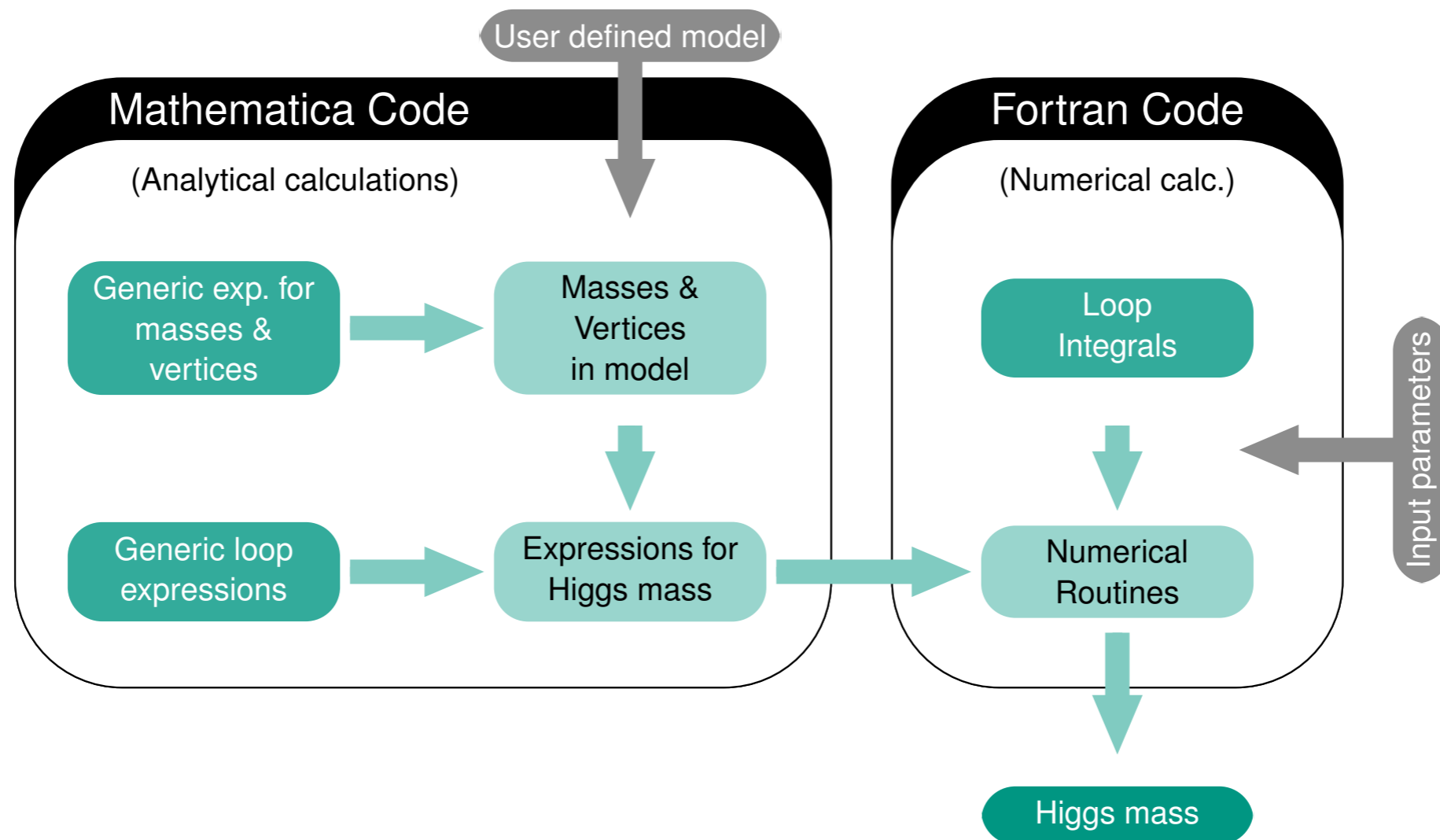
## \* Valid for any model and any real scalar

Florian Staub

# Precision Higgs mass calculations in BSM

\* Fully automated two-loop calculations:

SARAH/SPheno



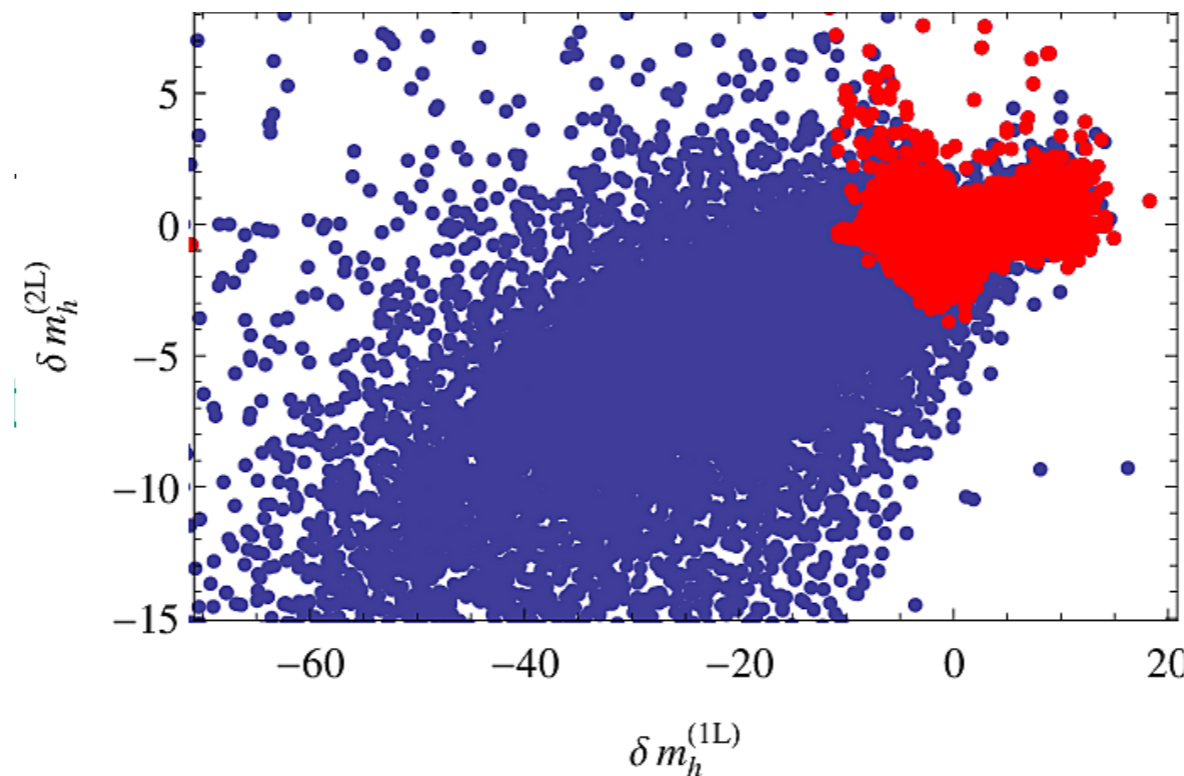
Florian Staub

# Precision Higgs mass calculations in BSM

- \* Study MSSM beyond Minimal Flavour Violation

$$\mathcal{L}_{SB} = \dots + T_u^{ij} \tilde{u}_i^* \tilde{q}_j H_u + T_d^{ij} \tilde{d}_i^* \tilde{q}_j H_d + T_e^{ij} \tilde{e}_i^* \tilde{l}_j H_d + \text{h.c.}$$

- \* Constrain couplings  $T_u^{ij}$  in the soft-breaking Lagrangian



- \* Can study NMSSM, vectorlike top partners, Dirac gauginos,...

Florian Staub

# Vacuum Stability and Origin of Mass

\* Higgs sector in the SM:

→ Wolfgang G. Hollik

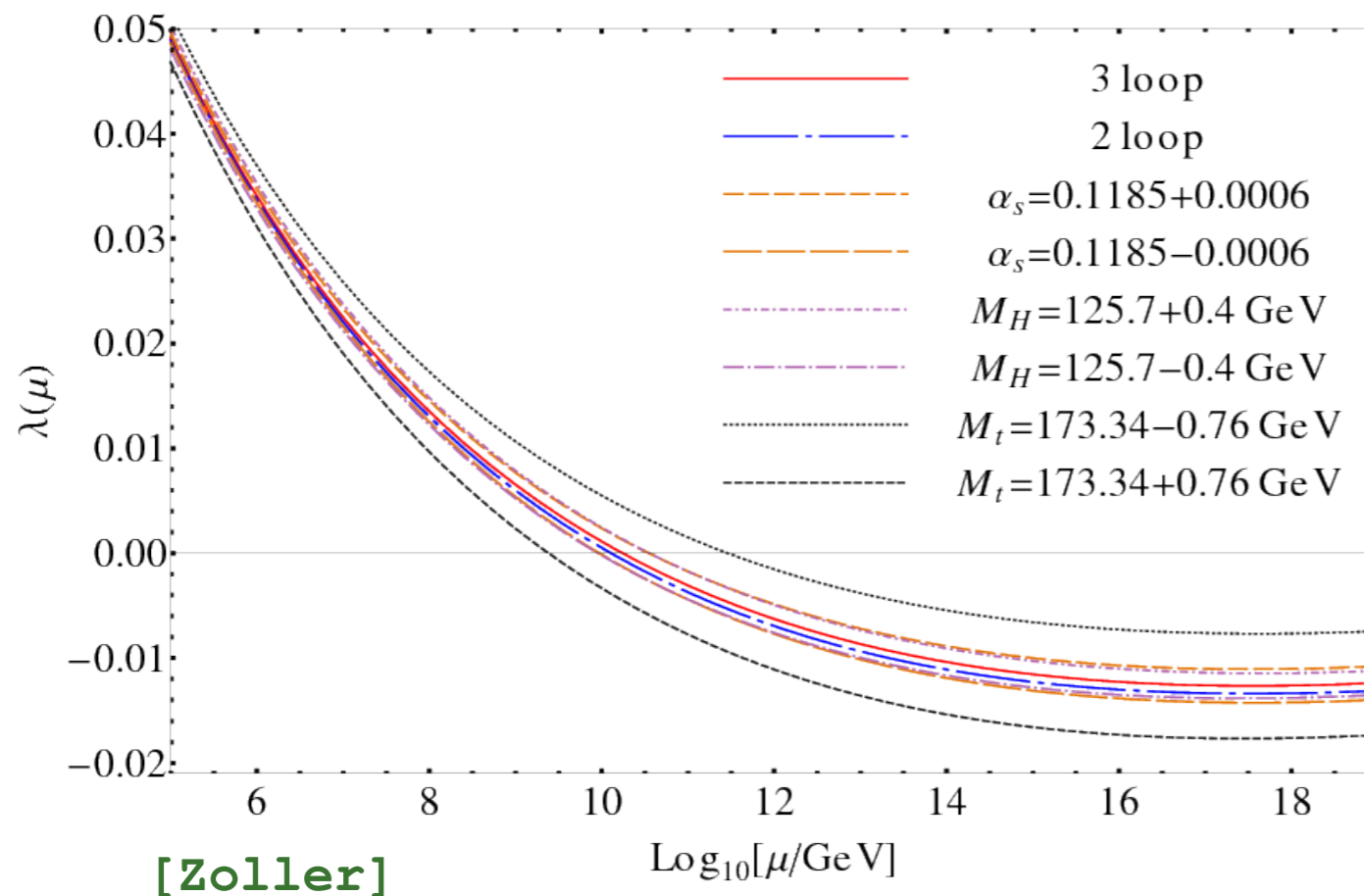
$$V_{\text{SM}} = -\mu^2 H^\dagger H + \lambda (H^\dagger H)^2$$

\* BSM: minimum may become unstable

\* Running of quartic self-coupling:  $\lambda = \lambda(Q)$

$\lambda(Q) \rightarrow 0$  for

$$Q \sim H \sim 10^{10} \text{ GeV}$$



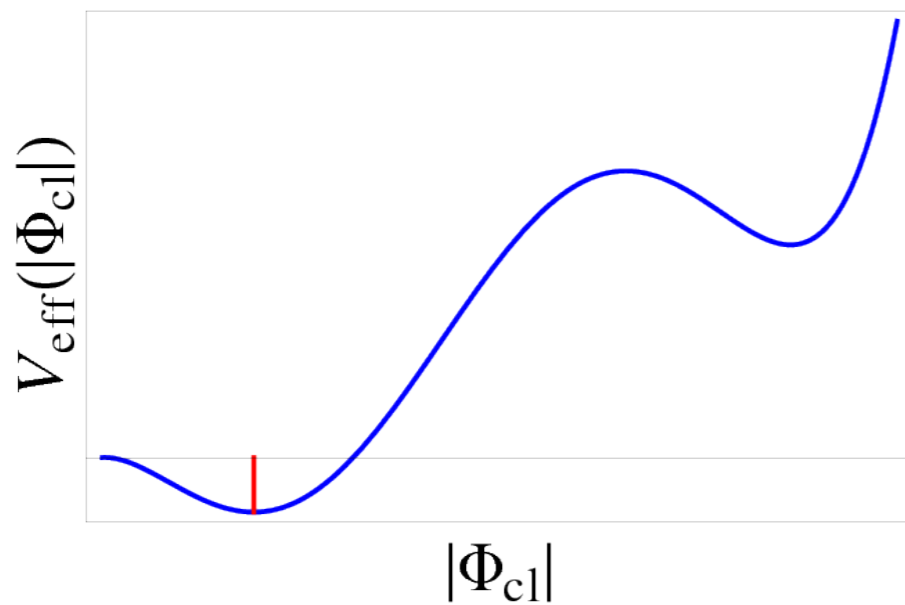
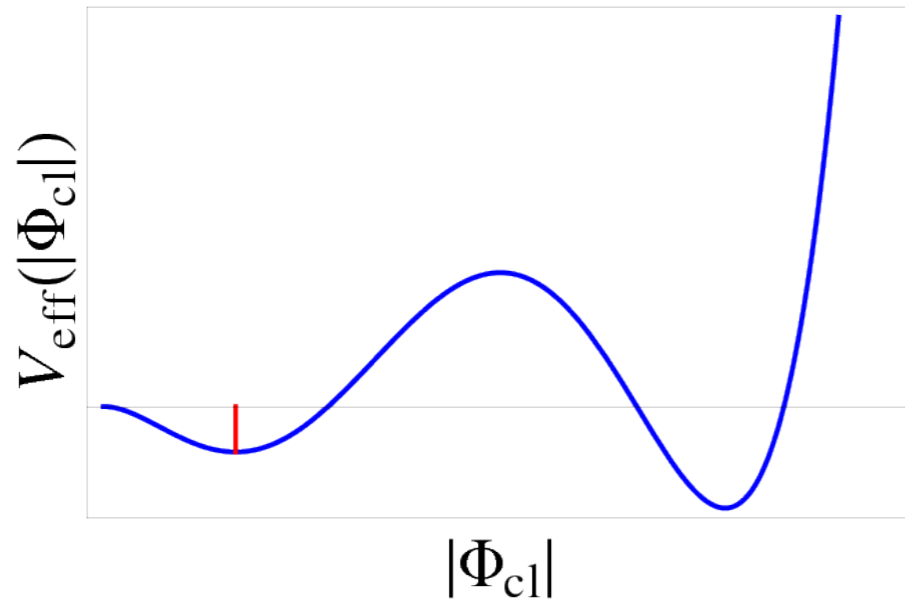
\* Main uncertainties:

$$M_{\text{top}}, \quad \alpha_s$$

# Vacuum Stability and Origin of Mass

\* Trans-Planckian VEV

\* Vacuum Stability

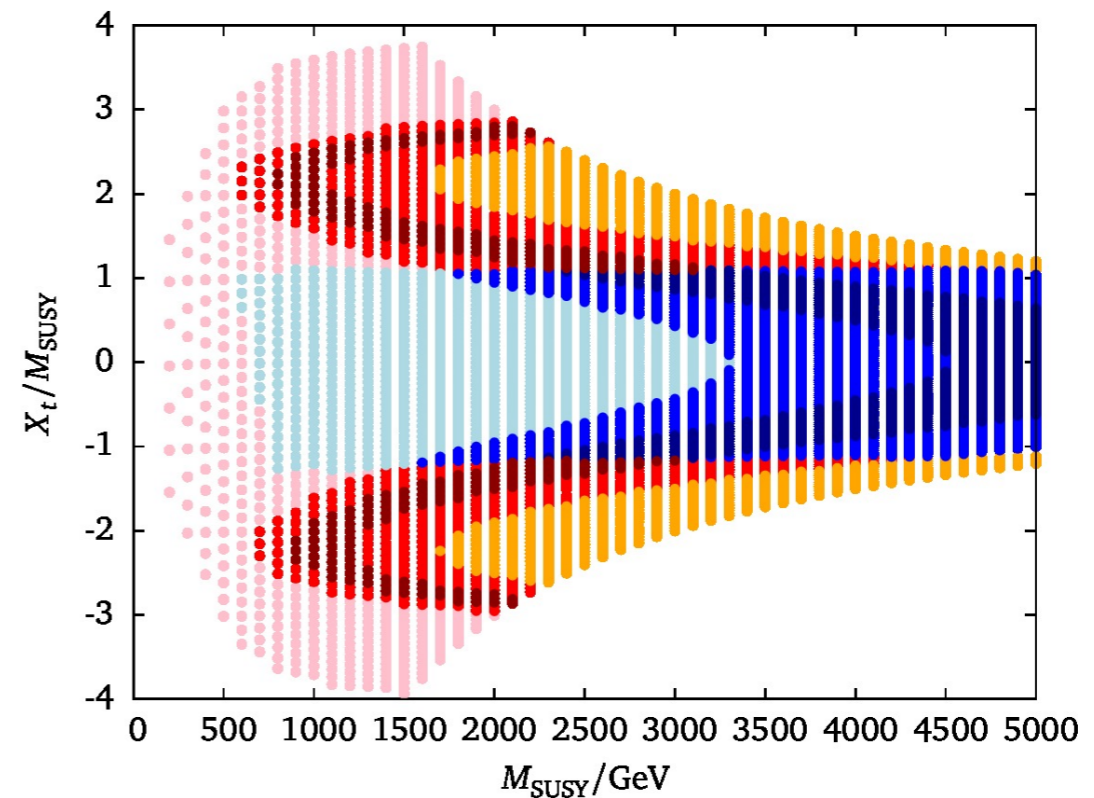
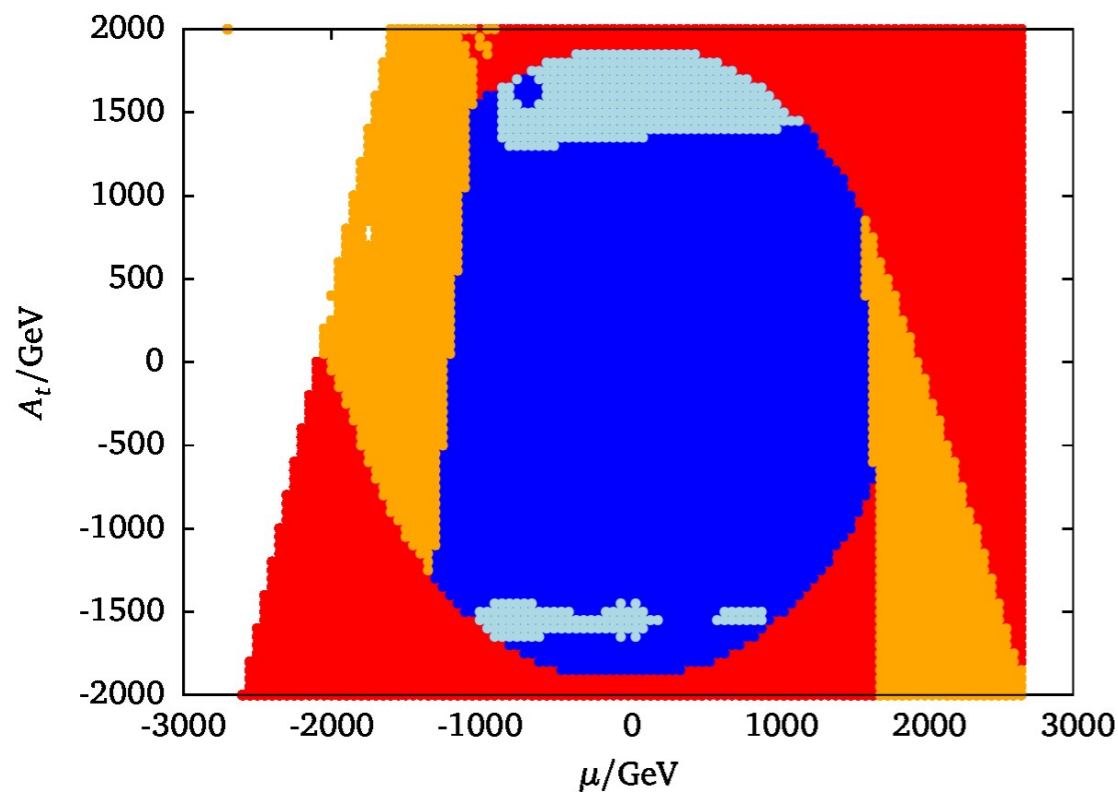


[Zoller]

[Degrassi et al. JHEP 1208 (2012) 098]

# Vacuum Stability and Origin of Mass

- \* BSM model: new particles contribute to the running of  $\lambda$
- \* Constrain BSM model parameters:  
require global minimum to coincide with EW minimum



Wolfgang G. Hollik

# Vector Boson Scattering

- \* SM: Higgs exchange cancels energy rise in VBS amplitude

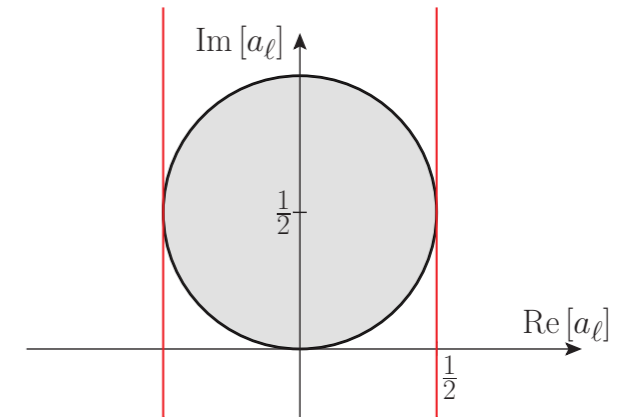
$$O(E^4) + O(E^4) + O(E^2) = O(E^0)$$

- \* VBS is sensitive probe for BSM physics: deviation of HVV vertex causes amplitude to grow  $\sim O(E^2)$   $\rightarrow$  unitarity violations
- \* EFT approach: new physics contributions via higher-dim. operators

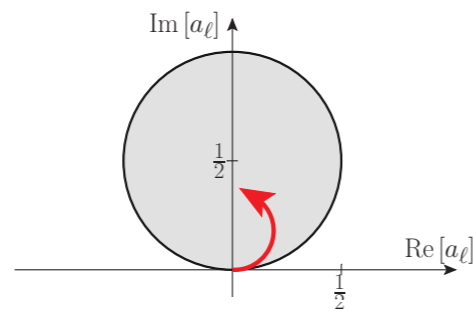
$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_{d \geq 4} \frac{C_i}{\Lambda^{d-4}} O_i^d$$

# Vector Boson Scattering

- \* Unitarity implies Argand-circle condition for partial wave amplitude
- \* Scenarios for new physics:

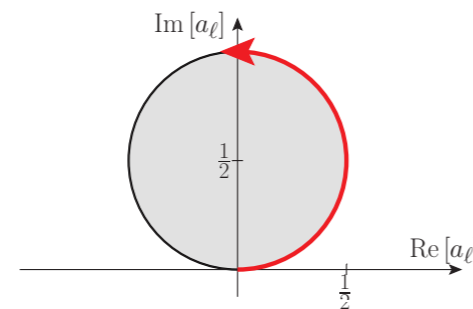


1 Inelastic



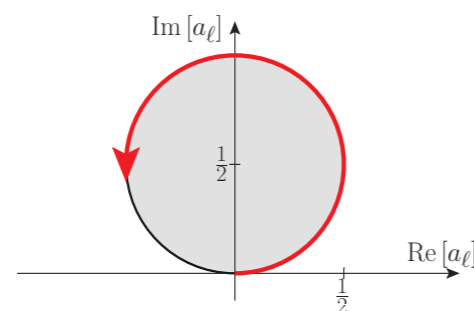
EFT+ Form-factor

2 Saturation



EFT elastic + T-Matrix

3 Resonance



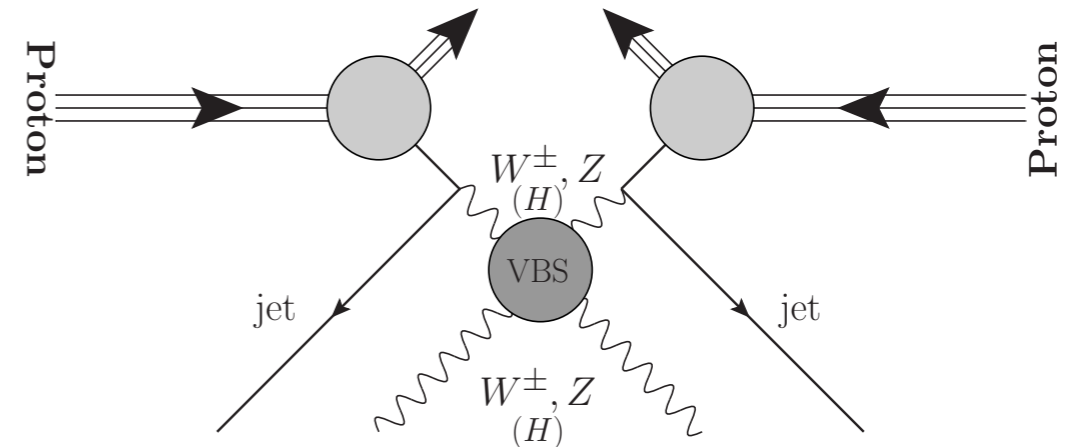
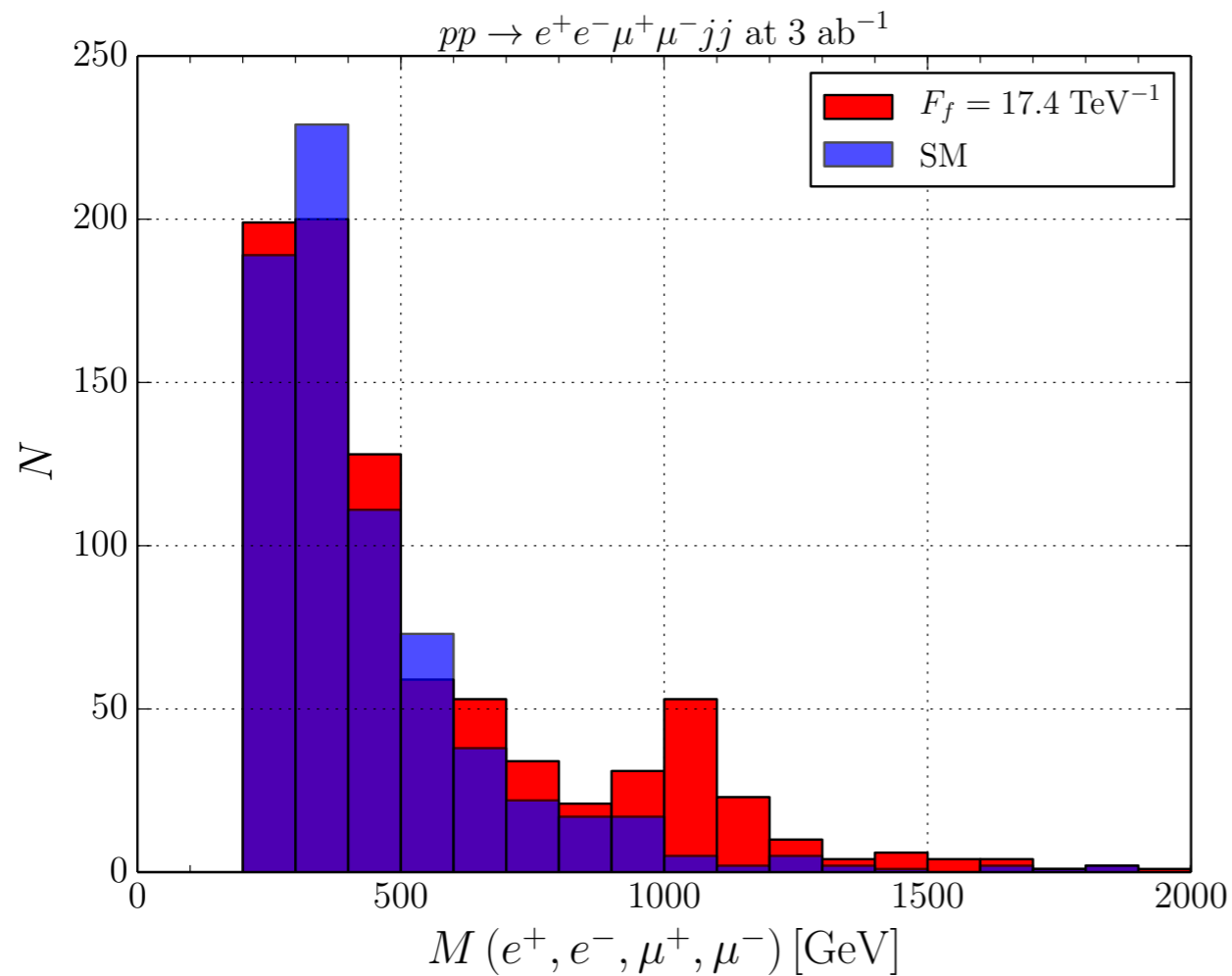
Adding additional resonances

Marco Sekulla



# Vector Boson Scattering

- \* Complete LHC process at 14 TeV in a simplified model with extra tensor resonance:



Marco Sekulla

# Theoretical status of the muon ( $g-2$ )

- \* Persistent deviation of 3.6 sigma:

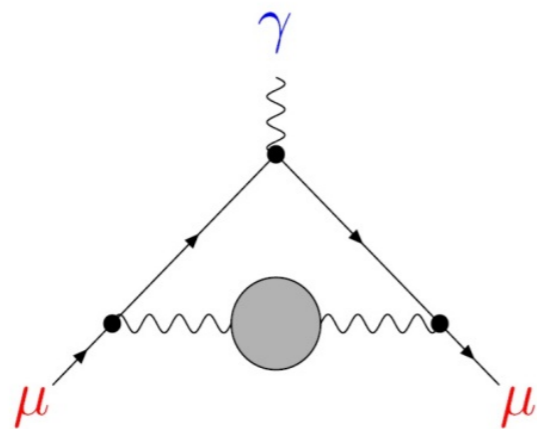
→ **Andreas Nyffeler**

$$a_\mu \equiv \frac{1}{2}(g-2)_\mu = \begin{cases} 116\,592\,080(54)(33) \cdot 10^{-11} & \text{E821 @ BNL} \\ 116\,591\,828(43)(26)(2) \cdot 10^{-11} & \text{SM prediction} \end{cases}$$

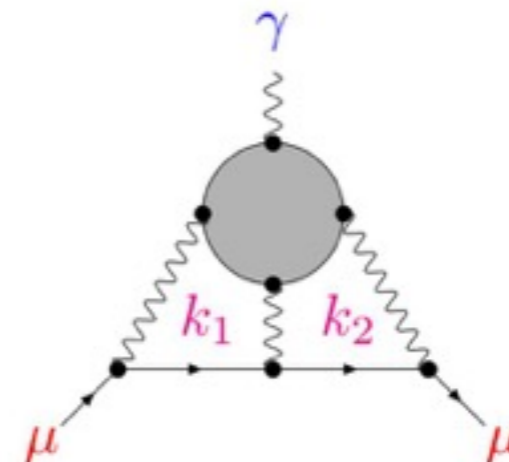
$$a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{weak}} + a_\mu^{\text{had}}$$

- \* Theoretical estimate dominated by QED
- \* Uncertainty of SM prediction dominated by QCD:

Hadronic vacuum polarisation:



Hadronic light-by-light scattering:

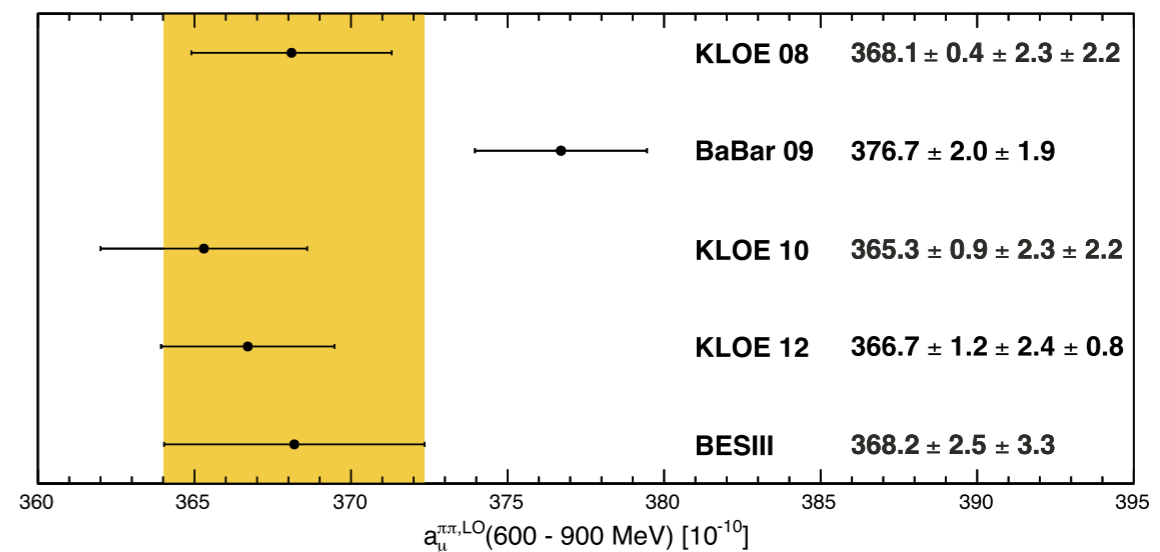
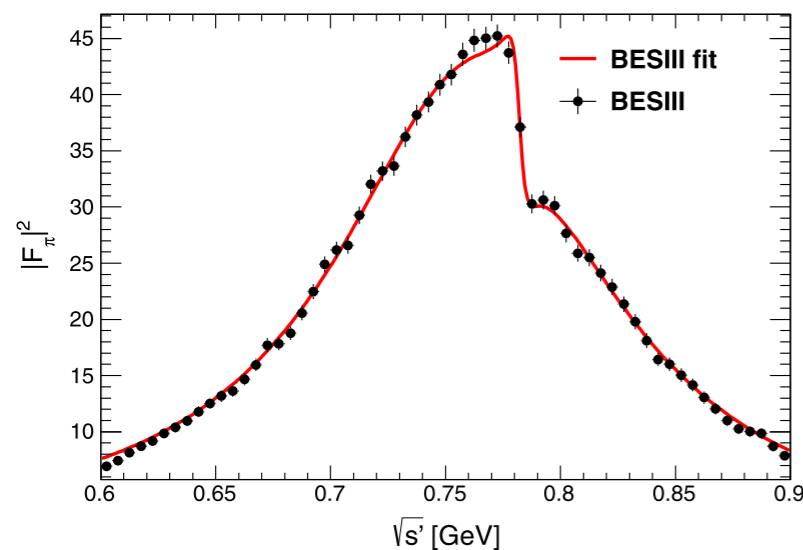


# Theoretical status of the muon ( $g-2$ )

## \* Dispersion relations:

$$a_{\mu}^{\text{hvp}} = \left(\frac{\alpha m_{\mu}}{3\pi}\right)^2 \left\{ \int_{m_{\pi}^2}^{E_{\text{cut}}^2} ds \frac{R_{\text{had}}^{\text{data}}(s) \hat{K}(s)}{s^2} + \int_{E_{\text{cut}}^2}^{\infty} ds \frac{R_{\text{had}}^{\text{pQCD}}(s) \hat{K}(s)}{s^2} \right\}$$

## \* Relies on experimental data for hadronic cross section $R_{\text{had}}(e^+e^- \rightarrow \text{hadrons})$



## \* New measurements of pion form factor by BESIII confirm $3.6\sigma$ tension

## \* Lattice QCD: Major effort in to compute $a_{\mu}^{\text{hvp}}$ ; Current precision: $O(5\%)$

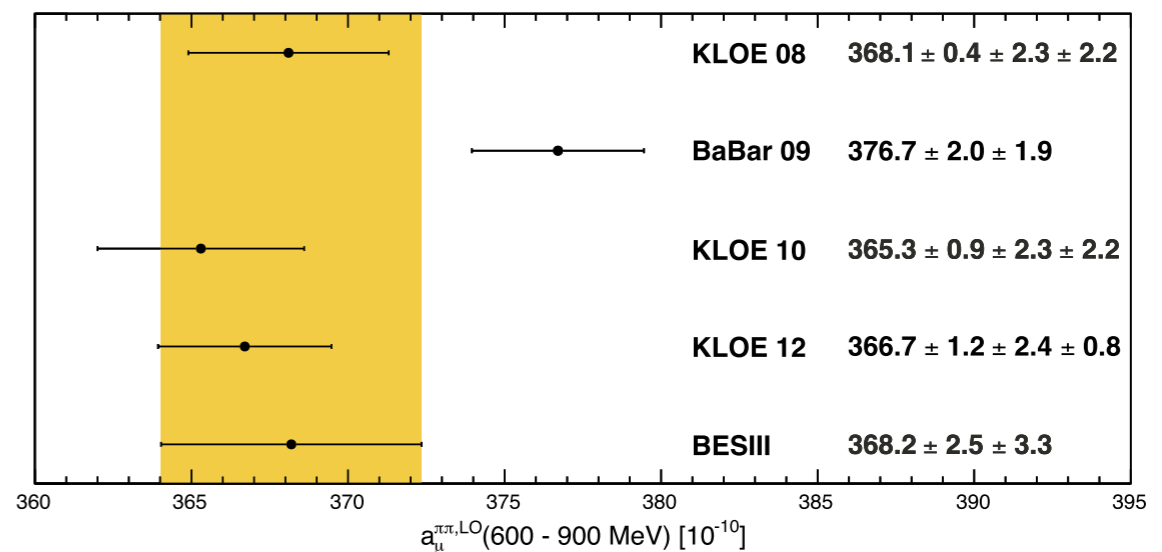
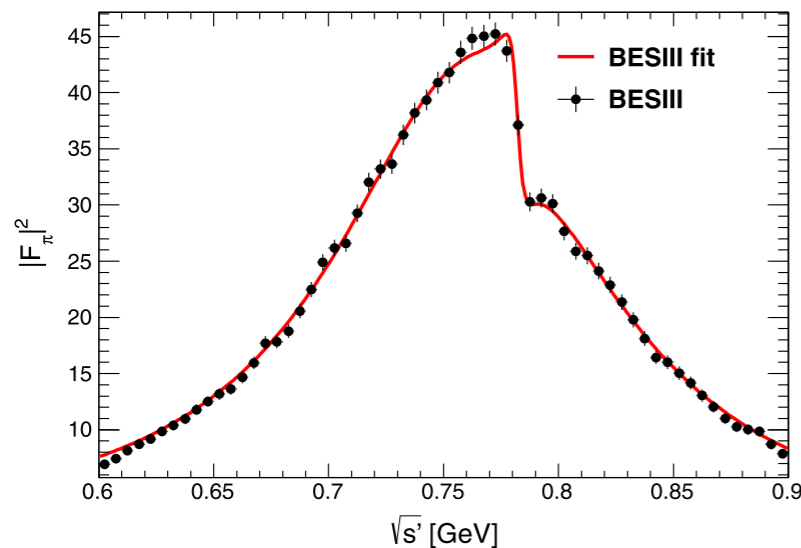
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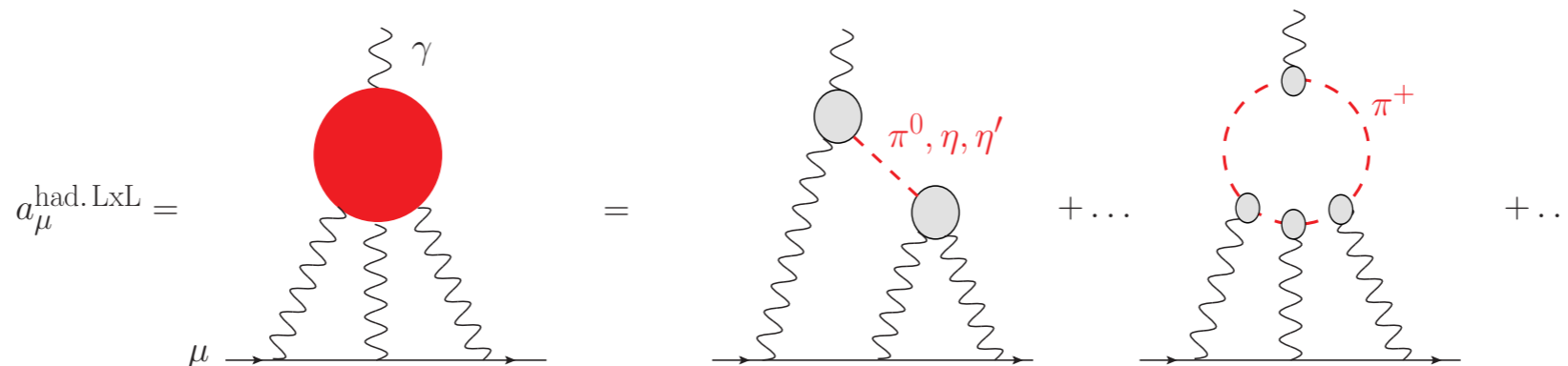


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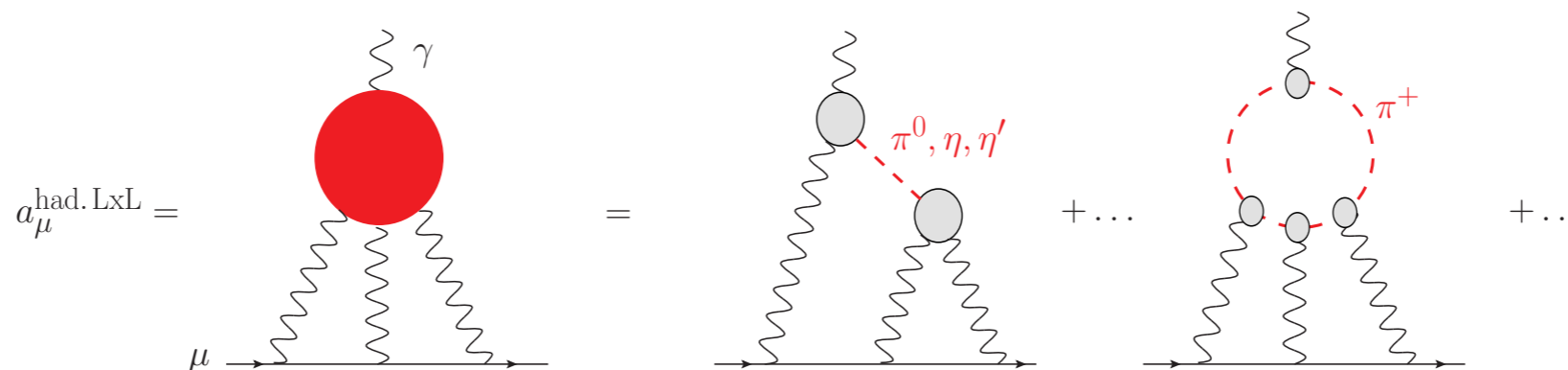


- \* Use hadronic models at low energies; exchange/loop contributions from resonances and dressed quark loops at high energies
- \* New approach: **Dispersion relations** to connect dominant light PS contributions to measurable form factors, e.g.  $\gamma^* \gamma^* \rightarrow \pi^0, \eta, \eta'$
- \* **Lattice QCD:** RBC/UKQCD Collab. (2005–2016), Mainz (2015/16)
- \* Various new physics scenarios to explain  $a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (290 \pm 90) \cdot 10^{-11}$   
SUSY @ large  $\tan \beta$ , dark photons,...

Andreas Nyffeler

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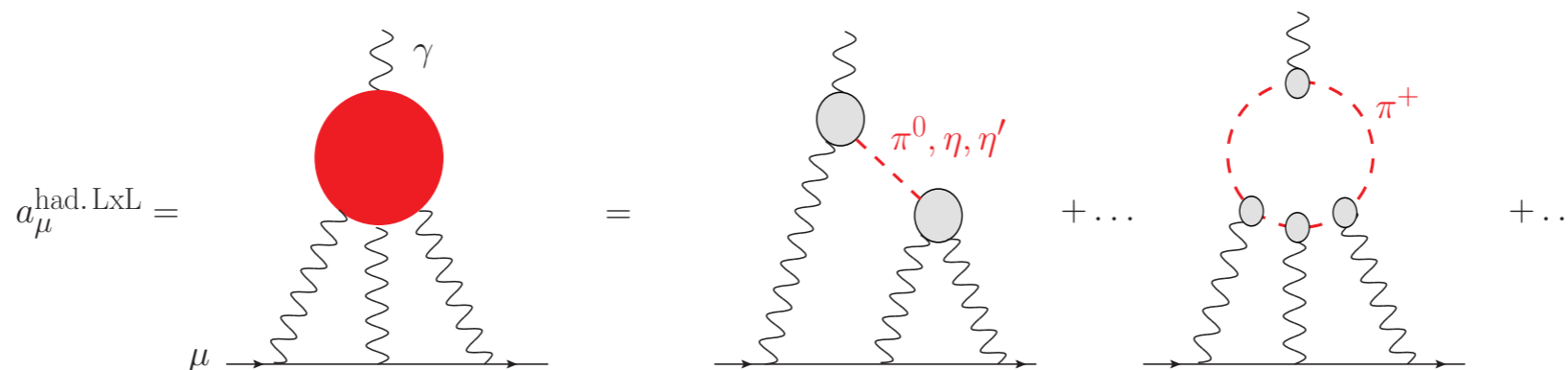


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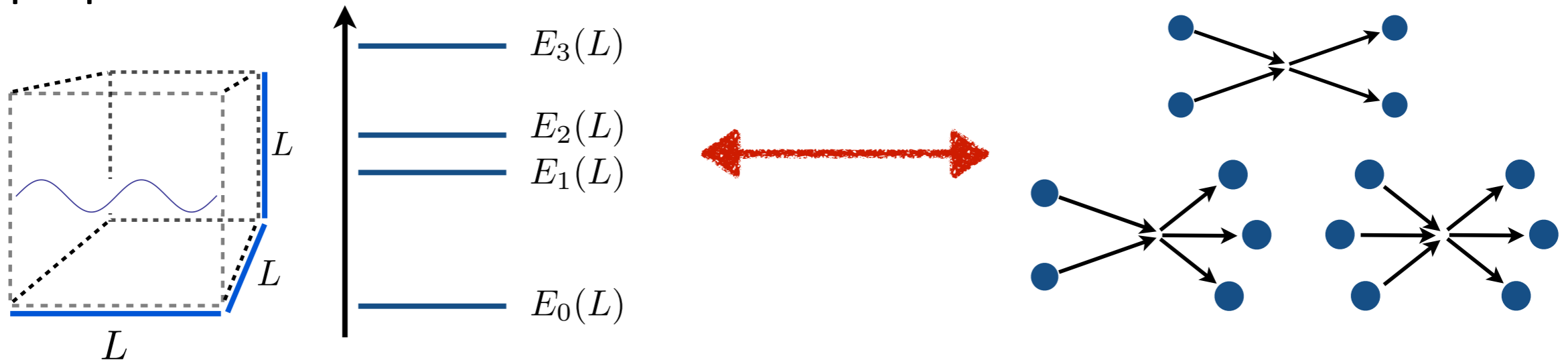
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Andreas Nyffeler

# Resonances and scattering in LQCD

- \* Impossible to compute scattering amplitudes directly in Lattice QCD → **Max Hansen**

- \* Can obtain energy levels in a finite box → relation to resonance properties



- \* (Generalised) Lüscher quantisation condition:

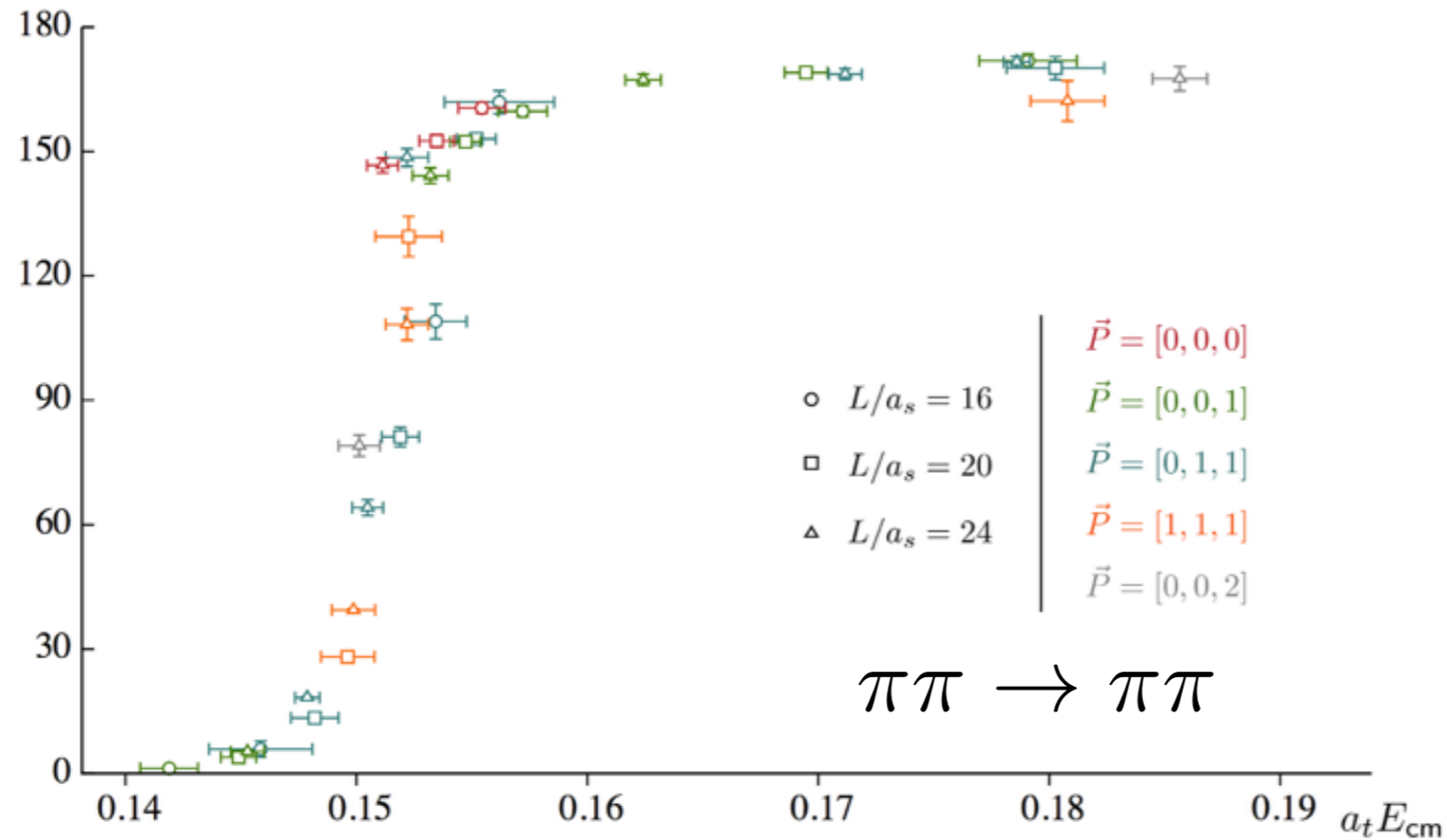
$$\det \left[ \underbrace{\mathcal{M}_2^{-1}(E_n^*)}_{\text{scattering amplitude}} + \underbrace{F(E_n, \vec{P}, L)}_{\text{known geometric function}} \right] = 0$$



# Resonances and scattering in LQCD

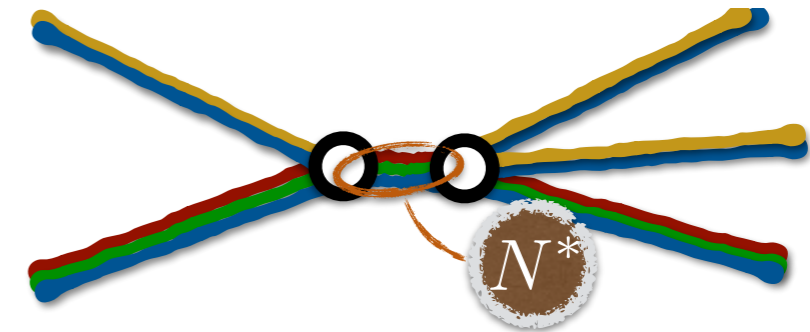
\* Simplest case: 2  $\rightarrow$  2 scattering

$$\cot \delta_{\ell=1}(E_n^*) + \cot \phi(E_n, \vec{P}, L) = 0$$

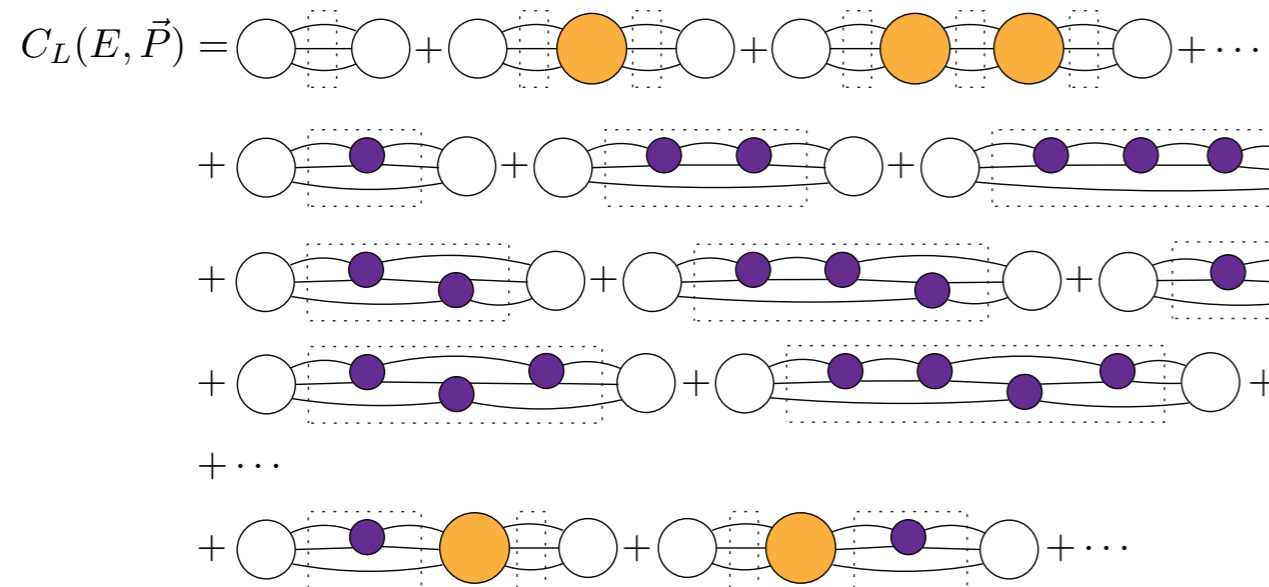


# Resonances and scattering in LQCD

- \* Derive generalisation for arbitrary two- and three-particle systems
- \* Relevant for 3-particle resonances, weak decay amplitudes  $K \rightarrow \pi\pi\pi, \dots$



- \* Formalism complete for simplest three-particle system



$$\det [\mathcal{K}_{\text{df},3}^{-1}(E_n^*) + F_3(E_n, \vec{P}, L)] = 0$$

Max Hansen

# Summary

## Many efforts to constrain BSM models

- Higgs mass calculations
- Vacuum stability
- Vector boson scattering
- Low-energy precision observables

## Methods

- Effective field theories, multi-loop calculations, lattice simulations

## Understand hadronic uncertainties

- strong coupling  $\alpha_s$ , hadronic contributions to  $(g-2)$